## The 10th 'vLTI School of Interferometry

## Fracties session I Interferometry Eseies aith nisfrib

## 2 Our first model : the uniform disk

It is now time to play with a first model. The one already loaded in the Examplel.asprox file is a uniform disk. It is the grounding of almost all interferometric-data analysis, and it is very often used, not only to perform stellar diameters fits, but also first-order interpretations of any extended objects.

## Question : What is the visibility function of a uniform disk?

Question : Give the expression of the first value for which the visibility becomes zero?
This corresponds to the interferometer spatial (or angular) resolution, i.e. the smallest object that can be fully resolved.

Question : Give the same expression with the stellar diameter and wavelength expressed in mas and $\mu \mathrm{m}$, respectively.
Now look at the OIFits viewer tab. Plot the visibility amplitude and phase (VISAMP and VISPHI) as a function of the baseline length (i.e. RADIUS in the software). To do so click on the three dot (...) button at the bottom-right corner, and then select the good X and Y Axes. Roughly measure on the plot the smallest baseline for which the visibility becomes zero and assume that the observations were made in the $B$ band (i.e., at $\lambda=0.46 \mu \mathrm{~m}$ ).

Question : What is our object diameter in mas?
Imagine that you obtained a single visibility measurement (i.e. for a single baseline) and assume that the studied object looks like a uniform disk.
Question : In which case(s) can you determine an unambiguous diameter?
Now look at the phase. It is always equal to $0^{\circ}$ or $180^{\circ}$. The jump between these two values happens when the visibility amplitude is equal to zero.
Question : Explain this phase signal.
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Targets

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## Notebook Map Observability UV coverage Olfits viewer

plot data

DEMO - DEMO $[0.460 \mu \mathrm{~m}$ - $\mathbf{0 . 4 6 0 ~} \mu \mathrm{m}]$ - SO-S1-S2-S3-S4-S5-S6-S7-S8-S9-S10-S11-S12-S13-S14-S15-S16
Day: 2010-09-21 - Source: 00:00:00.000 89:00:00.000




- Color by effective wav... $-\square$ Skip Flagged $\square$ Draw lines ...
(b) $\mathrm{A}|\mathrm{D}| \mathrm{F}$ Show VISAMP, VISPHI vs RADIUS


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Below this value there are other lobes of the visibility that match the same values.

## The object is centro-symmetric

Its Fourier Transform is Real
The phase is 0 (positive number) or $180^{\circ}$ (negative)

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3. Few other 1D distributions

### 3.1 Limb darkened disk

Question : Note the baseline length corresponding to the first zero of visibility and the secondlobe amplitude.

Now imagine you would estimate the size of this 4 mas limb-darkened star by measuring the position of the first zero of visibility and using the formula determined for a uniform disk in the previous section.
Question : Does the star appears bigger or small than its real size? Explain why.
Question : How can you discriminate between the uniform disk and the limb darkened disk?

### 3.2 Gaussian distribution

Change the model to a "gaussian" (remove previous), and click on Add. Look at the new set of parameters shown in the bottom part of the window. This model has also four parameters, i.e. flux_weightl, $x l, y l$ like for all models, and fwhml, the full width at half maximum of the Gaussian distribution. Let's set this value to 4 mas and then click on Ok to close the window.
Question : What is the Fourier transform of a Gaussian distribution?
Question : Compare the phase signal to that of the uniform disk.
Question : What is the baseline length corresponding to a visibility of 0 ?

### 3.3 Ring

Open the Target editor again, Remove the Gaussian model and Add a Ring model instead. This time the model has 5 parameters : flux_weight $1, x l, y l$, a diameter like the uniform disk, and also a width. Let's consider the case of a 4 mas infinitely-thin ring : diameter $1=4$, and width $1=0$.
Question : What are the baseline length corresponding to the first zero of visibility and the amplitude of the second lobe?

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Open the Target editor again, Remove the Gaussian model and Add a Ring model instead. This time the model has 5 parameters : flux_weightl, $x l, y l$, a diameter like the uniform disk, and also a width. Let's consider the case of a 4 mas infinitely-thin ring : diameter $1=4$, and width $1=0$.
Question : What are the baseline length corresponding to the first zero of visibility and the amplitude of the second lobe?

