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# Astrometry with HST

Gerard van Belle  
PRIMA Instrument Scientist  
3 Jun 2008

(with substantial inputs from – and thanks to –  
Fritz Benedict)



# Why HST FGS?

- Calibrating the Galactic Cepheid period-luminosity (PL) relationship were primary missions of the space astrometric satellites FAME and DIVA
  - FAME and DIVA got cancelled
- The very distant promise of the Space Interferometry Mission and GAIA
  - SIM, to be launched in 2015(?), with preliminary results due by 2018
  - GAIA, launch in 2012 and final results by 2020
- Benedict et al proposed to reintroduce Galactic Cepheids as a fundamental step in the extragalactic distance scale many years before our other space-based competition
- **Only** means to do  $\sim$ mas astrometry on faint sources



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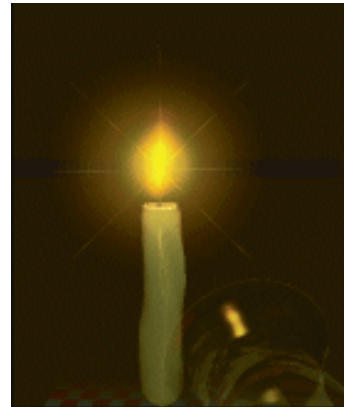


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# Why Important?

## Cepheid are attractive Standard Candles

- Cepheids are among the brightest stellar distance indicators
- These `standard candles' are relatively young stars, found in abundance in spiral galaxies
- For extragalactic distance determinations many independent objects can be observed in a single galaxy
- Their large amplitudes and characteristic (sawtooth) light curve shapes facilitate their discovery and identification



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# Why Important?

## Cepheids are easy to observe

- Cepheids have long lifetimes, and hence can be re-observed at other times and other wavelengths (unlike supernovae, for example)
- The Cepheid PLR has a small scatter. In the I band, the dispersion amounts to only  $\sim 0.1$  mag (Udalski et al. 1999)
- Fortunately (for Benedict et al!), an accurate geometric calibration of the PL relation, at any given metallicity, had not yet been established



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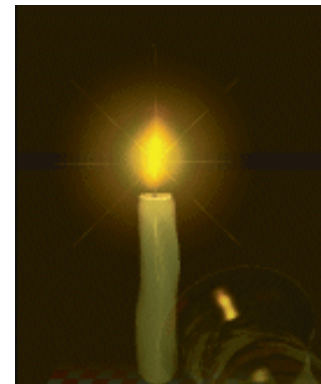


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# Why Important?

Current calibration is leveraged thru LMC/SMC

- Cepheid absolute magnitude apparently depends on metallicity
  - LMC and SMC have non-solar metallicities
- Intent of Benedict et al. was to produce a PLR calibration using solar metallicity Cepheids
  - A solar metallicity PLR can be applied directly to extragalactic Cepheids
- This will remove the need to step through the LMC/SMC
- Very few long-period local Cepheids have distances measured
  - $\ell$  Car is ideal ( $P \sim 35^d$ )
  - Will be treated as a illustrative example for this talk



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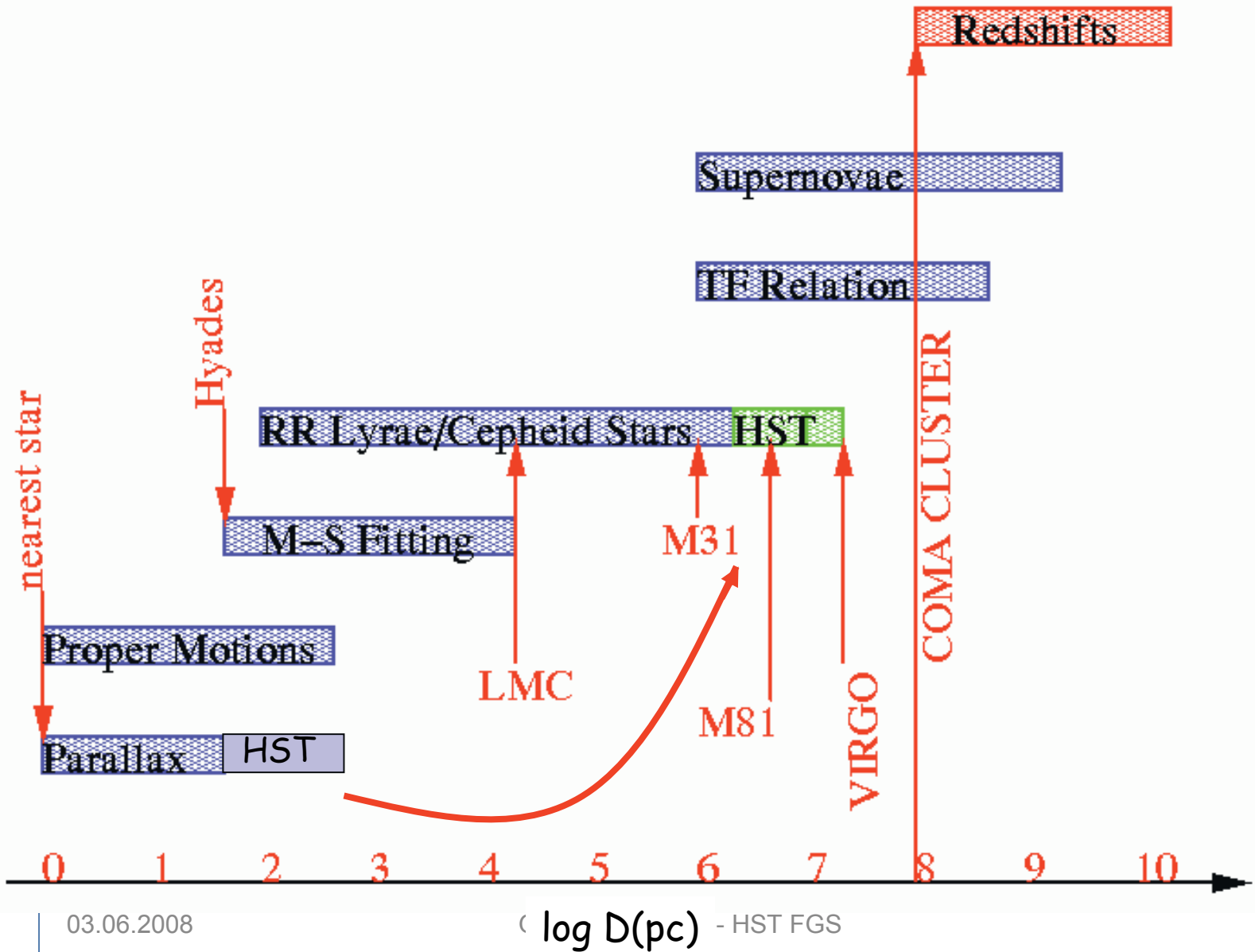
# The Distance Scale Ladder



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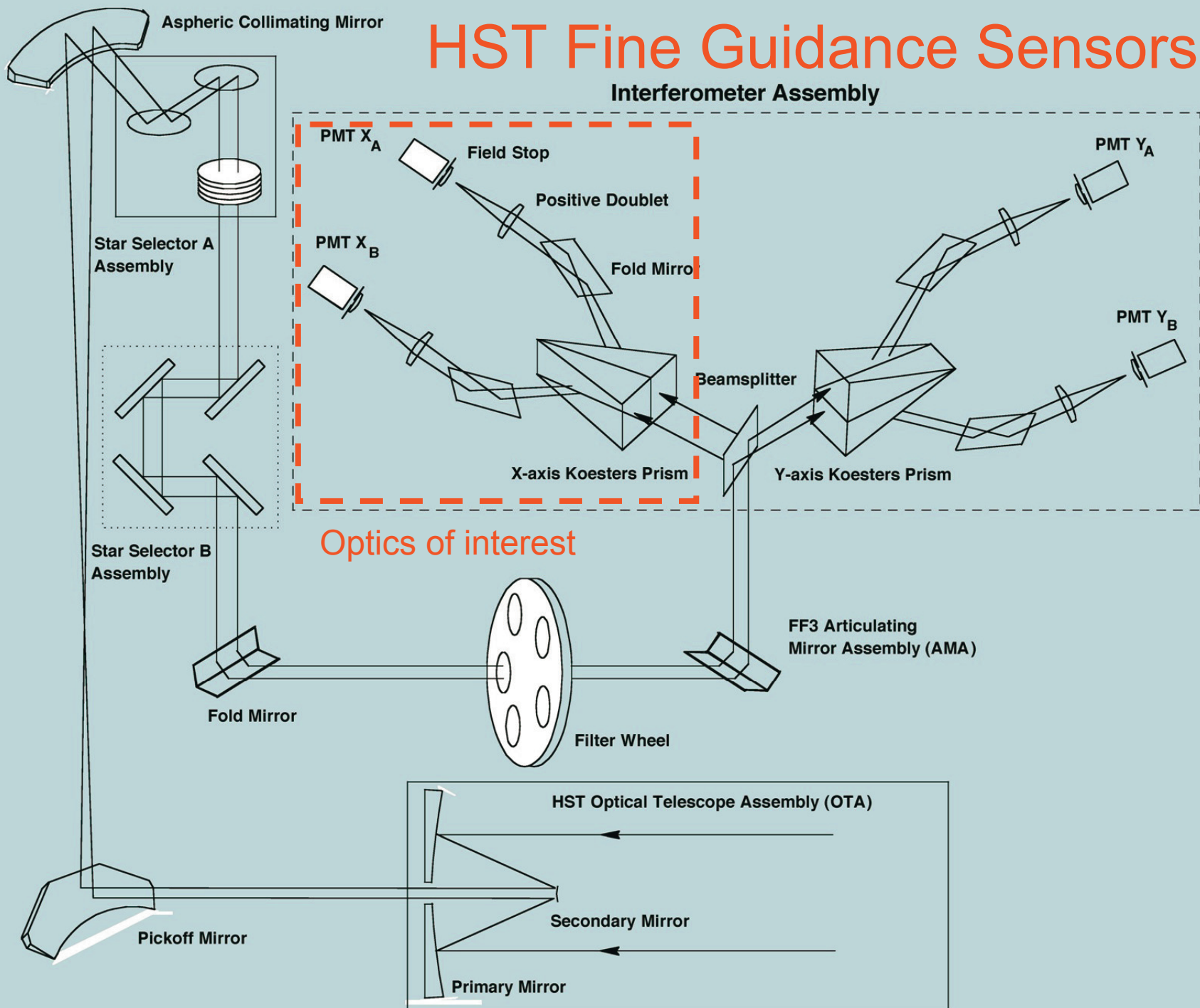


