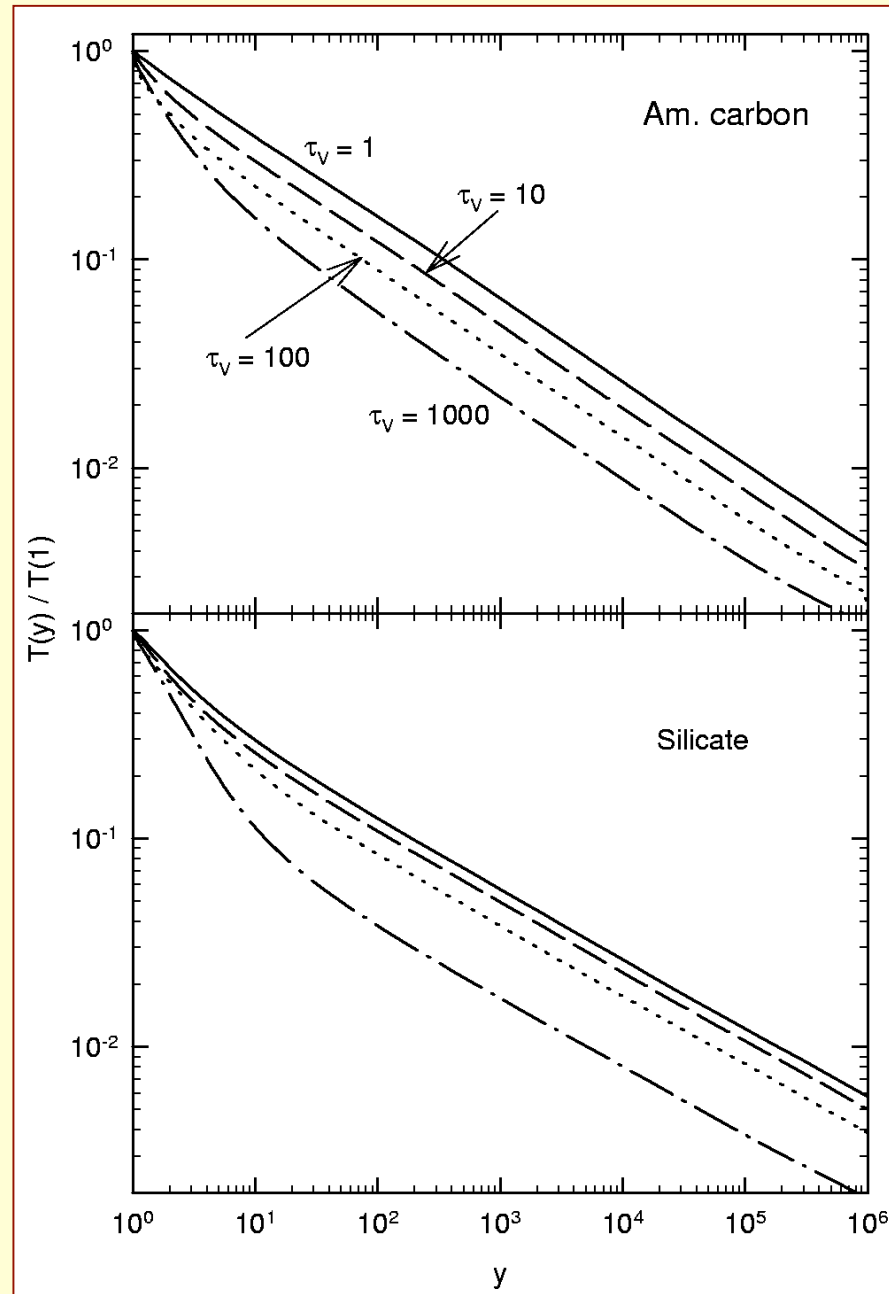


The Obscuring Torus (2)

Moshe Elitzur
University of Kentucky



Dust Temperature Profile



Ivezic & Elitzur 97

Clumpy Media Modeling

- Nenkova, Ivezić & Elitzur 2002, ApJL 570, L9
- Elitzur, Nenkova & Ivezić 2003, astro-ph/0309040
- Elitzur 2006, astro-ph/0612458

Clumpy Medium

$$\text{filling factor: } \phi = n_c V_c \ll 1$$

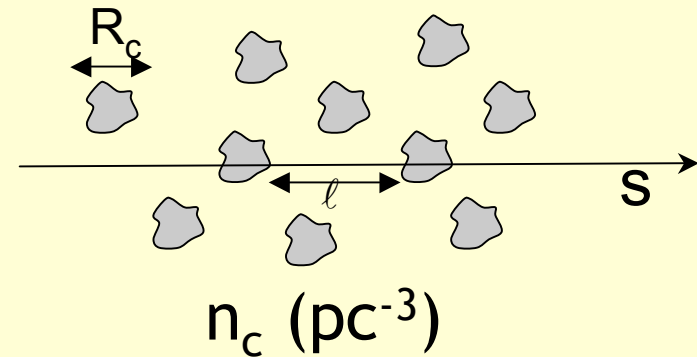
$$\phi = n_c A_c R_c = R_c / \ell \ll 1$$