The star appears smaller although it has exactly the same size as before.
The light emission is more "concentrated" in the center due to the limb darkening.

## By measuring the $2^{\text {nd }}$ lobe amplitude

## A Gaussian distribution

The phase is always 0

The zero is at the infinity

Fractioe session I: Interferometry besiosuith fiFPo


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### 3.1 Limb darkened disk

## $\mathrm{B} \approx 32 \mathrm{~m}$ <br> Aplitude $\approx 0.092$

Question : Note the baseline length corresponding to the first zero of visibility and the secondlobe amplitude.

Now imagine you would estimate the size of this 4 mas limb-darkened star by measuring the position of the first zero of visibility and using the formula determined for a uniform disk in the previous section.
Question : Does the star appears bigger or small than its real size? Explain why.
Question : How can you discriminate between the uniform disk and the limb darkened disk?

### 3.2 Gaussian distribution

Change the model to a "gaussian" (remove previous), and click on Add. Look at the new set of parameters shown in the bottom part of the window. This model has also four parameters, i.e. flux_weightl, $x l, y l$ like for all models, and fwhml, the full width at half maximum of the Gaussian distribution. Let's set this value to 4 mas and then click on Ok to close the window.
Question : What is the Fourier transform of a Gaussian distribution?

## Question : Compare the phase signal to that of the uniform disk.

Question : What is the baseline length corresponding to a visibility of 0 ?

### 3.3 Ring

Open the Target editor again, Remove the Gaussian model and Add a Ring model instead. This time the model has 5 parameters : flux_weight $1, x l, y l$, a diameter like the uniform disk, and also a width. Let's consider the case of a 4 mas infinitely-thin ring : diameter $1=4$, and width $1=0$.
Question : What are the baseline length corresponding to the first zero of visibility and the amplitude of the second lobe?

The star appears smaller although it has exactly the same size as before.
The light emission is more "concentrated" in the center due to the limb darkening.

By measuring the $2^{\text {nd }}$ lobe amplitude

$B \approx 39 \mathrm{~m}$
Aplitude $\approx 0.4$

### 3.4 Comparison of these models

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Question : First, classify the models in term of sharpness/smoothness
Question : What is the relation between the distribution sharpness and the $2^{\text {nd }}$ lobe amplitude ?

### 3.5 Model confusion

If the interferometer largest spatial frequency (the ratio baseline length over wavelength) is not of the order of the typical size of your source, this may cause problems when you try to interpret your data.

Question : Compare the visibility obtained at 100 m for a 0.9 mas uniform disk and a 0.5 mas Gaussian distribution.
Now switch to the K band using the UV-Coverage tab and changing the Instrument mode.
Question : Do the same comparison.
Typical uncertainties on the visibility measurements are of the order of a few percent.
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Go back to the B band, and compare the visibility at 100 m from the 0.9 mas uniform disk and a 0.61 mas Gaussian distribution.
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### 3.6 Point source and flat field

There is two additional intensity distributions that are widely used for modelling :

- the point source used to model a source too small to be resolved whatever by the interferometer
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Note that these models are useless on their own and are only used to build multi-component models described further down.

Question : What are the point source and flat field visibility functions?
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## Sharpness in image $\Leftrightarrow$ higher lobes in FT

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plot data

DEMO - DEMO $[0.460 \mu \mathrm{~m}-0.460 \mu \mathrm{~m}]$ - S0-S1-S2-S3-S4-S5-S6-S7-S8-S9-S10-S11-S12-S13-S14-S15-S16 Day: 2010-09-21 - Source: 00:00:00.000 89:00:00.000


Longer baselines for 2nd lobe

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The visiblity are very similar at 100 m ( 0.23 ) Having measurements at multiple baselines length can help discriminate between these models + longer baselines for $2^{\text {nd }}$ lobe measurements

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FT(Point Source) : V=1
FT(flat field) : $V=1$ if $(B=0)$ and $V=0$ otherwise

## 4. Going 2D with flattened models

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In the previous sections you learned about 1D functions to model interferometric measurements. Now it is time to take a look at two-dimensional intensity distributions.