1997:02:19 07:06:57



# HST Fine Guidance Sensors

## Interferometer Assembly



Optics of interest



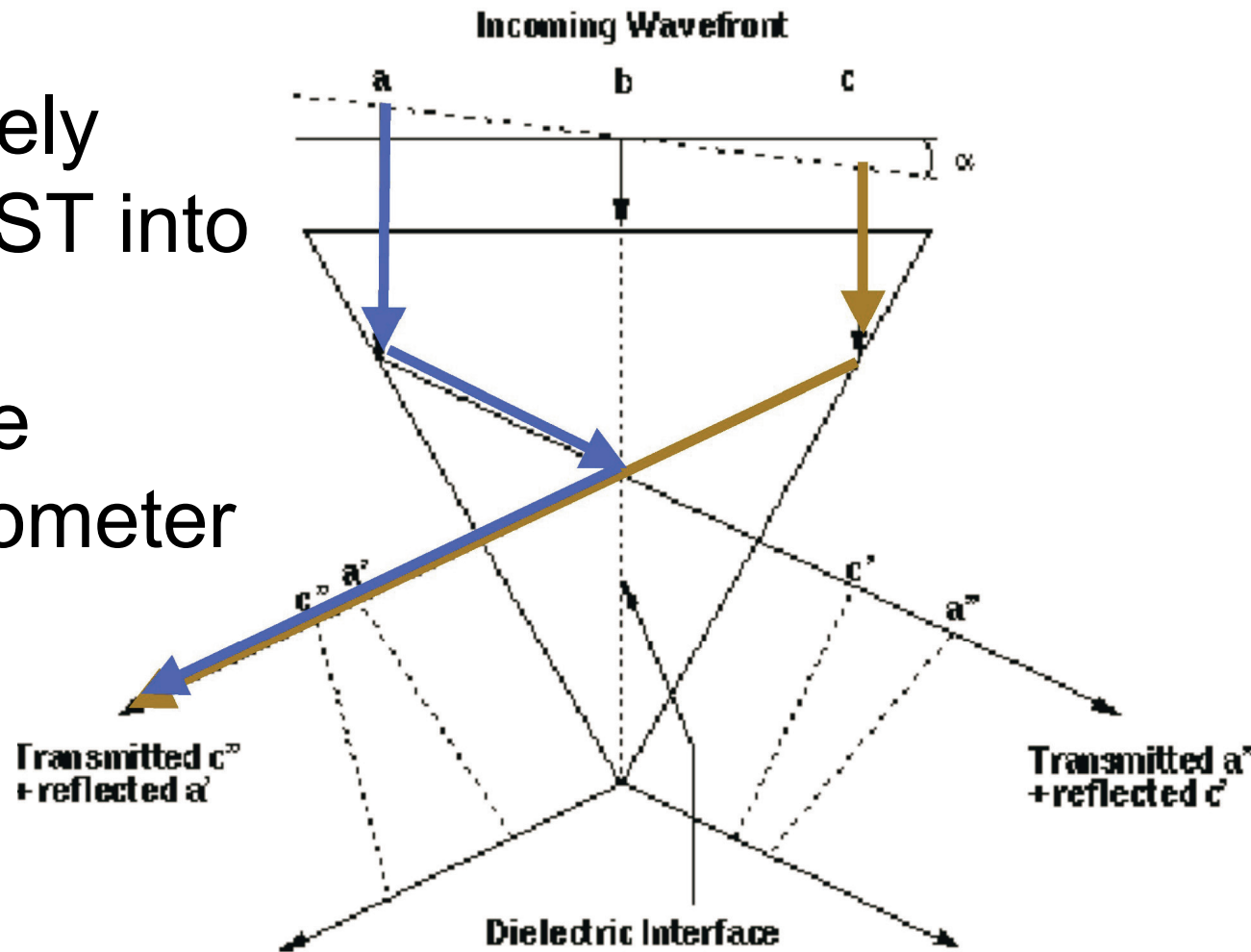
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# FGS Kösters Prism

- Effectively turns HST into a 2.4m baseline interferometer



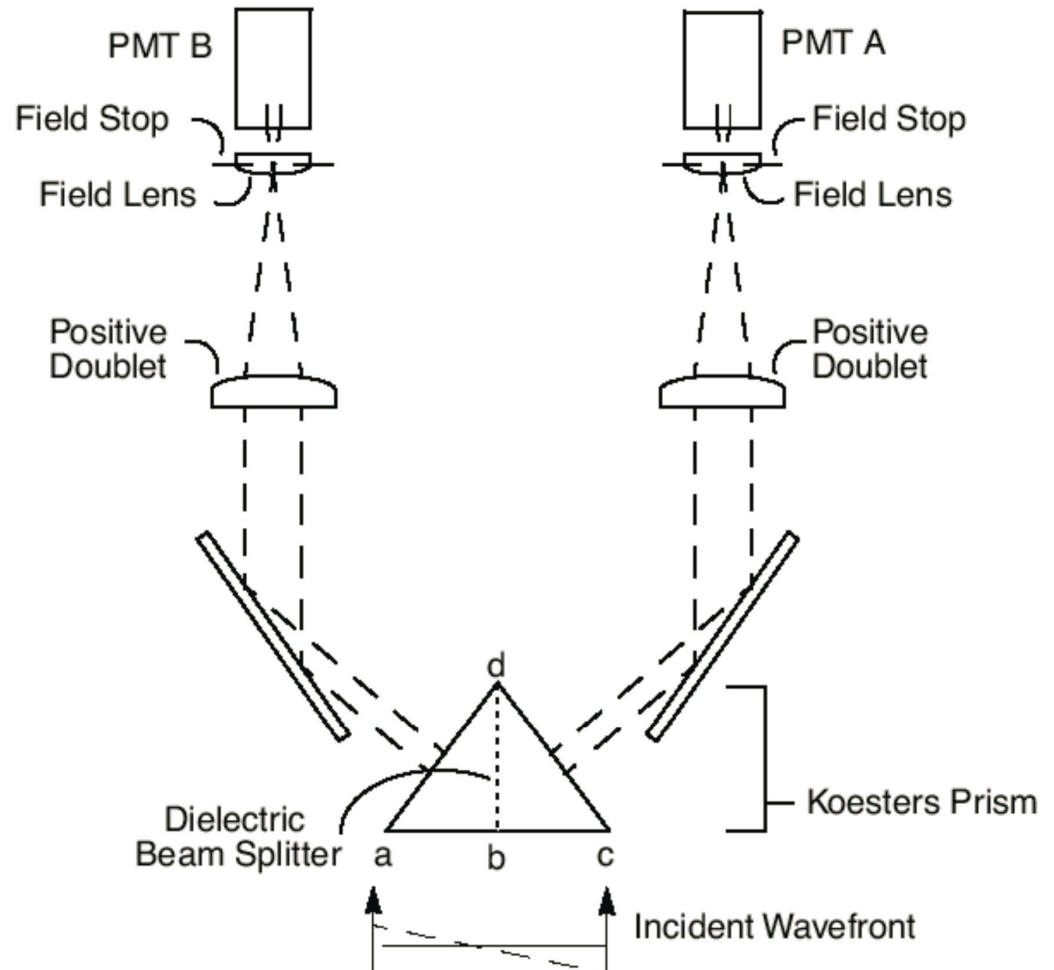
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# FGS PMT Detectors

- Two PMTs sample interference signal



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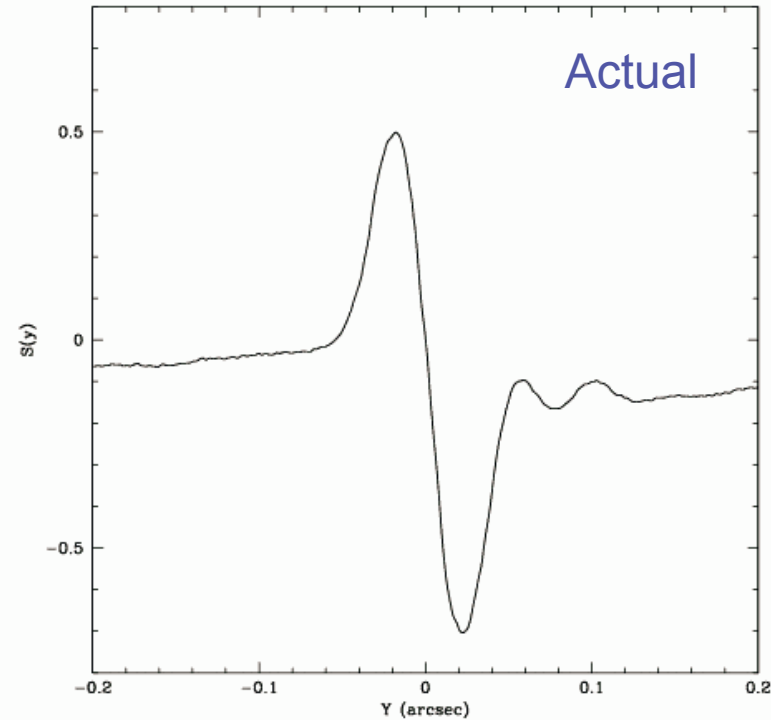
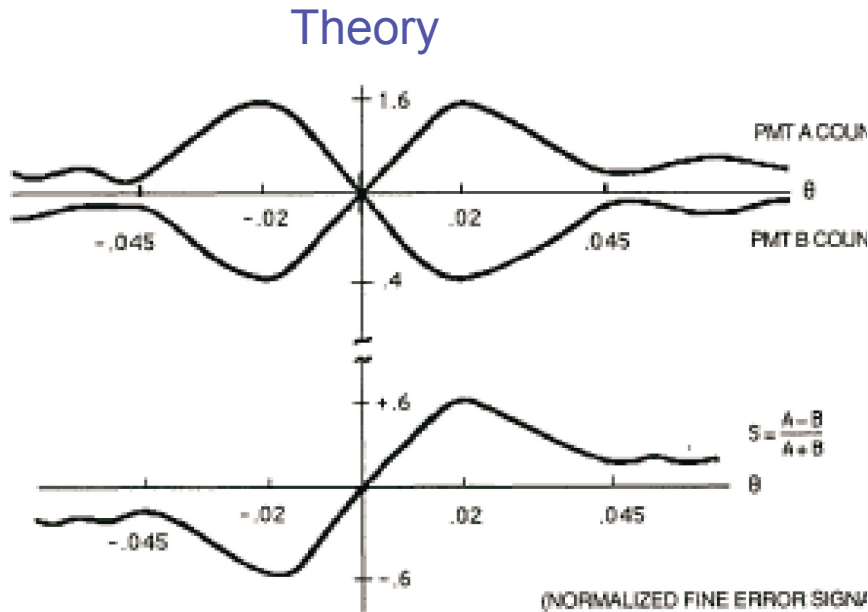
# FGS Detector Response



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$$S = (A-B)/(A+B)$$

# The Astrometry Model

A 3d volume of space is modeled using GaussFit (Jefferys, McArthur, & Fitzpatrick 1988, *Cel Mech*, **41**, 39)

Model requires as input (with variances)

**Lateral Color Calibration** - FGS contains refractive optics. Position of a blue star is displaced relative to the position it would have, if it were red.

**B-V Color Indices** - required for lateral color correction.

**Cross Filter Calibration**- targets with  $V < 9$  require a neutral density 5 (ND5) filter. Filter wedge displaces the position of the FGS interferometer fringe. Bright star position must be corrected. Depends on star color.

**Reference Frame Spectrophotometric Parallaxes** - from spectral types and photometry data. Required to obtain absolute parallax for the science target.

Solution process is allowed to adjust these input parameters (by amounts depending on their variances) to find the 'best' solution. In other words calibrations and any other prior knowledge about the reference frame go into the model as observations with error.