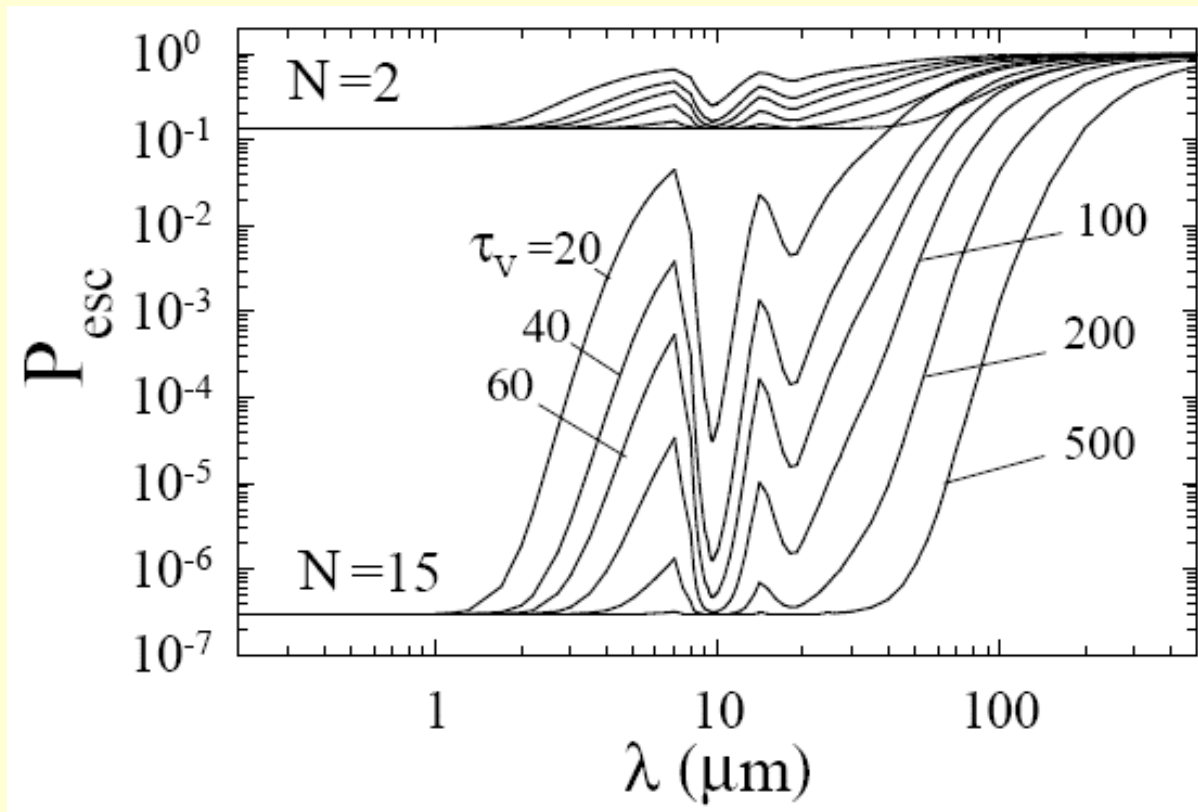
$$n_c, R_c \Rightarrow \phi, N = n_c A_c = 1 / \ell \text{ (pc}^{-1}\text{)}$$

$$\text{segment } ds: d\mathcal{N}(s) = N(s)ds \quad \text{emission: } S_{c\lambda} d\mathcal{N}(s)$$

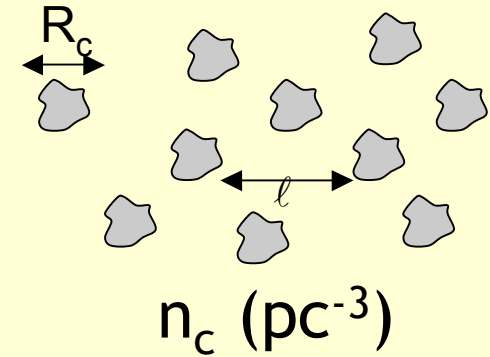
👉 Natta & Panagia 84: $P_{\text{esc}} = e^{-t}$; $t = \mathcal{N}(s)(1 - e^{-\tau})$