### 4.1 Elliptical distributions

Question : Compare its visibility function to the one obtained for the 4 mas uniform disk
Now modify the model so that the major-axis is oriented East-West.
Question : Where is the first zero of the visibility function?
Question : What uniform disk diameter does this correspond to?
Finally, put the disk major-axis at $45^{\circ}$.
Question : Can you conclude on the extension measured by an interferometer?
Now, let's use a new set of baselines. Load the configuration file Example2.asprox. Look at the UV plan in the UV coverage tab. The baselines in the new set all have the same length, i.e. 42 m , but they have different position angles, and cover all directions.
Go to the OIFits viewer tab and plot the Visibility (VISAMP and VISPHI) as a function of the position angle (POS_ANGLE).
Question : Without looking at the model can you determine the major-axis position angle?
Question : Assuming an elliptical Gaussian model what are the major and minor axes FWHMs?

### 4.2 Application to geometrically thin disk

Elliptical intensity distributions are widely used to model geometrically-thin circumstellar disks. In this case the flattening is due to the projection of the disk on the sky-plane, i.e., perpendicular to the observer line of sight. At an inclination angle of $0^{\circ}$, i.e. pole-on, the disk is not flattened, and the elongation ratio (i.e. major-axis/minor-axis) grows with the inclination angle.

Question : Find the formula of the elongation ratio for this simple geometrically thin disk model Question : Conclude on the inclination angle of our object.


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Interferometer DEMO Instrument DEMO_SPATIAL

Fractioe session

| Configuration(s) |  |  |
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Information

\section*{| Notebook | Map | Observability | UV coverage | Olfits viewer |
| :--- | :--- | :--- | :--- | :--- | :--- |}

plot data

DEMO - DEMO $[0.460 \mu \mathrm{~m}$ - $0.460 \mu \mathrm{~m}]$ - SO-S1-S2-S3-S4-55-S6-S7-S8-S9-S10-S11-S12-S13-S14-S15-S16 Day: 2010-09-21 - Source: 00:00:00.000 89:00:00.000


hide Kavelength: $0.460 \mathrm{um} \mid$ Spatial Freq: 63.03 Ma | Radius: $29.00 \mathrm{~m} \mid$ Pos. angle: 0.00 deg | Hour angle: 0.01 h
Infos:
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y Axes | VISAMP |
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| VISPHI |

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## Notebook Map Observability UV coverage Olfits viewer

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(es) $A|D| F$ Show VISAMP, VISPHI vs RADIUS

- Color by effective wav... $\quad \square$ Skip Flagged $\square$ Draw lines ... x Axis RADIUS V $\square \log \square$ inc. $0 \bigcirc$ auto $\bigcirc$ default $\bigcirc$ fixed
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## 4 Going 2D with flattened models

In the previous sections you learned about 1D functions to model interferometric measurements. Now it is time to take a look at two-dimensional intensity distributions.

### 4.1 Elliptical distributions

Question : Compare its visibility function to the one obtained for the 4 mas uniform disk Now modify the model so that the major-ax is is oriented East-West.
Question : Where is the first zero of the visibility function?
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Finally, put the disk major-axis at $45^{\circ}$.
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Now, let's use a new set of baselines. Load the configuration file Example2.asprox. Look at the UV plan in the UV coverage tab. The baselines in the new set all have the same length, i.e. 42 m , but they have different position angles, and cover all directions.
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### 4.2 Application to geometrically thin disk

Elliptical intensity distributions are widely used to model geometrically-thin circumstellar disks. In this case the flattening is due to the projection of the disk on the sky-plane, i.e., perpendicular to the observer line of sight. At an inclination angle of $0^{\circ}$, i.e. pole-on, the disk is not flattened, and the elongation ratio (i.e. major-axis/minor-axis) grows with the inclination angle.
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> The baseline is North-South oriented and so it "sees" The major-axis of the Elongated disk

Twice as far, i.e., $\mathrm{B}=58 \mathrm{~m}$
Now the baseline is oriented along the minor-axis

## 2mas

At $45^{\circ}$ we found 3.1 mas, an intermediate value between the major and minor axes.
The interferometer only measures extension along the baseline orientation