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# $\ell$ Car Reference Frame Spectrophotometric Parallaxes

- Photometry
  - FGS (V)
  - SAAO (UBVRI)
  - 2MASS (JHK)
  - McDonald/UVa (Washington - DDO)
- Color-color diagrams
  - Mapping to Spectral type from Bessell 1988 (PASP, 100, 1134)
  - J-H vs H-K and J-H vs V-K, for example
  - M - DDO51 vs M - T<sub>2</sub>



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# $\ell$ Car Reference Frame Spectrophotometric Parallaxes

- Spectral Typing and Luminosity Classification
  - SAAO - estimates  $\pm 2$  subtypes
- $M_V$  and  $(B-V)_0$ ,  $(V-I)_0$ ,  $(V-R)_0$ ,  $(V-K)_0$  from AQ2000
- $A_V$  from our photometry
- Additional luminosity class confirmation from reduced proper motion diagram
- Spect. Parallaxes ( $m-M = 5 \log d - 5$ ,  $\pi = 1/d$ )  
$$\pi_{sp} = 1/(10^{(V - M_V + 5 - A_V)/5})$$



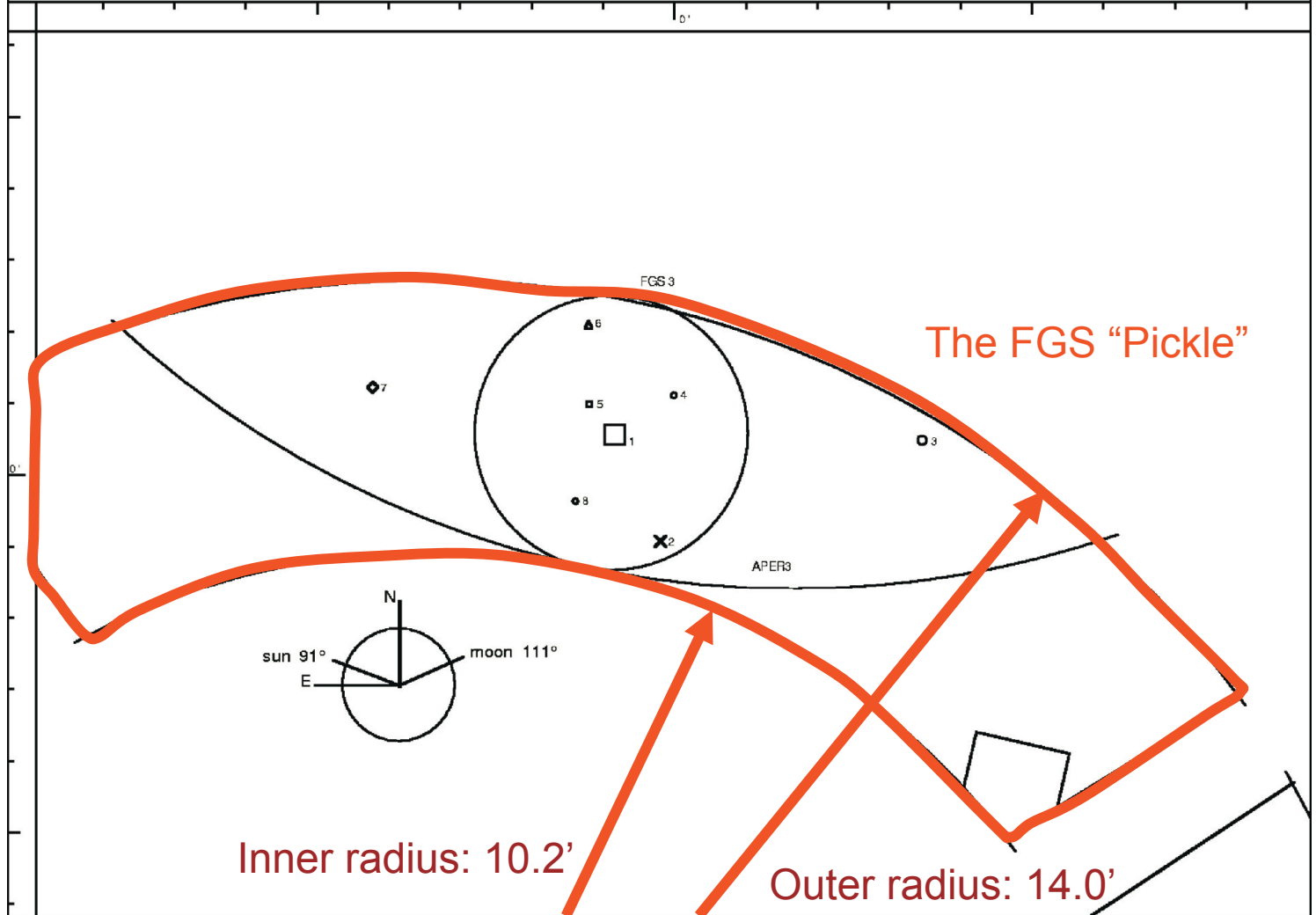
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# Field of View of FGS

File : OzTeX: to-from cfgauss, abridged: Astrophys π:RR Lyr π:RR Lyr & rFile : Ωδ` Ô^¿ Pickles 4.05, by James McCartney, docs:  
 V1: Ra: 19h 25m 42.935s Dec: 42° 35' 25.537" Roll: 9.00° Orient: -102.32° Veh.Roll: 282.32°  
 AntiSun: 88° Moon: 111° Plate Roll: 0° Tobs: 96/04/29.500 Tcat: 00/01/01.500 Now: 0/10/2 21:50:44



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# FOV After Multiple Visits



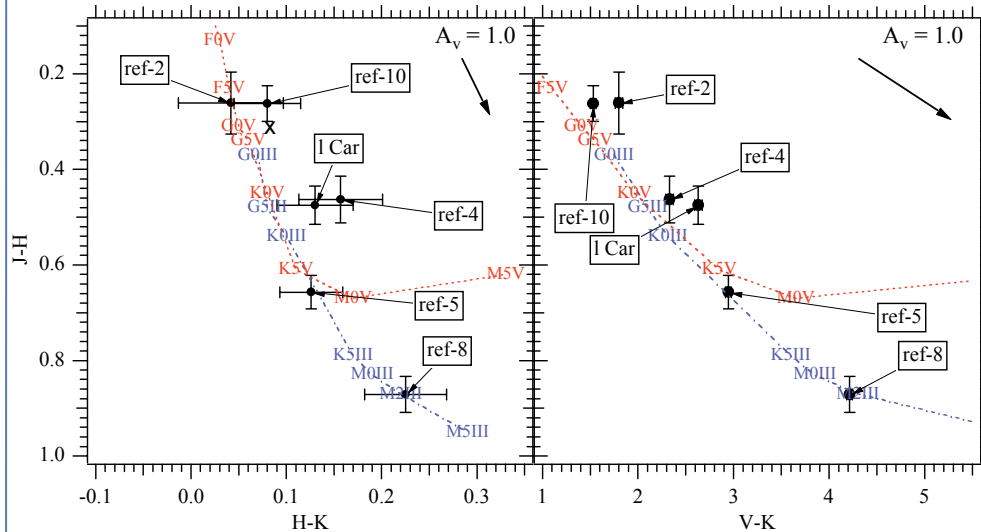
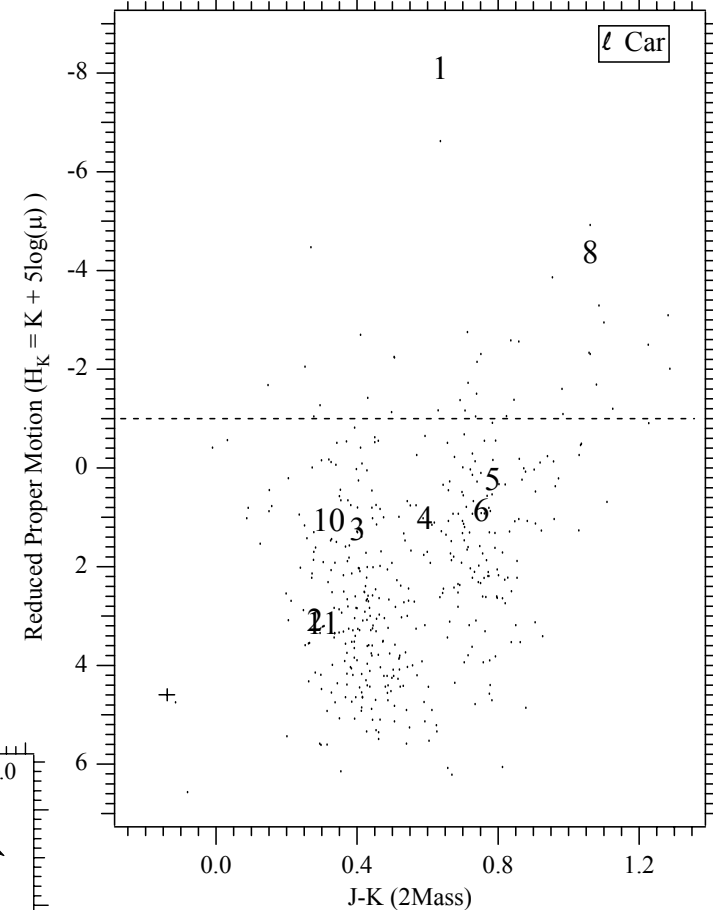
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# Reference Frame Objects

PropID	FGS ID	V	SpT	pi(sp)	err
38	2	<b>14.29</b>	G0V	0.00118	0.00027
39	3	13.57	G0V	0.00161	0.00037
40	4	<b>13.53</b>	G5III	0.00037	0.00012
41	5	<b>13.18</b>	K0III	0.00042	0.00010
44	8	<b>10.62</b>	M0III	0.00079	0.00018
45	9	13.44	F3V	0.00103	0.00024
46	10	<b>12.97</b>	F4V	0.00134	0.00031
47	11	<b>15.58</b>	F3V	0.00040	0.00009



- Photometry from Menzies and 2MASS
- Proper motions from UCAC2
- Spectral classifications from Feast