👉
$$I_{C\lambda} = \int e^{-t} S_{c\lambda} N(s) ds$$





Example: N_{tot} cubic clouds of size R_c
in a cubic volume of size L :



$$n_c = N_{\text{tot}}/L^3$$

$$\phi = n_c R_c^3 = N_{\text{tot}} (R_c/L)^3$$

$$N = n_c R_c^2 = \frac{N_{\text{tot}}}{L} \left(\frac{R_c}{L} \right)^2$$

$$\mathcal{N} = NL = N_{\text{tot}} \left(\frac{R_c}{L} \right)^2$$

$$N_{\text{tot}} = \mathcal{N}^3 / \phi^2$$

Monte Carlo Results

$$\tau_{\text{av}} = \mathcal{N}(1 - e^{-\tau}) ?$$

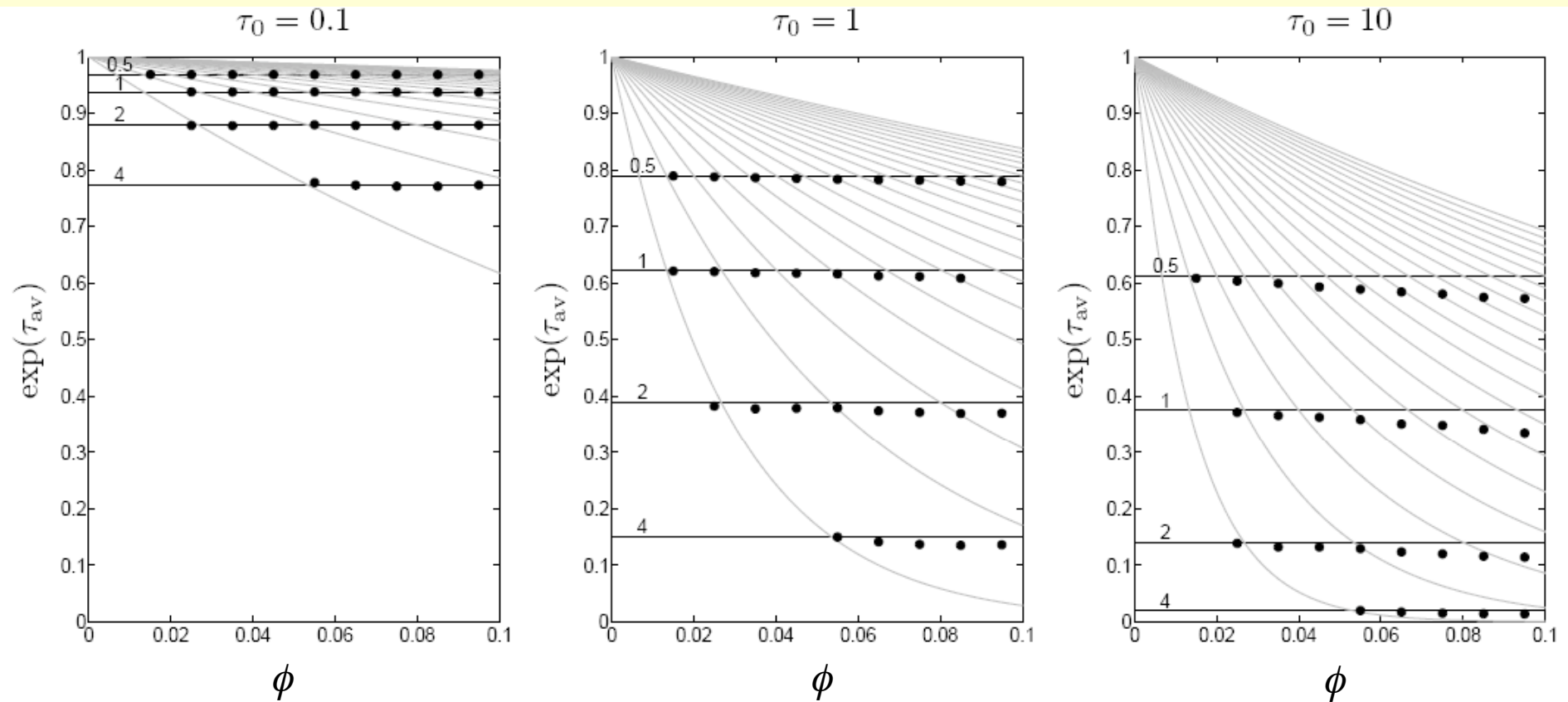
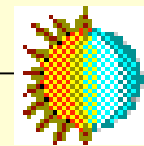
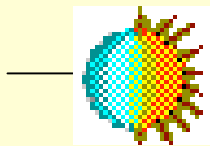


Fig. 1.— Averaged response function $\exp(\tau_{\text{av}})$ versus filling factor ϕ for $\tau_0=0.1, 1$ and 10 . Filled circles and horizontal black lines indicate the results from numerical simulations and theoretical predictions respectively, using $\mathcal{N}=0.5, 1, 2$ and 4 . The errorbars are comparable to the size of the circles. Gray curved lines trace the loci defined by $R/L = 0.01, 0.02 \dots, 0.2$ increasing from the left.