## Notebook Map Observability UV coverage Olfits viewer


DEMO - DEMO [0.460 $\mu \mathrm{m}$ - $0.460 \mu \mathrm{~m}]$ - S0-S7 Day: 2013-09-06 - Source: 00:00:00.000 89:00:00.000


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Using the FT given in the cheatsheet for the Gaussian

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\mathrm{fwhm} \approx 1.66 \sqrt{-\ln V} \frac{\lambda}{\pi B} \Leftrightarrow f w h m=1 \text { and } 0.5
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Imagine that your model is a weighted sum of N components :

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where $I_{i}(x, y)$ is the intensity distribution of the $\mathrm{i}^{\text {th }}$ component and $f_{i}$ its relative flux with $\Sigma f_{i}=1$.
Question : What is the visibility function (i.e. normalized Fourier Transform) for this model?

### 5.1 Star + circumstellar disk model

Let's look at a simple star + circumstellar disk example. First, load a new observation file : Example3.asprox. Go to the UV coverage tab and look at it (again remove the annoying Plot rise/set uv tracks option). It is composed two perpendicular strips of baselines : one North-South and one East-West. It will allow us to probe our object along these two perpendicular orientations.
Now, open the Target Editor and create a two components model composed of a 0.5 uniform disk (for the star) and an elliptical Gaussian distribution (for the circumstellar disk), with a 8 mas majoraxis oriented North-South and a 4 mas minor-axis. Put the flux contribution of each component to $50 \%$.
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Targets

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| Interferometer | demo | $\checkmark$ |
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| Instrument | demo_spatial |  |

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Night restriction $\square$ Date 2013/09/06 Min. Elevation 30 Wind $\square$
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\section*{| Notebook Map Observability UV coverage OFFits viewer |
| :--- | :--- | :--- |}


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Radius: $25.00 \mathrm{~m} \mid$ Poo, angle: $90.00 \mathrm{deg} \mid$ Hour angle: -5.99


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the level of the plateau between the baselines resolving the Gaussian and the ones resolving the Uniform disk have changed. This plateau allows to make a direct measure of the relative flux of the two components of our model.

Baselines shorter than the plateau : B < 20 m
Disk elongated $\Leftrightarrow$ Baselines in many orientations.

No. The star start to be significantly resolved for baselines larger than 60 m .

### 5.2 Binaries

A second kind of very useful two components model is the binary model. We will use a single strip of North-South aligned baselines to exlpore this model. So, load the Example1.asprox file.
Then, open the Target Editor and create a model consisting of two point sources. Set their flux to 0.2 and 0.8 . Look at the second component, the $x 2$ and $y 2$ parameters have been replaced by sep 2 and pos_angle 2 , i.e. polar coordinates. Choose sep $2=5$ and pos_angle $2=0$. This simulates two unresolved stars separated by 5 mas in the North-South orientation, i.e. aligned with our baselines.

Question : Describe and explain the visibility function.
Write down the amplitude of the sinusoidal modulation. Set the filux ratio to $0.1 / 0.9$ and then to $0.5 / 0.5$.
Question : What is the link between the flux ratio and the amplitude of the binary modulation?
Write down the modulation period in meter, and express it in $\mathrm{B} / \lambda$ units (cycles/rad). Then set the binary separation, i.e. sep2, to 10 mas. and do this again.

Question : Give the relation between the binary separation (in rad) and the modulation period (in cycles/rad).
Now change theta2 to $90^{\circ}$ : binary in the East-West orientation.
Question : Describe and explain the visibility function.
Do the same but with theta2 equal to $30^{\circ}, 45^{\circ}$, and $60^{\circ}$.
Question : How does this affect the visibility function? Why?
Finally replace the components by uniform disks and try various diameters between 0 and 2 mas, for each component, separately.
Question : What is the effect of resolving one component on the visibility function?

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Question : Give the relation between the binary separation (in rad) and the modulation period (in cycles/rad).