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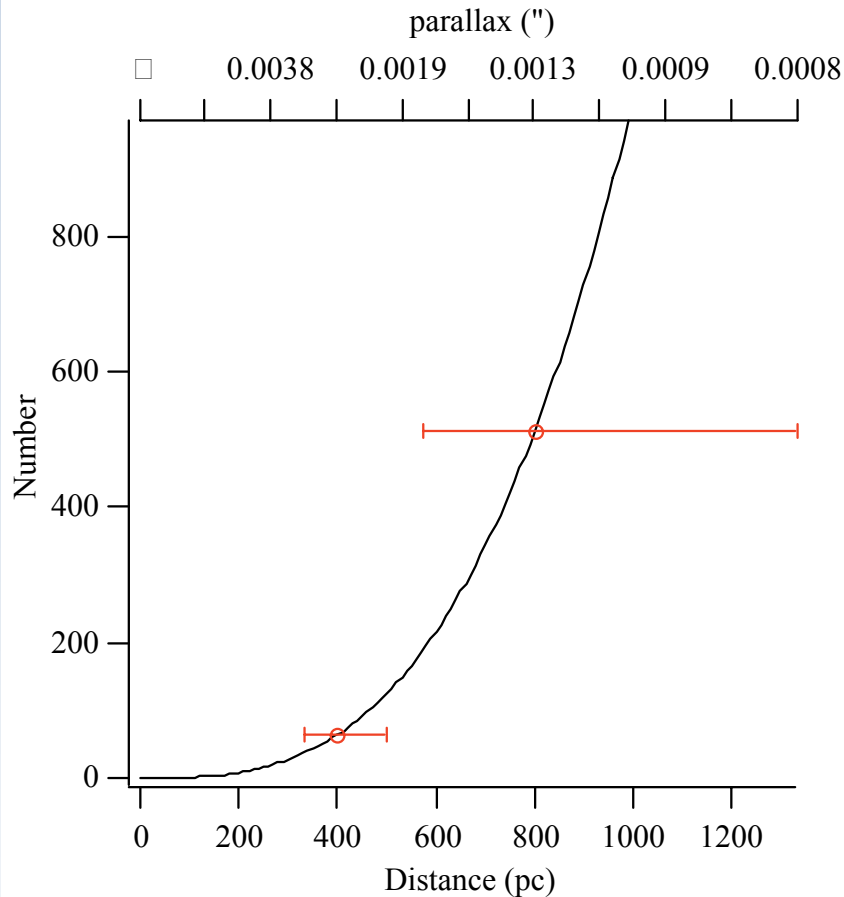
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# Another Complication

## Transforming Parallax to Absolute Magnitude (in the presence of noise)

# Lutz-Kelker Bias

- Assuming uniform distribution for this class of object
- $\pm 0.5$  milliarcsec error
- Frequentist's viewpoint - for a given error you are more likely to have underestimated the distance (measured an object that is really more distant)
- LK bias proportional to  $(\sigma_{\pi}/\pi)^2$
- It is a correction to any absolute magnitude, e.g.,  $M_V$



Lutz & Kelker 1973 PASP 85 573



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# The Absolute Magnitude of a Cepheid

- Lutz-Kelker Bias
  - scales as  $(\sigma_{\pi}/\pi)^2$
  - and depends on an assumed distribution of evolved stars, which is taken to be  $n(r) \sim \text{const.}$
- For  $\ell$  Car
  - $\pi_{\text{ABS}} = 2.01 \pm 0.20$  mas,
  - $\sigma_{\pi}/\pi = 0.10$ ,
  - and the LK bias correction,  
 $\text{LKB} = -0.08$  mag.

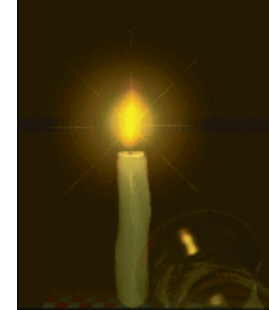


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# Calibrating a Candle



## $\ell$ Car Parallax

$$x' = x + lcx(B-V) - \Delta XF_x$$

$$y' = y + lcy(B-V) - \Delta XF_y$$

$$\xi = Ax' + By' + C - \mu_x \Delta t - P_\alpha \pi_x$$

$$\eta = -Bx' + Ay' + F - \mu_y \Delta t - P_\delta \pi_y$$

yields  $\pi_{abs} = 2.01 \pm 0.20$  mas

HIPPARCOS  $\pi_{abs} = 2.06 \pm 0.27$  mas  
(from the redo; van Leeuwen et al 2007)

$$A_V = 0.52 \pm 0.06$$

$$A_K = 0.06 \pm 0.01$$

$$m-M = -5 \log \pi_{abs} - 5 + A - LKB$$

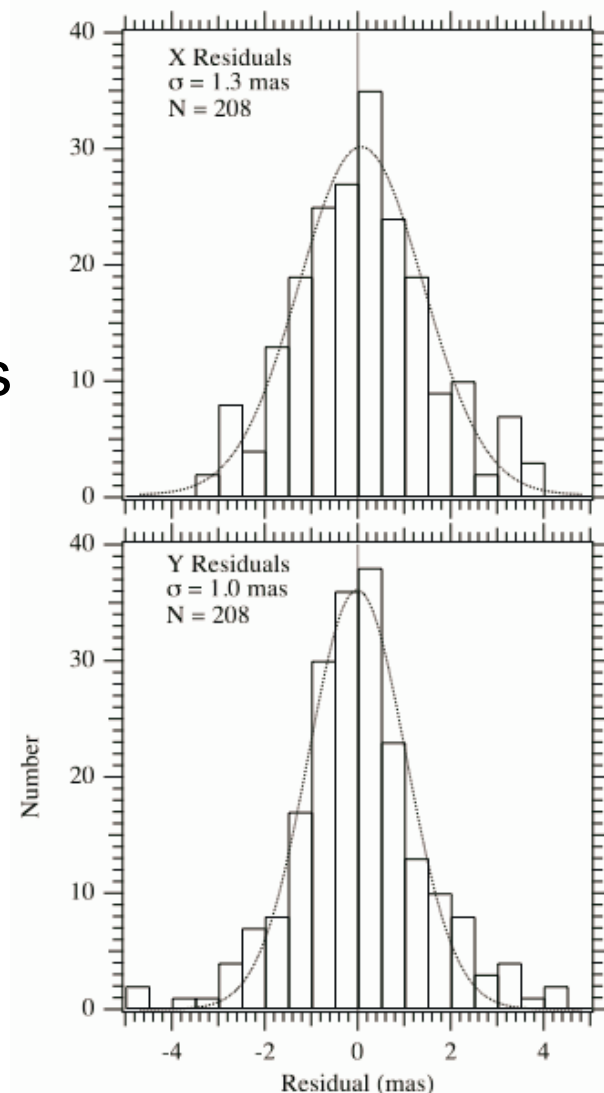
Solve for absolute magnitude,

$$M_V = -5.35 \pm 0.22$$

$$M_K = -7.55 \pm 0.21$$

03.06.2008

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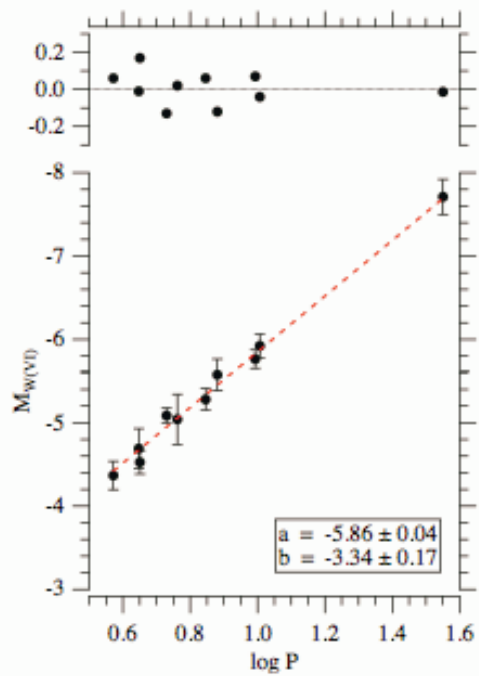
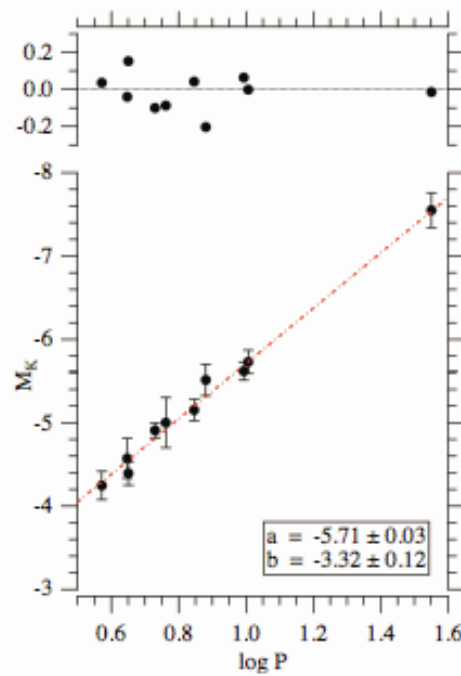
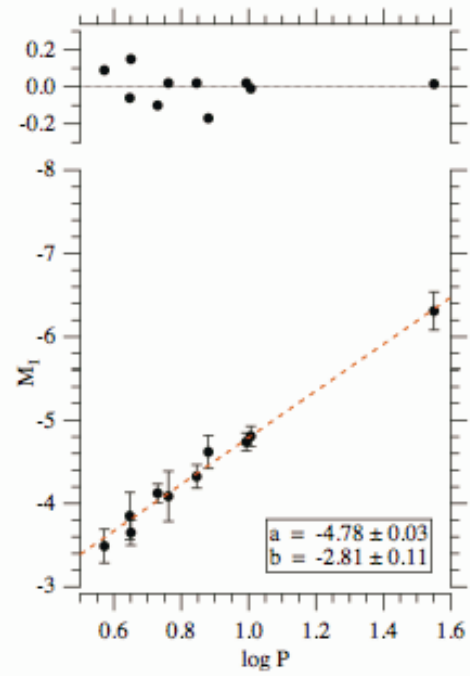
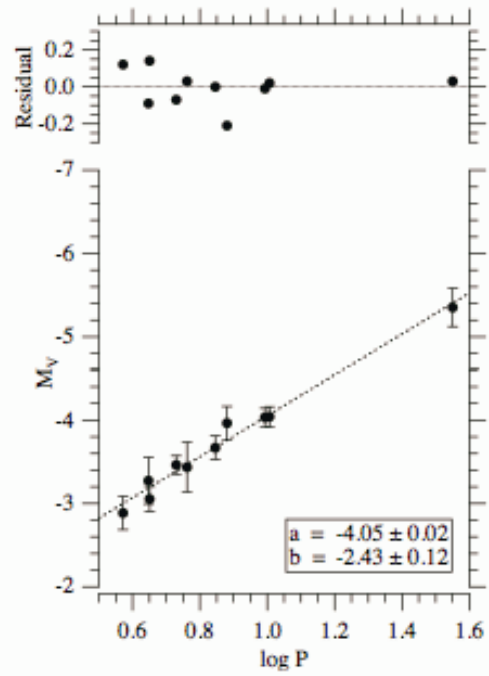


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Do for all Cepheids  
and a selection of  
bandpasses

Galactic Cepheid PLR  
with N=10 objects

$$M = a + b (\log P - 1)$$



Benedict et al 2007 AJ 133 1810



# Tests

- So, who's right about  $H_0$ ? Sandage (~62km/s/Mpc) or Freedman (~72km/s/Mpc)?
- NGC 4258