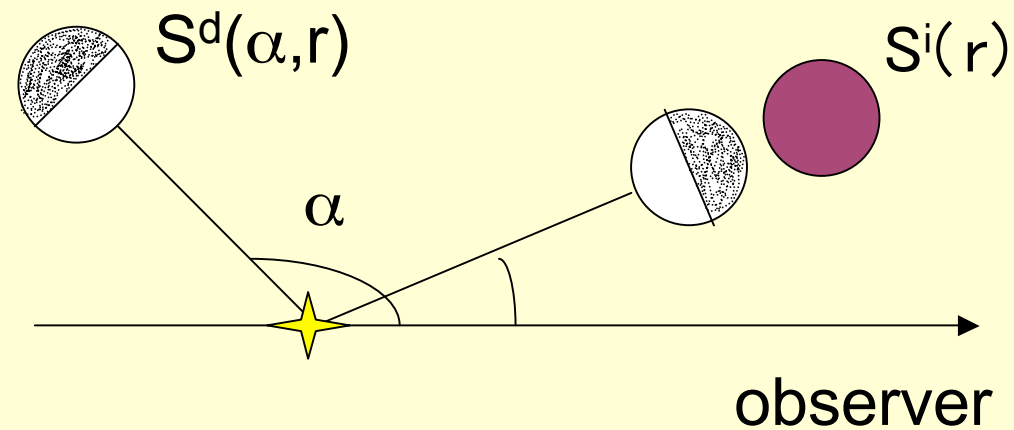
Conway, Elitzur & Parra 07



Cloud Emission - Anisotropy



Direct & Indirect Heating

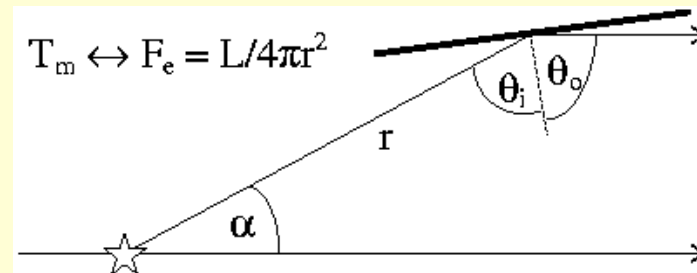
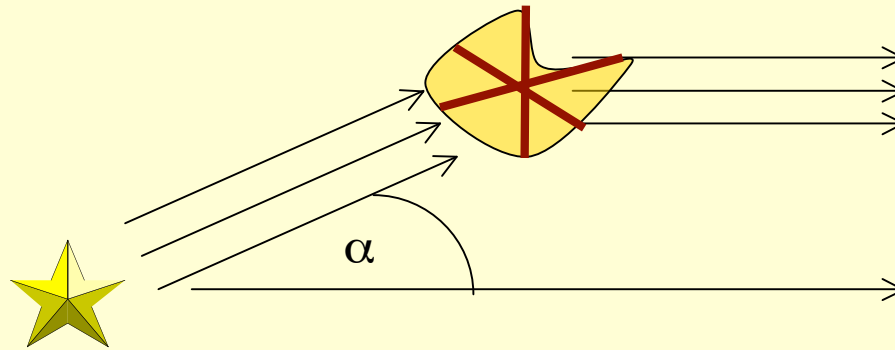


Composite source function:

$$S_c(\alpha, r) = p S^d(\alpha, r) + (1 - p) S^i(r)$$

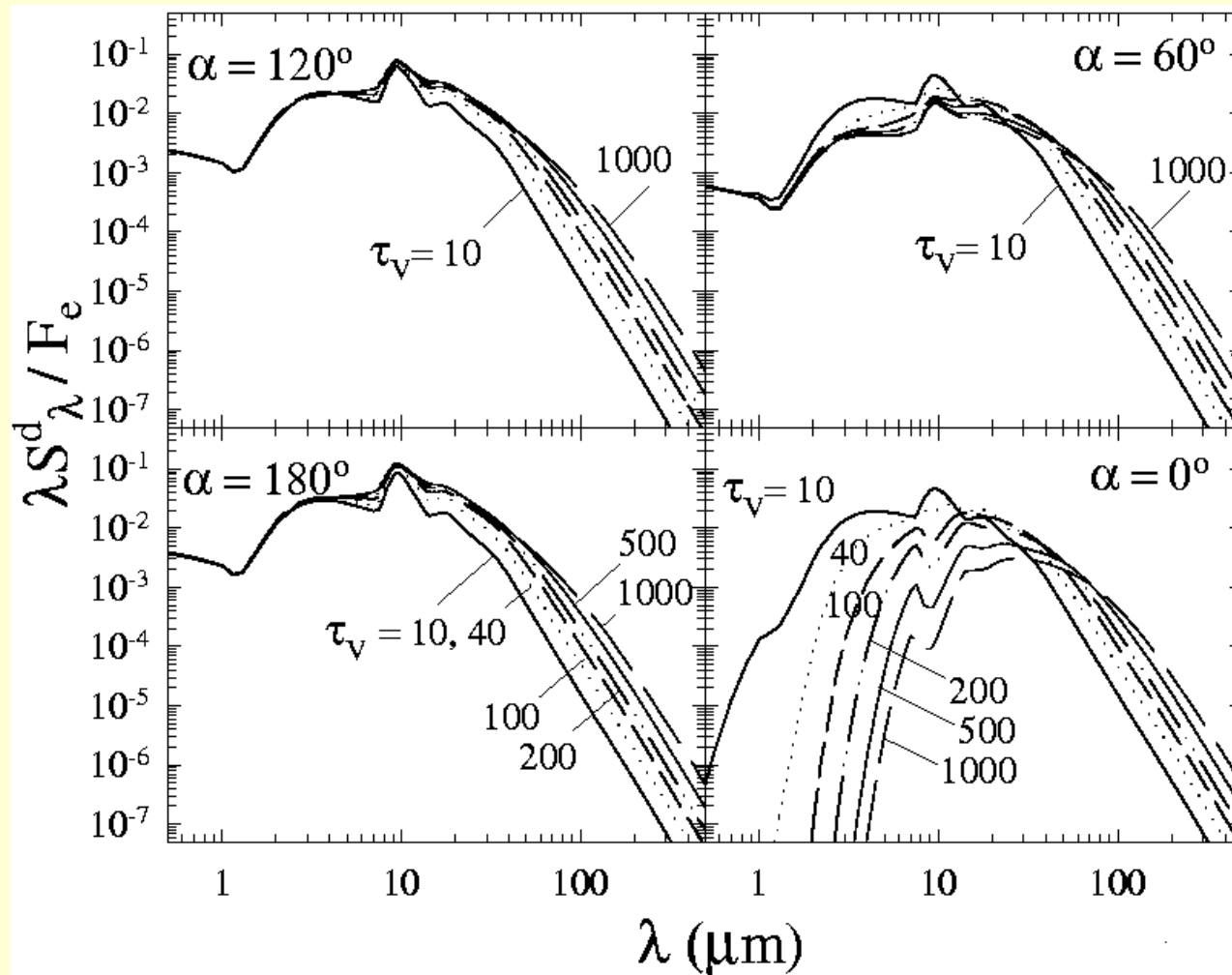
$$p(r) = e^{-\mathcal{N}(r)}$$

Directly-heated Cloud Modeling

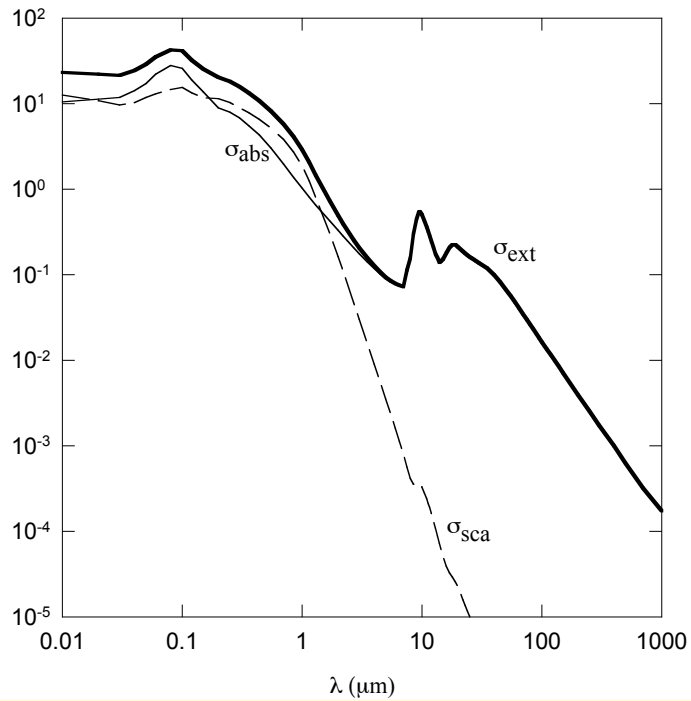