Now change theta2 to $90^{\circ}$ : binary in the East-West orientation.
Question : Describe and explain the visibility function.
Do the same but with theta2 equal to $30^{\circ}, 45^{\circ}$, and $60^{\circ}$.
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Finally replace the components by uniform disks and try various diameters between 0 and 2 mas, for each component, separately.
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It is a convolution of two distributions in the image plane, so in the Fourier plane it amounts to a mutiplication of the binary pattern with the FT of a disk, i.e., a Bessel function

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In this session, we will use a N band image of a dusty disk surrounding a massive hot star generated with the radiative transfer code MC3D developed by Sebastian Wolf.
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Question : what is the field of view (the size) of this image?
Play with the zooming and the color scale.
Question : Can you explain the shape of the intensity distribution?
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## Notebook Map Observability UV coverage OlFits viewer

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As the object intensity distribution has no sharp edge beside the inner rim that is very small compared to the object extension, its visibility function is closer to that of a Gaussian distribution.


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Up to now we've been working with simple geometric models. But one might want to use homemade models such as outputs from radiative transfer codes. For that purpose ASPR02 allow us to upload images in fits format and computes the visibility corresponding to this model and the selectel interferometer and instrument configuration.
In this session, we will use a N band image of a dusty disk surrounding a massive hot sta/ generated with the radiative transfer code MC3D developed by Sebastian Wolf.
First, load the Example3.asprox file to have two strips of perpendicular baselizes. Then, open the Target Editor. In the Model tab, choose User Model and then click on the pen button. Go to the models sub-directory and choose the HD62623.fits file. After selecting the file you should see the image in the Target Editor window.

Question : what is the field of view (the size) of this image?
Play with the zooming and the color scale.
Question : Can you explain the shape of the intensity distribution?
Close the Target Editor window, and go to the UV Coverage tab to select the N band. Look at the 2D Fourier transform of the image overplotted on the UV Coverage plot.
Finally, go back to the OiFits viewer tab to see North-South and East-West cuts of the 2D-visibility function. As before, plot VISAMP \& VISPHI as a function of RADIUS.
Question : Is the visibility function closer to that of a Gaussian distribution or uniform disk?
Question : What are the values of the visibility in the two orientations for a 20 m baseline?
Question : Using these values estimate the objects extension in the North-South and East-West orientations.

Question : Assuming that the disk is geometrically thin what is the object inclination angle?

## 227 mas

We see the inner rim of the dusty disk, the disk emission in N band, and some central emission which correspond to the central star.The disk is flattened which is a hint that it is not seen pole-on.

As the object intensity distribution has no sharp edge beside the inner rim that is very small compared to the object extension, its visibility function is closer to that of a Gaussian distribution.


$$
\begin{gathered}
\text { Elong }=1 / \cos \text { (incl.) } \\
\text { Elong }=45.4 / 34.7=1.31 \\
\text { } \operatorname{lncl} \approx 40^{\circ}
\end{gathered}
$$

## 6 Effect of the Wavelength

## 6 Effect of the observed wavelength

### 6.1 Achromatic objects observed at various wavelengths

The spatial resolution of an inteferometer strongly depends on the observing wavelength. Imagine that our North-Pole interferometer is able to observe in any photometric band between $0.46 \mu \mathrm{~m}$ (B) and $12 \mu \mathrm{~m}(\mathrm{~N})$.
Question : Which band will give the highest resolution?

To change the observing wavelength go to the UV Coverage tab. You can select a photometric band between B and N in the Instrument mode list.
Question : Give the ratio between the resolutions in $\mathbf{N}$ and B bands
Let's assume a 0.05 uncertainty on our visibility measurement and three baselines of 50,70 and 100 m .

Question : In which band should we observe a 1 mas star?
Question : Should we observe a 5 mas star with the same configuration?
Now, let's do a multi-wavelength observation. First load the Example4.asprox file. It contains a 3 telescopes (S0-S5-S16) configuration of baselines. Unlike for the other exercices the observing wavelength is not fixed to one band but ranges between $0.1 \mu \mathrm{~m}$ to $10 \mu \mathrm{~m}$, the "Wide" (and fake) instrument mode of the UV Coverage panel.

Note that for this observation we use a 1 mas uniform disk model.
First plot the visibility and phase as a function of the baseline length to see the visibility of the three baselines.