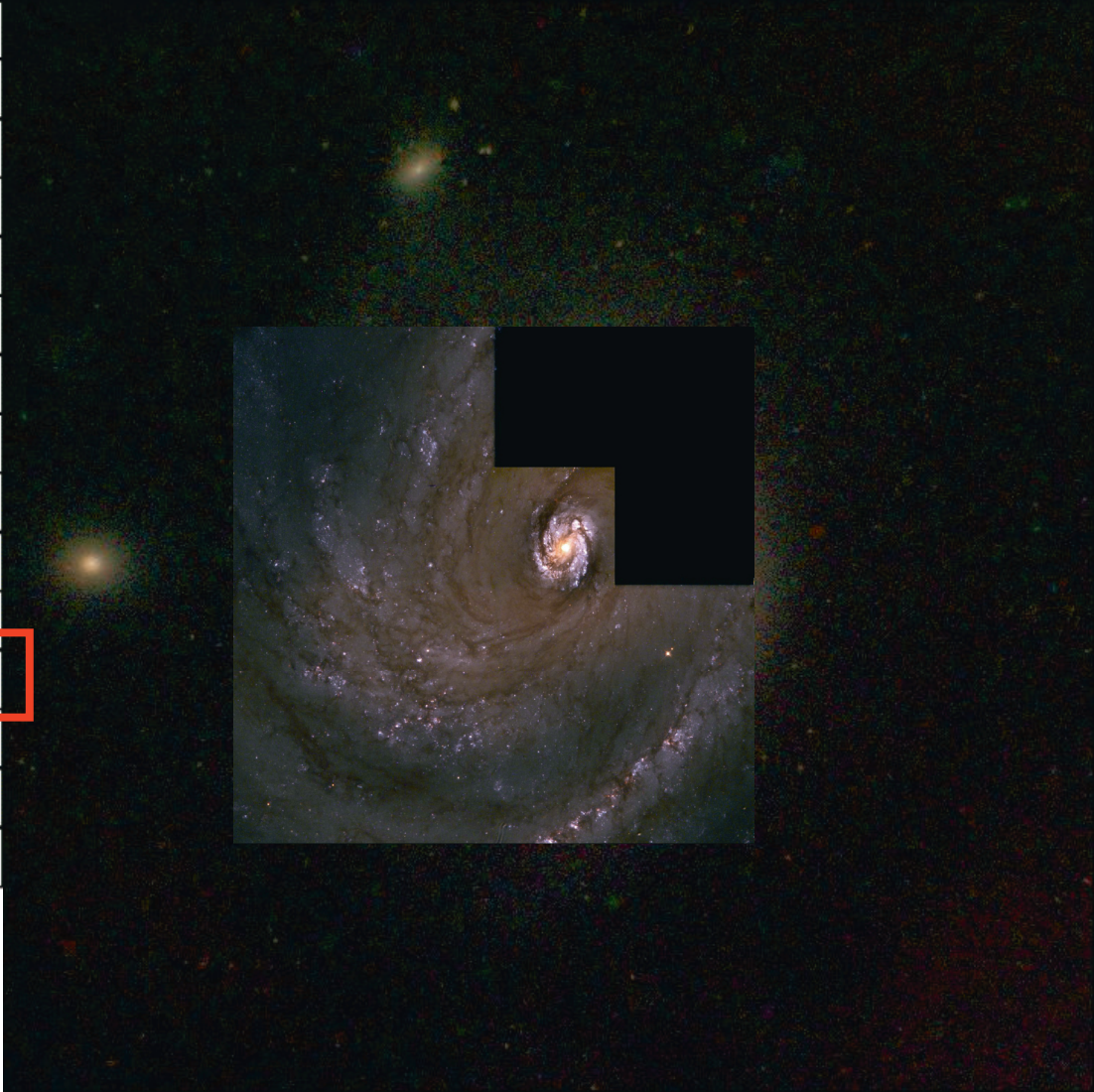
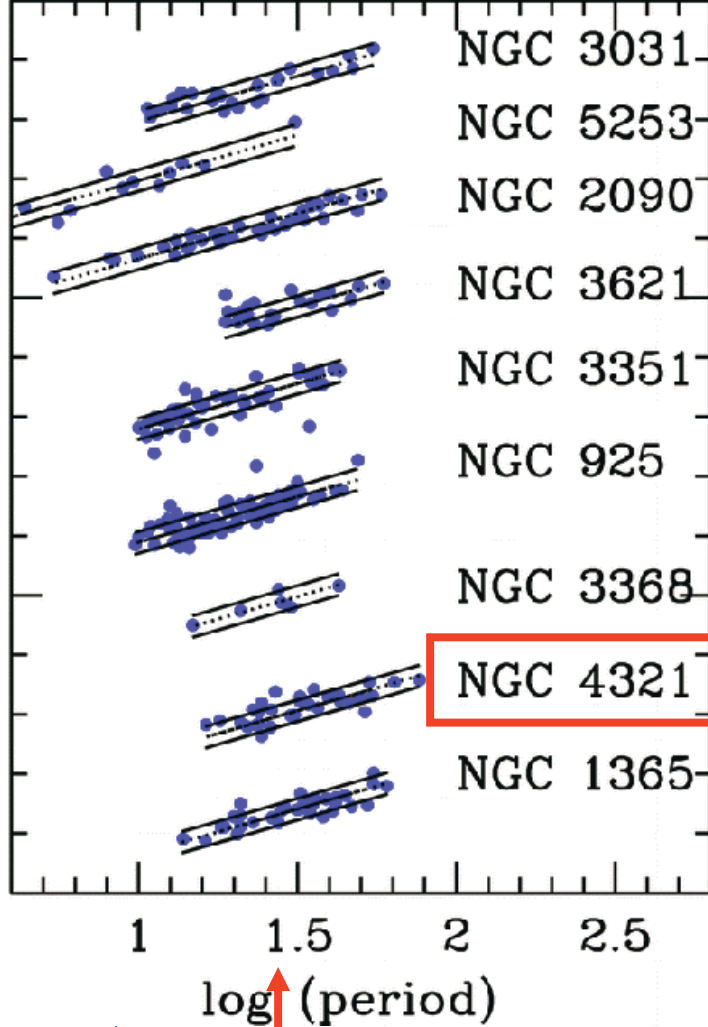
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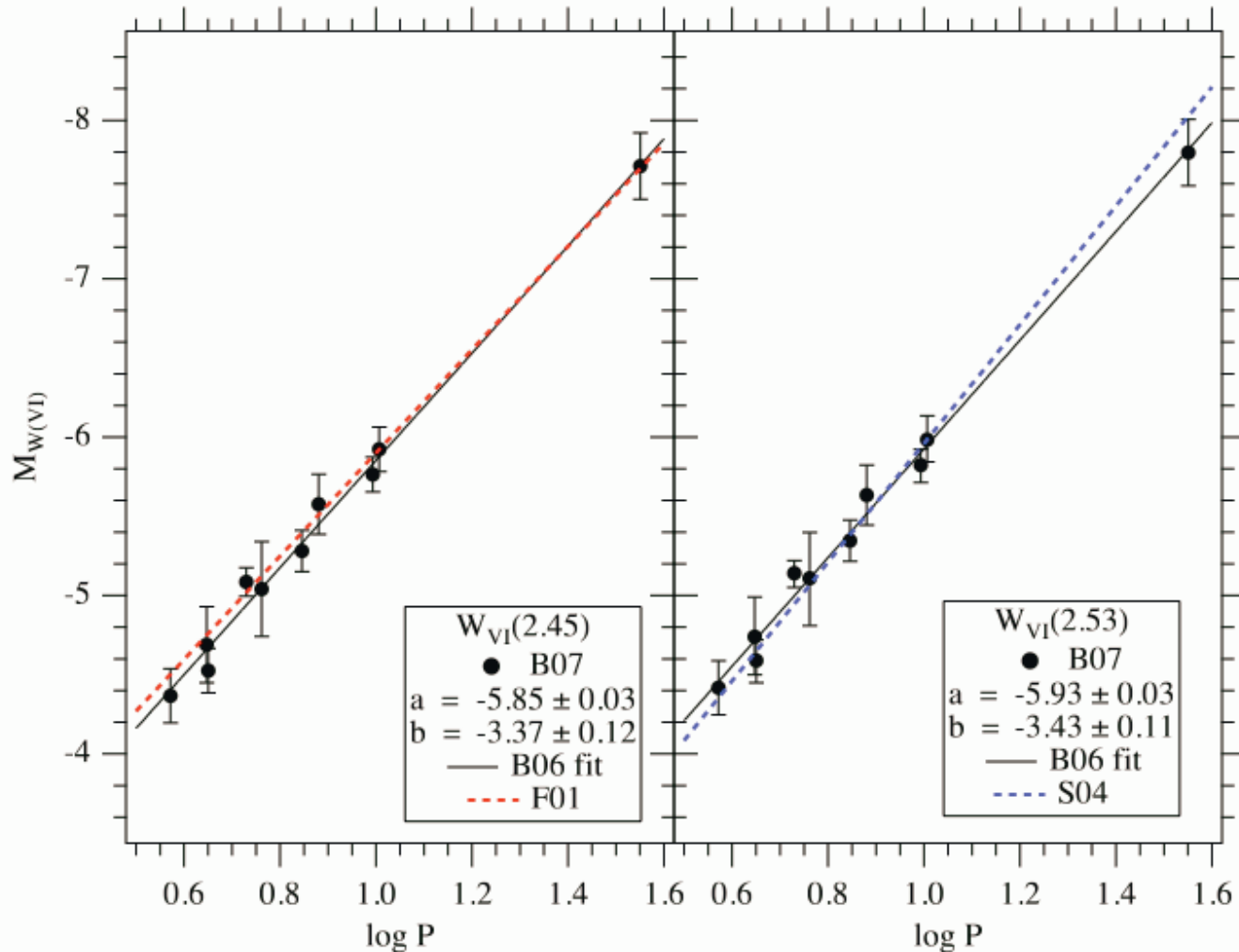


I magnitude (arbitrary scale)



Note the  $\log(P)$  of most of the Cepheids

# Freedman or Sandage?



Adopting our PLR would tend to increase the Sandage  $H_0$  value, but **leave the Freedman  $H_0$  unchanged.**