Question : Explain why we obtain a large range of values for the visibility of each baseline.
Now plot the visibility as a function of the spatial frequency $\mathrm{B} / \lambda$ (SPATIAL_FREQ). The different colors correspond to different wavelengths from purple for the smallest one $(0.1 \mu \mathrm{~m})$ to red for the largest one ( $10 \mu \mathrm{~m}$ ).
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## Notebook Map Observability UV coverage Olfits viewer

plot data
DEMO - DEMO $[0.460 \mu \mathrm{~m}-0.460 \mu \mathrm{~m}]$ - SO-S1-S2-S3-S4-55-S6-S7-S8-S9-S10-S11-S12-S13-S14-S15-S16
Day: 2013-09-06 - Source: 00:00:00.000 89:00:00.000


原 olfits done.

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No, it would be overresolved by the 50 m baseline. The star should be observed in the J, H, K, or L bands.

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For the same baseline length, observing at different $\lambda$ leads to probing different spatial frequencies.

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Fractioe session I: Interferonetry wesiosithen FFor


## Notebook Map Observability UV coverage Olfits viewer

 plot data```
DEMO - DEMO [0.1025 \mum - 9.9975 \mum] - SO-S6-S16
```

Day: 2013-09-10 - Source: 00:00:00.000 89:00:00.000

This that case it is strictly equivalent to observing with different baselines lengths. It helps a lot to enhance the UV coverage.



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### 6.2 Examples of chromatic objects

Question : Assuming that a star and its circumstellar environment emit as black-bodies, can you conclude on their flux ratio dependence on the wavelength? Which component will dominate the visible flux? What about the mid-infrared?

Question : How does the model depend on the wavelength?
Before closing the Target Editor let's rotate our model by $90^{\circ}$ so that our 3 North-South baselines will make measurements along the major-axis (i.e. the equator) of this object. Now, close the Target Editor and go to the OiFits Viewer tab.
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Question : Is the object more extended in the visible $(0.5 \mu \mathrm{~m})$ or the mid-infrared $(10 \mu \mathrm{~m})$ ?
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The central star (hotter, but of smaller angular size) will dominate on the short wavelength, and gradually the cooler but much larger environment will take its place when the wavelength increases.

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DISCO model taken from the AMHRA website https://amhra.oca.eu/AMHRA/disco-gas/input.htm

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The size of the circumstellar disk emission grows with $\lambda$. Its relative contribution to the total flux is also growing with the $\lambda$.
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 Instrument DEMO_3T_SPECTRAL $\rightarrow$ 50 S6 516 -

Night restriction $\square$
Date 2013/09/10Min. Elevation 30 Wind $\square$ status: A Warning

## Notebook Map Observability UV coverage OIfits viewer

plot data
DEMO - DEMO $[0.4763 \mu \mathrm{~m}-9.9975 \mu \mathrm{~m}]$ - SO -S6-S16
Day: 2013-09-10 - Source: 00:00:00.000 89:00:00.000




( $\rightarrow$ A D F Show VISAMP, VISPHI vs SPATIAL_FREQ
$\qquad$
$\square$

- $\square$ Skip Flagged $\square$ Draw lines x Axis SPAIIAL_RREQ
- $\square \log \square$ inc. 0
auto $\bigcirc$ default $\bigcirc$ fixed
Axes $\frac{\text { VISAMP }}{\text { VISPHI }}$
- $\square \log \square$ inc. $0 \bigcirc$ auto $\bigcirc$ default $\bigcirc$ fixed
$\sqrt{10}$ olfits done.


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The object is more extended at $10 \mu \mathrm{~m}$ where the large circumstellar disk dominates the emission

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Fractioe session I: Interferometry besiosuith fiFPo
Targets

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Interferometer DEMO
Instrument DEMO_3T_SPECTRAL
$\checkmark$

- S0 56 S16
Night restriction $\square$
plot data DEMO - DEMO [0.4763 $\mu \mathrm{mm}-9.9975 \mu \mathrm{ml}]$ - SO-S6-S16
Day: 2013-09-10 - Source: 00:00:00.000 89:00:00.000


## $V=0 \Leftrightarrow$ Spatial Frequency $B / \lambda=158.3 M \lambda$


$1 5 0 \longdiv { 1 6 6 . 5 1 4 }$
$\theta \approx 250 / 158.3 \approx 1.58 \mathrm{mas}$





SPATIAL_FREQ (M ${ }^{120}$

hide Wavelength: 0.6279 mm | Spatial Freq: 156 . $30 \mathrm{ma} \mid$ Radius: $100.99 \mathrm{~m} \mid$ Pos. angle: -0.00 deg | Hour angle: 0.01 h

Infos:
$\begin{aligned} & \text { दf } A|D| F \\ & \text { Show VISAMP, VISPHI vs SPATIAL_FREQ }\end{aligned}$
$\qquad$

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Plot the visibility and phase as a function of the spatial frequency. For chromatic objects, such plots mix-up the spatial and spectral dependency of the object. To disentangle these aspects you can draw imaginary lines between points of the same colour (i.e. wavelengths) : this will gives you information on the object spatial distribution at each wavelength.
Question : Is the object more extended in the visible $(0.5 \mu \mathrm{~m})$ or the mid-infrared $(10 \mu \mathrm{~m})$ ? Question : Assuming that the star is a uniform disk, estimate the stellar diameter in mas Question : Assuming a distance of 60 pc give the stellar Radius in $\mathbf{R}_{\odot}$.

The central star (hotter, but of smaller angular size) will dominate on the short wavelength, and gradually the cooler but much larger environment will take its place when the wavelength increases.

The size of the circumstellar disk emission grows with $\lambda$. Its relative contribution to the total flux is also growing with the $\lambda$.

The object is more extended at $10 \mu \mathrm{~m}$ where the large circumstellar disk dominates the emission
$V=0$ for $B / \lambda \approx 158.3 \Leftrightarrow \theta \approx 1.58$ mas

### 6.2 Examples of chromatic objects

Question : Assuming that a star and its circumstellar environment emit as black-bodies, can you conclude on their flux ratio dependence on the wavelength? Which component will dominate the visible flux? What about the mid-infrared?

## Question : How does the model depend on the wavelength?

Before closing the Target Editor let's rotate our model by $90^{\circ}$ so that our 3 North-South baselines will make measurements along the major-axis (i.e. the equator) of this object. Now, close the Target Editor and go to the OiFits Viewer tab.
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The central star (hotter, but of smaller angular size) will dominate on the short wavelength, and gradually the cooler but much larger environment will take its place when the wavelength increases.

The size of the circumstellar disk emission grows with $\lambda$. Its relative contribution to the total flux is also growing with the $\lambda$.

The object is more extended at $10 \mu \mathrm{~m}$ where the large circumstellar disk dominates the emission

$$
\mathrm{V}=0 \text { for } \mathrm{B} / \lambda \approx 158.3 \Leftrightarrow \theta \approx 1.58 \mathrm{mas}
$$

$1^{\prime \prime}=1$ au at 1 pc.
1au $\approx 107$ Dsol
Rstar $\approx 0.107 \times$ distance (in pc) $\times \theta$ (in mas) Rstar $\approx 10$ Rsol

## 7 Bonus

### 6.3 Bonus : play with the models from the AMHRA service

You can go to the AMHRA service web page, download models and load them on ASPRO2. Currently, AMHRA gives access to the following models:

- Kinematic Be Disk: Model of the geometry (size and shape) and kinematics (rotation and expansion) of circumstellar disks, especially of Be stars observed at high spectral resolution ( $\mathrm{R}>1000$ ). It is not adapted to our DEMO interferometer that does not have a high spectral resolution mode. But you might test it with GRAVITY (in $\operatorname{Br} \gamma$ line) or MATISSE (in $\operatorname{Br} \alpha$ line)
- Disk and stellar Continuum DISCO : we already used it, but you might want to compute model with different paramters.
- Evolved stars (Red Supergiants and AGBs): Stellar surface maps of evolved stars computed from 3D hydrodynamical simulation with C05B0LD-OPTIM3D
- Binary spiral model : Phenomenological model mimicking the shock caused by the collision between the winds from massive stars (e.g. the WR and OB stars)
- Supergiant $B[e]$ stars with HDUST : Grid of models for $B[e]$ supergiants, i.e. hot stars surrounded by gaseous and dusty circusmtellar disk.