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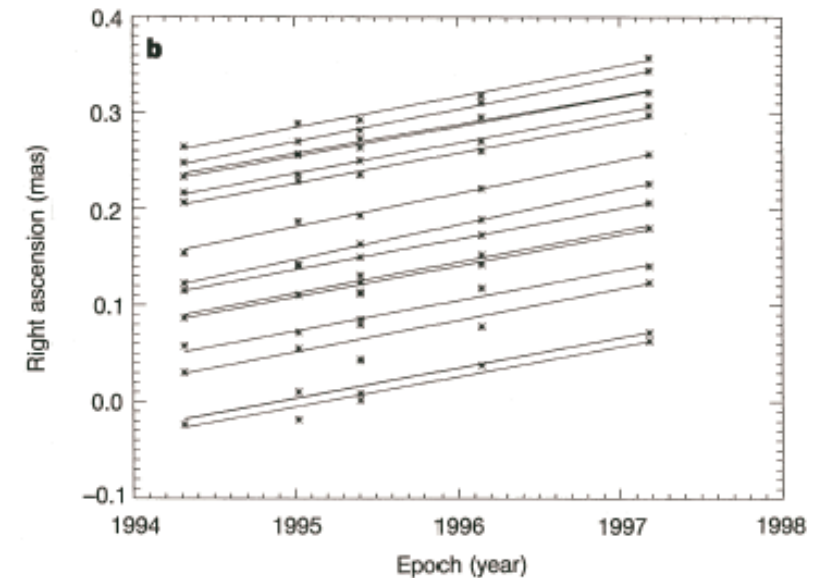
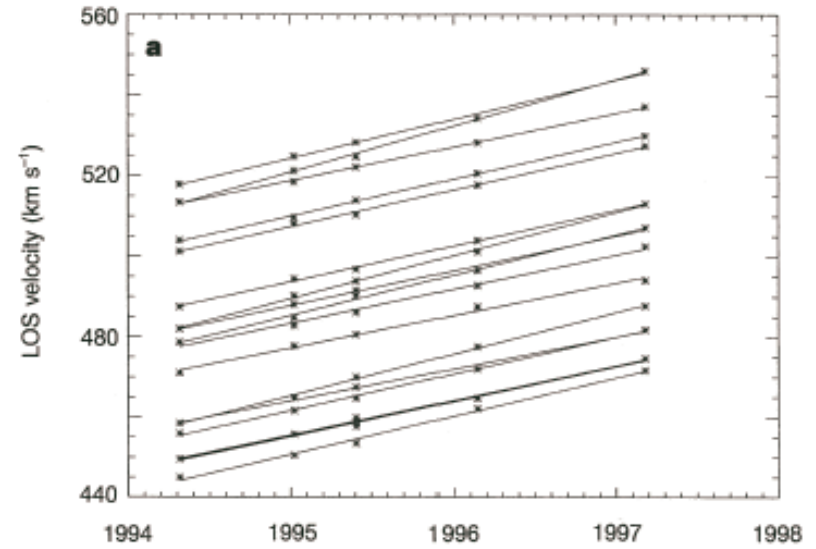
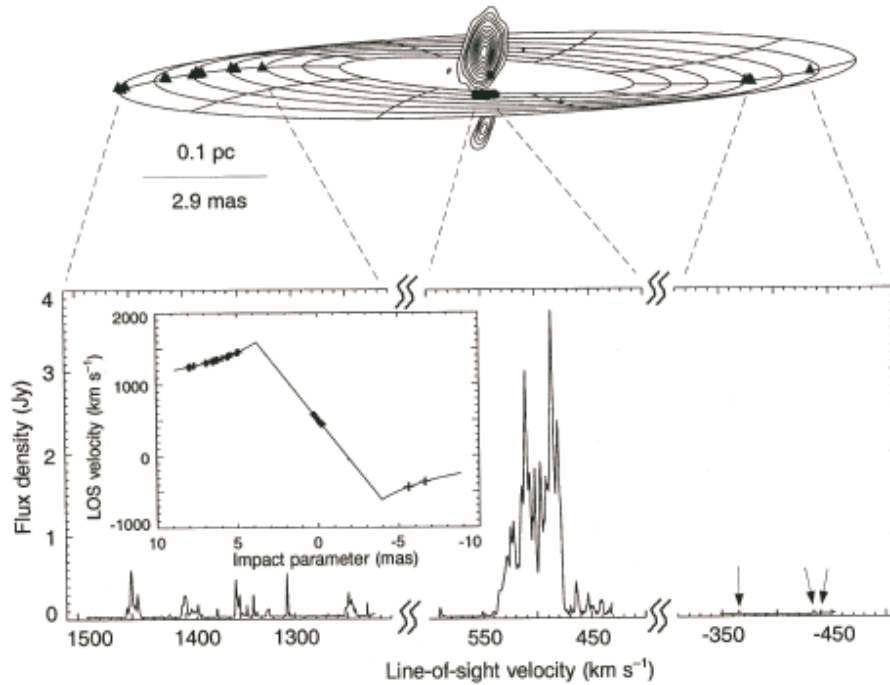
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# NGC 4258

- Contains Cepheids
- Contains a black hole orbited by masers that emit radio waves
- Radio astronomers have measured the velocities and motions of those objects with VLBI
- Comparing the velocity with the amount of motion on the sky yields a distance
- That distance agrees ‘exactly’ with our distance obtained by comparing our Cepheids to those in the galaxy



# NGC 4258 Masers



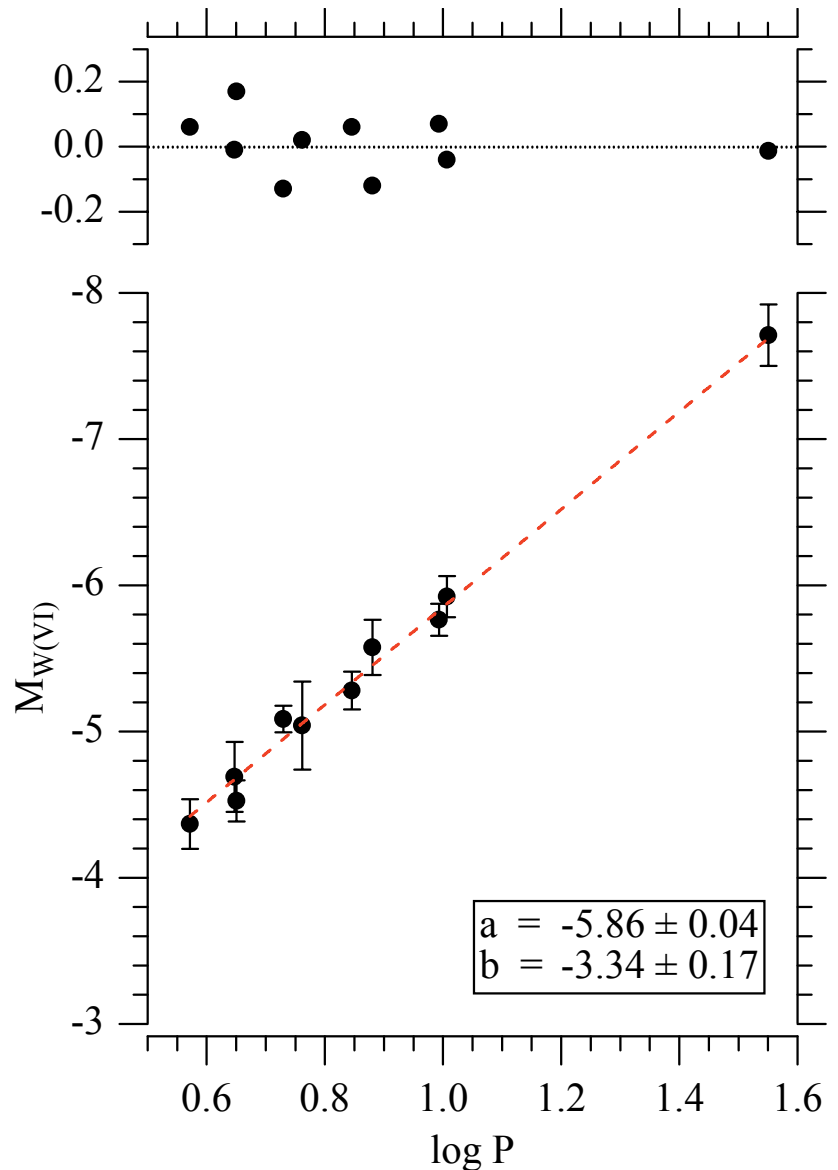
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Second Astronomy

# $W_{VI}$ band

- NGC 4258
  - Macri has applied our  $W(VI)$  PLR to 85 of his inner-field Cepheids and finds  $m-M = 29.21 \pm 0.02$
  - Herrnstein et al. (1999) get  $m-M = 29.29 \pm 0.15$  from masers
  - Using our LMC  $m-M^*$  and the Macri et al. (2006) differential (LMC-NGC 4258) modulus yields  $m-M = 29.28 \pm 0.08$



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# How far away is the LMC ?



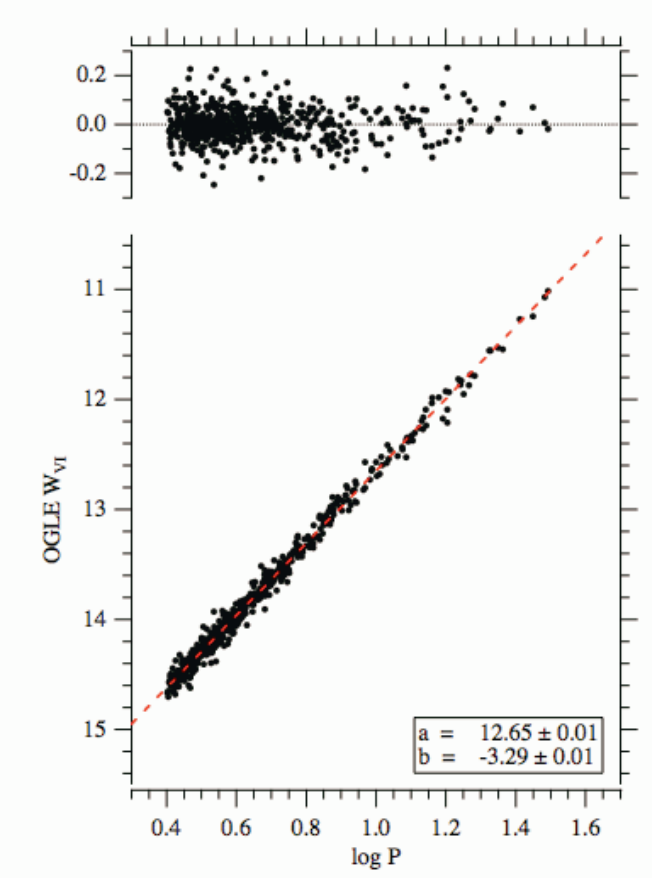
# LMC Cepheid PLR from preened (from Kanbur et al 2003) OGLE photometry



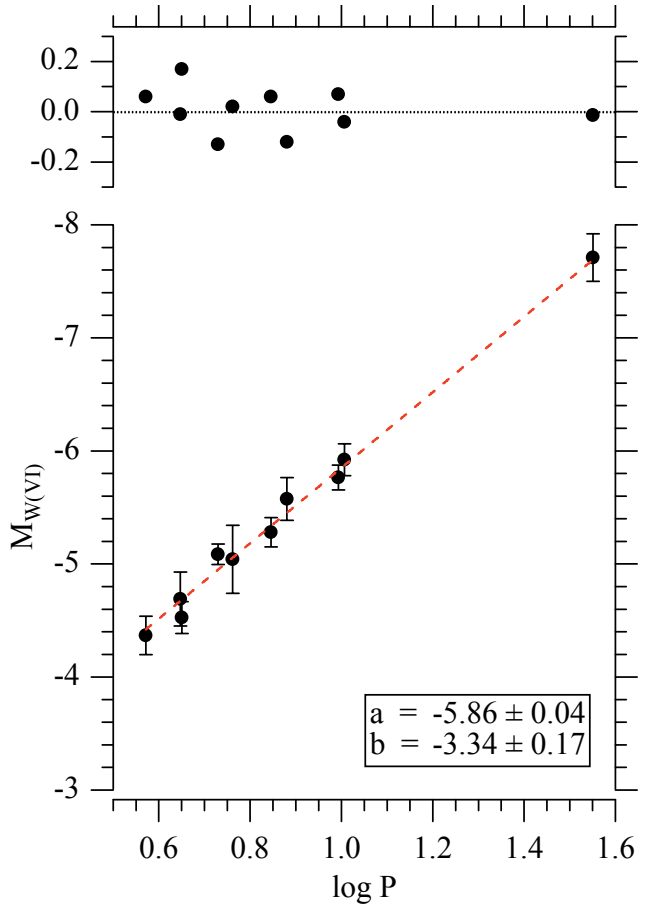
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- We derive an uncorrected  $m-M = 18.50 \pm 0.03$  for the LMC.

- Metallicity corrections

- Macri et al. (2006), comparing near-nucleus Cepheids with those at the edge of NGC 4258, get a correction in  $W_{VI}$ ,  $\gamma = -0.29 \pm 0.11$  for 1 dex in metallicity

- Kennicutt et al. (1998) get for M101  $\gamma = -0.24 \pm 0.16$  for 1 dex in metallicity

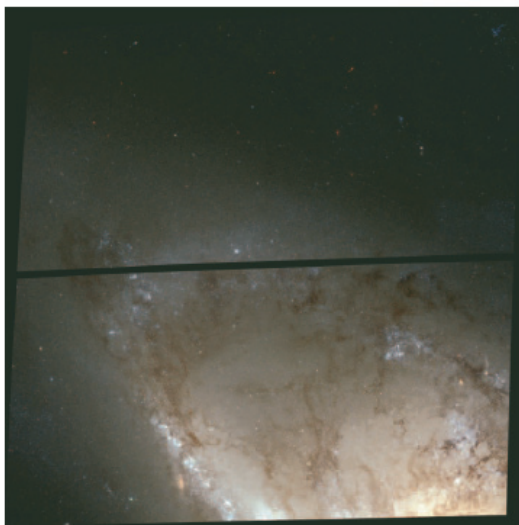


FIG. 3.—Color composite of the *HST* ACS/WFC inner field of NGC 4258.

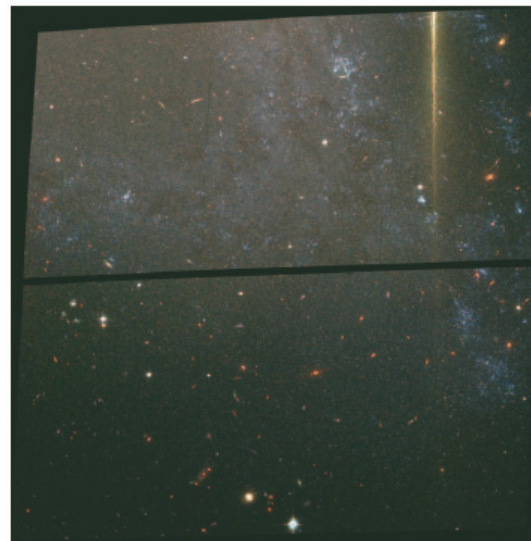


FIG. 2.—Color composite of the *HST* ACS/WFC outer field of NGC 4258.





- Groenewegen et al. (2004) find LMC metallicity of  $-0.36$  dex
- Weighted average of Macri & Kennicutt  $\gamma$  corrections yields LMC distance modulus correction of  $-0.10 \pm 0.03$
- Therefore, LMC  $(m-M)_0 = 18.40 \pm 0.05$
- Compare with eclipsing binary results (Fitzpatrick et al 2003),  $(m-M)_0 = 18.42$



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# Distance scale summary

Demonstrated that Galactic Cepheids are again a useful distance scale tool

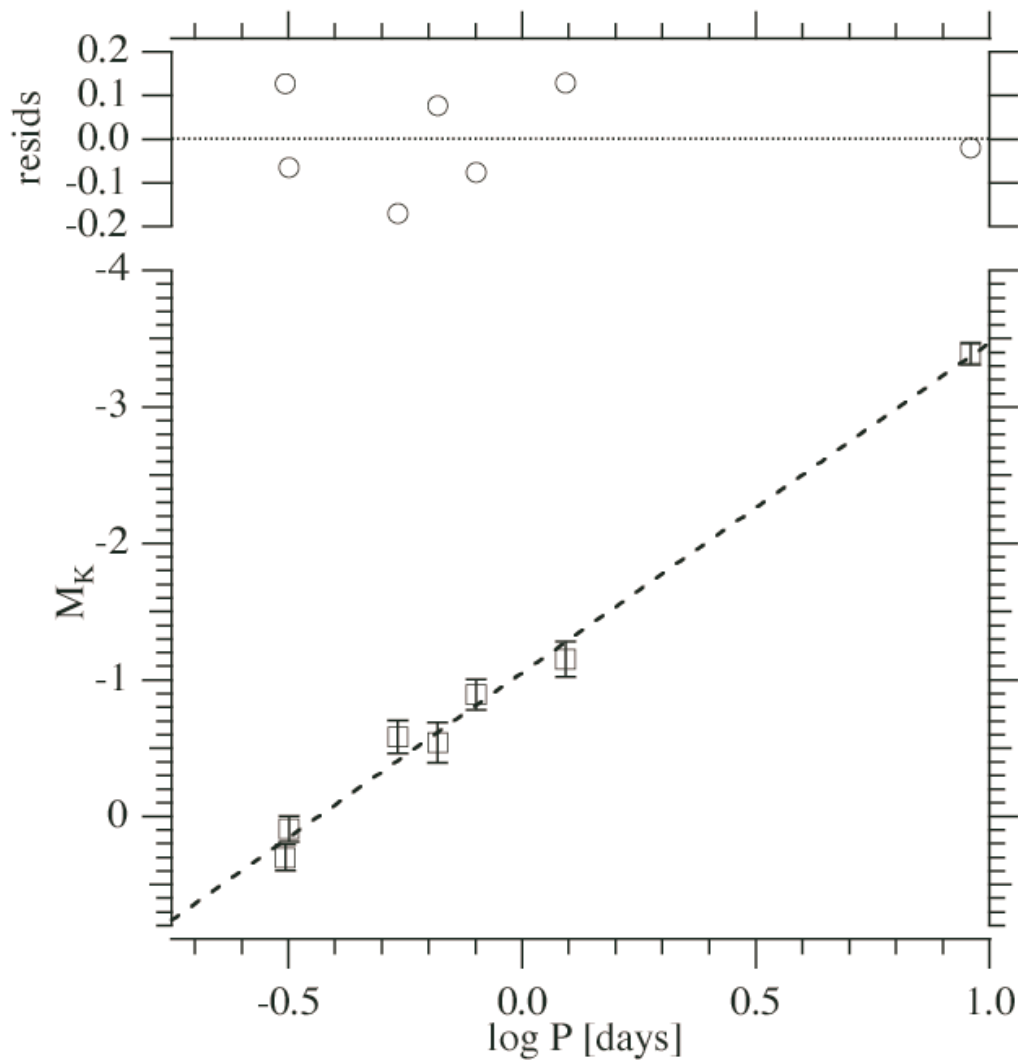
LMC distance modulus  $m-M = 18.40 \pm 0.05$  (details on request)

For NGC 4258 the maser and Cepheid distances agree

Have aided calibration of other techniques to increase numbers of long-period Cepheids in the PLR

Have done such a good job that the Cycle 16 HST TAC awarded Benedict et al. >100 orbits to measure RR Lyr and Pop II Cepheid parallaxes to establish a Pop II PLR calibration.





**If Benedict et al. do as well on these RR Lyr and Pop II Cepheids as they did on the Pop I Cepheids, they should have something like this in two years**

Figure 1: A simulated Pop II Period-Luminosity relation built with absolute magnitude estimates from an  $M_V$ -[Fe/H] relation from Chaboyer *et al.* (1998) and an  $M_K$  - logP relation (Matsunaga *et al.* 2006) for RRL and Pop II Cepheids. The scatter is simulated, but representative of what we expect, based on our previous parallax work with Pop I Galactic Cepheids (Benedict *et al.* 2007). Data of this expected quality would yield a zero-point error of 0.04 magnitudes.



Pop II PLR will help determine distances to globular clusters

But wait!  
There's another way to do this

Two independent approaches would greatly improve the accuracy, right?

# Controversy!!

The Parallax of the Pleiades - an issue that won't go away



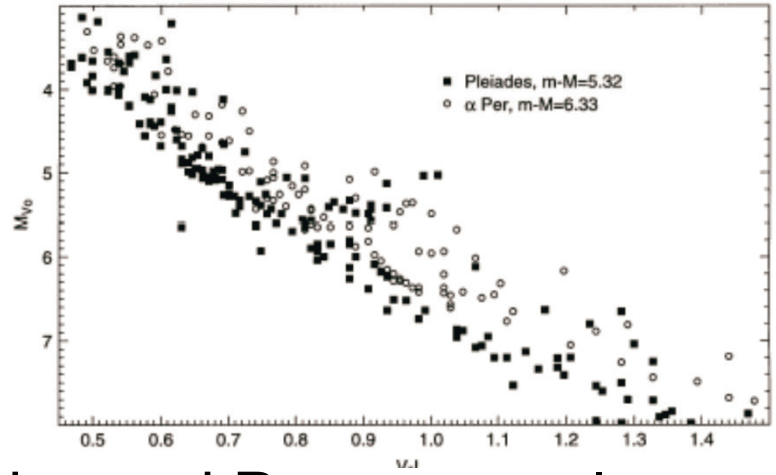
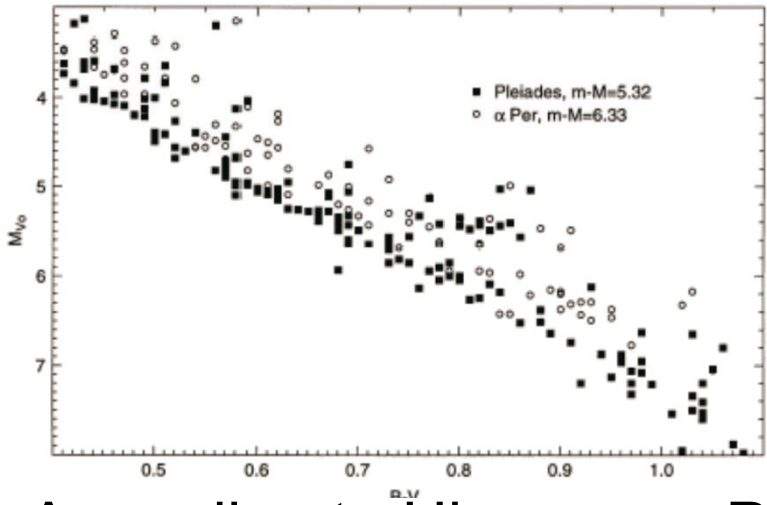
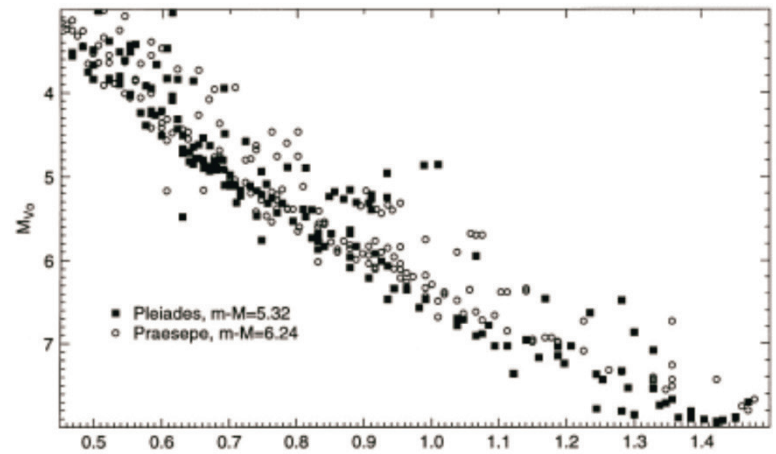
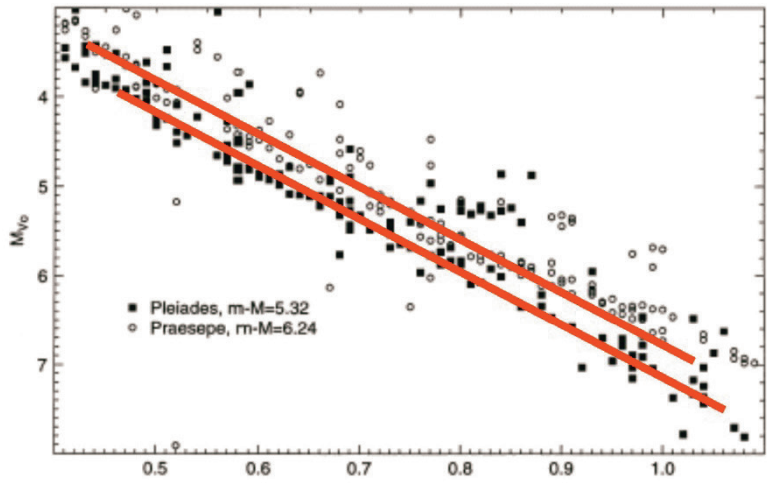
# This Distance Between Us



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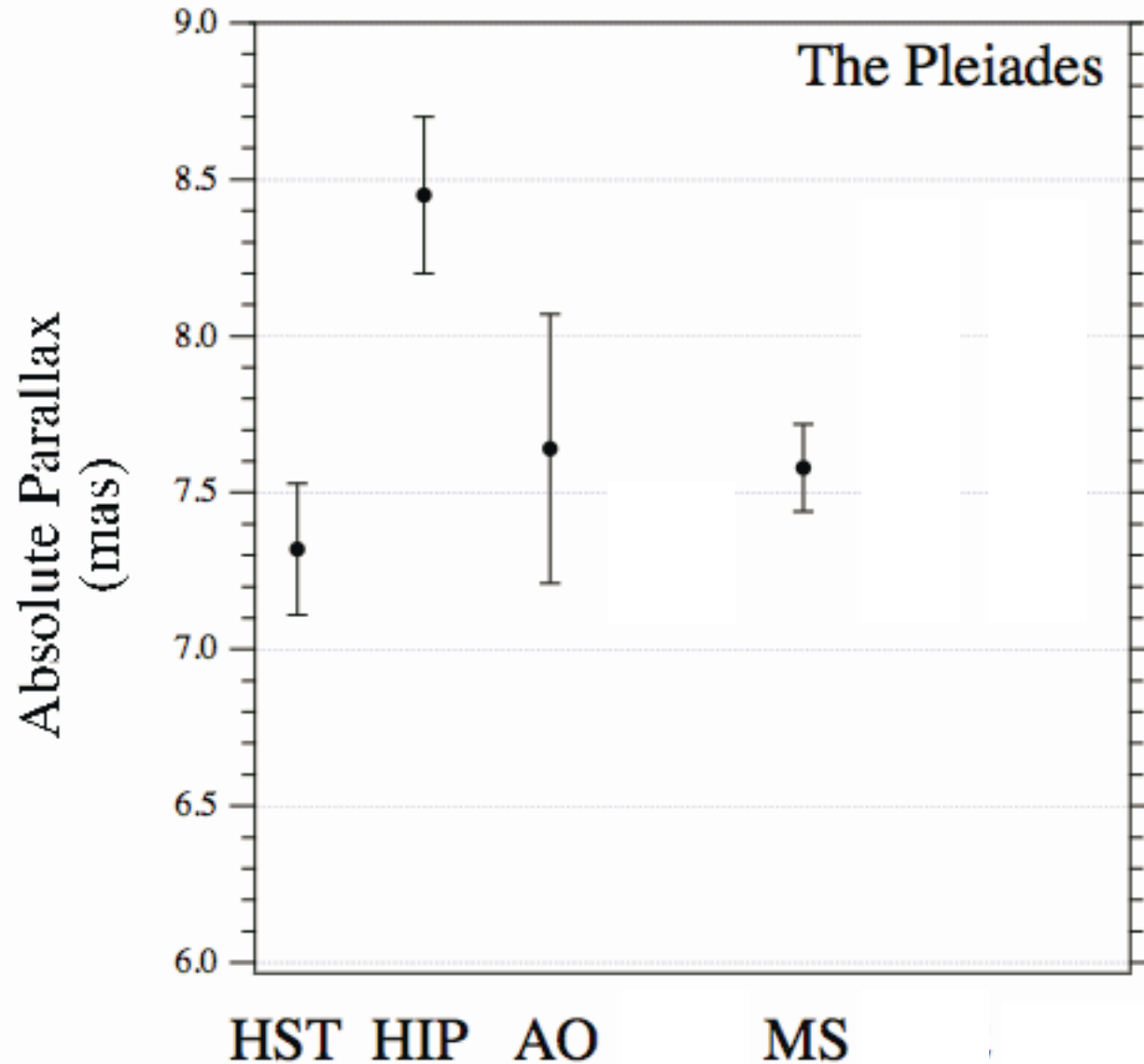


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According to Hipparcos, Pleiades and Praesepe color-luminosity relationships are offset (Pinsonneault et al 1998)

# Pleiades Distance



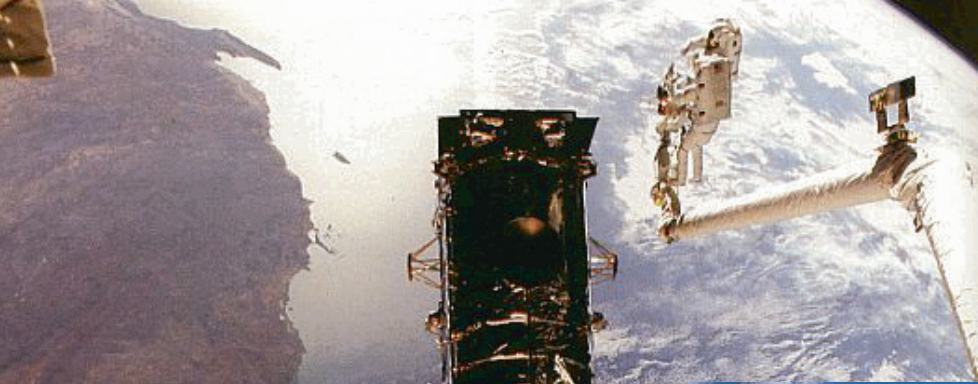
HST = Soderblom, Nelan,  
Benedict, McArthur et  
al 2005

HIP = Perryman et al  
1997

AO = ?

MS = Pinsonneault et al  
1998

# SM4: October 2008



03.06.2008



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# Take-Home Lessons

- Careful consideration of sometimes unfamiliar error terms (eg. Lutz-Kelker bias) is necessary
- Careful consideration of reference frame is necessary
- Long-term stability (and **repeatability**) is necessary
- Comparison (and contradiction) with other methods needs to be carefully considered
- Interferometry provides measures at angular scales not available in traditional imagers
- These techniques should be applicable for astrometry with PRIMA



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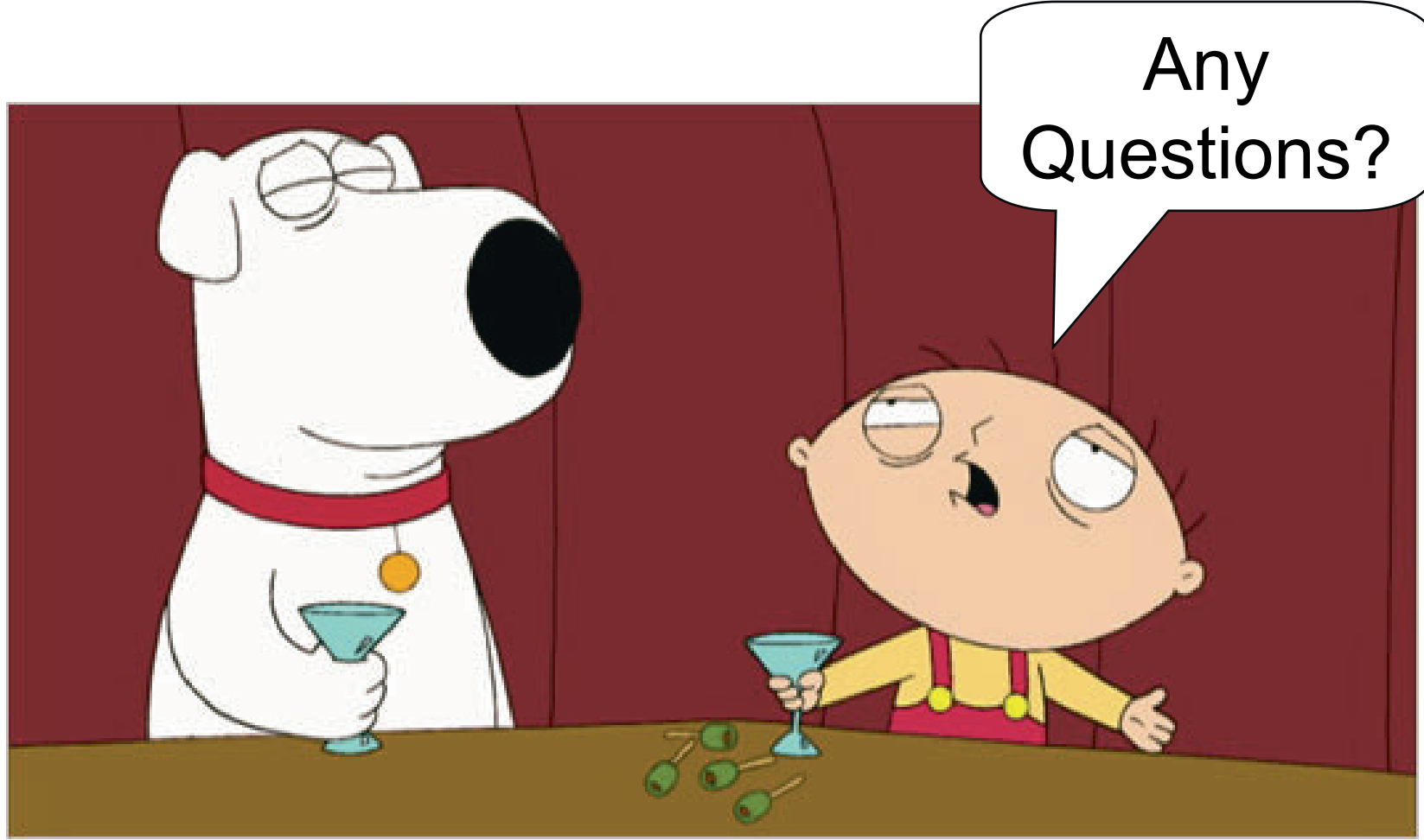
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Don't Miss: HST FGS poster (Eder Martioli / Fritz Benedict)