Solutions by DUSTY <http://www.pa.uky.edu/~moshe/dusty/>

Directly Illuminated Clouds



Standard ISM dust x-sections

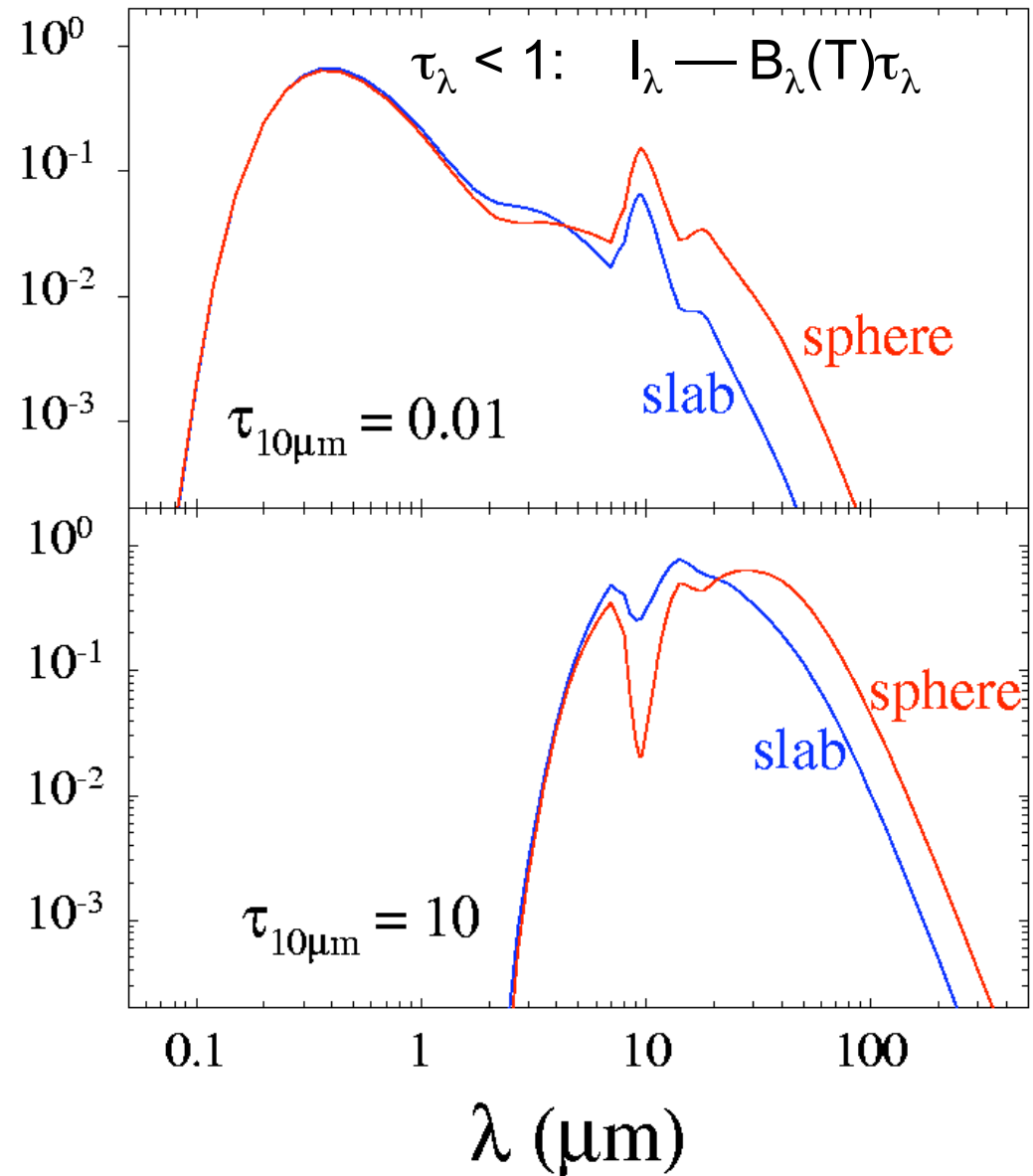


Silicate Features — Basics

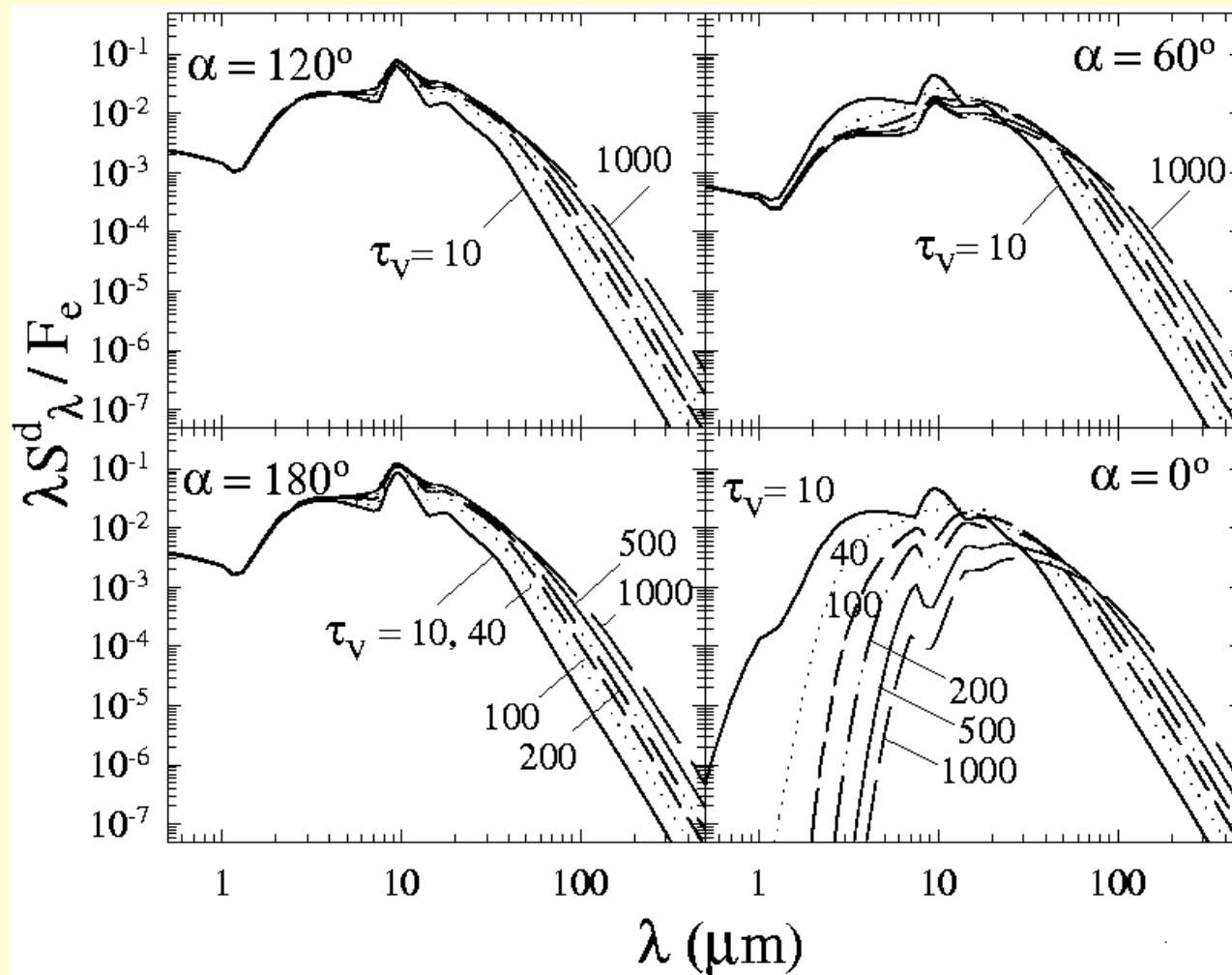
$$I_\lambda = B_\lambda(T)[1 - \exp(-\tau_\lambda)] \quad \{+ I_{in} \exp(-\tau_\lambda)\}$$

$\tau_\lambda > 1$: $I_\lambda \sim B_\lambda(T)$
 T gradient \Rightarrow
 absorption feature:

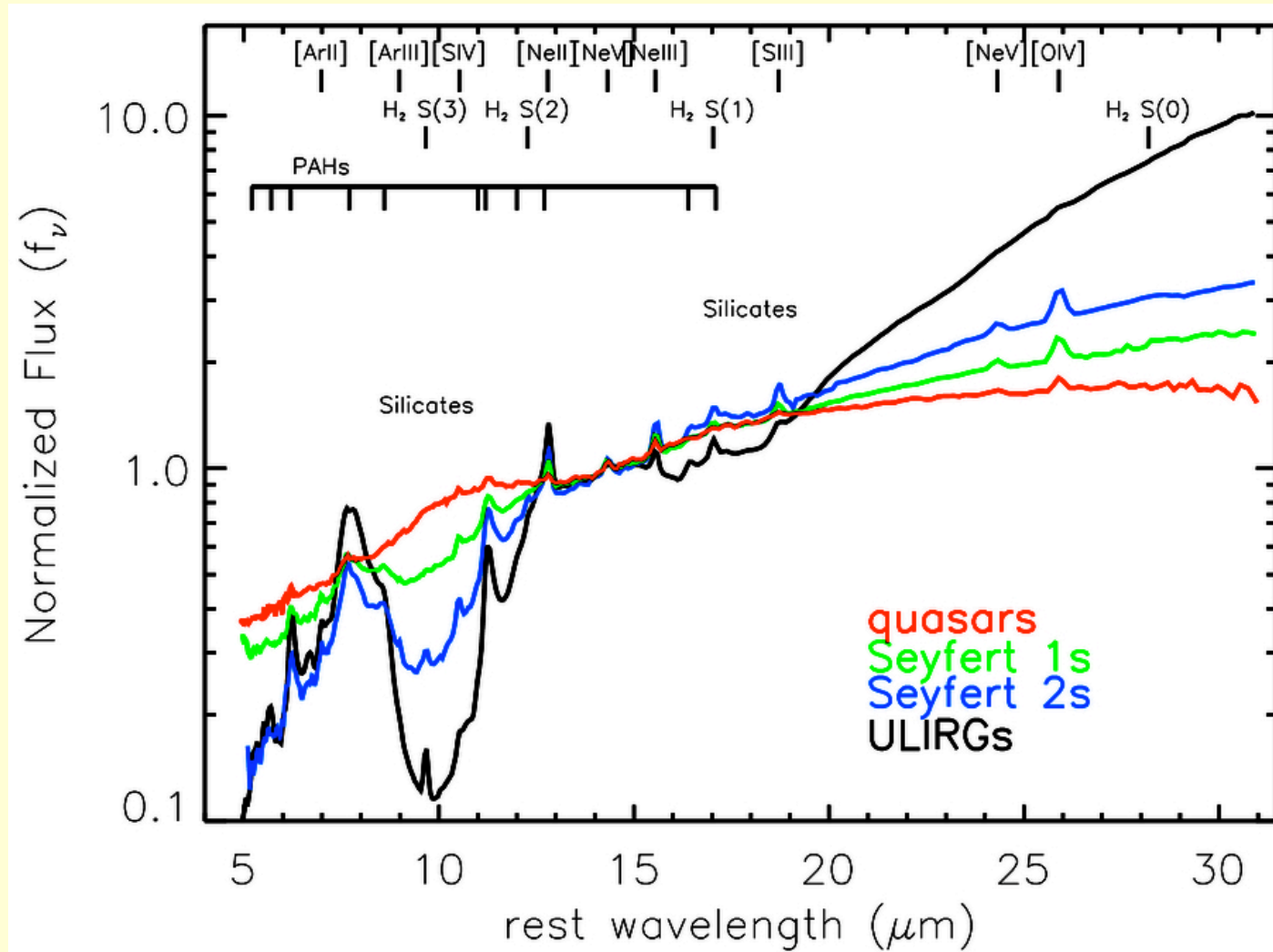
λf_λ



Directly Illuminated Clouds

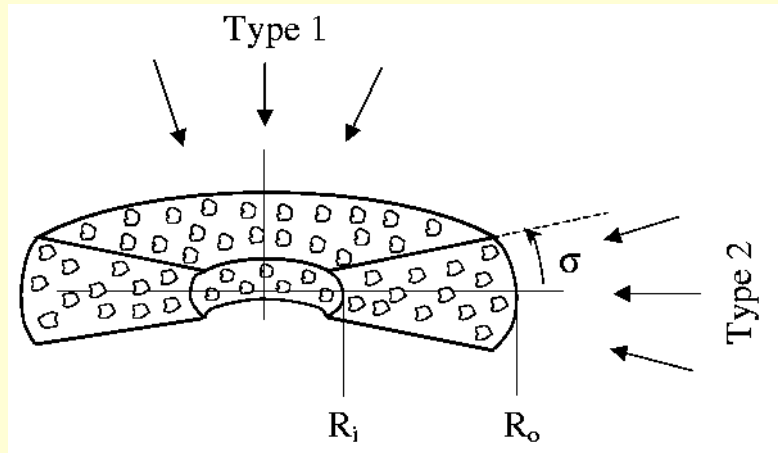


Average SED's



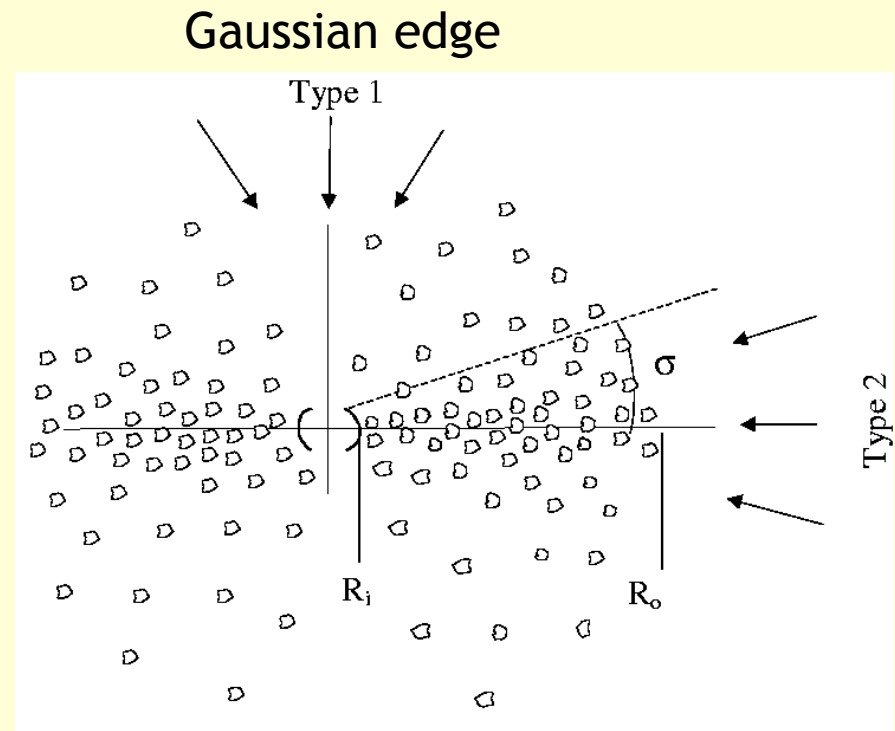
Hao+ '07

AGN Modeling:



sharp edge

$$\mathcal{N}_T(\beta) = \begin{cases} \mathcal{N}_T(0) & \beta < \sigma \\ 0 & \beta > \sigma \end{cases}$$



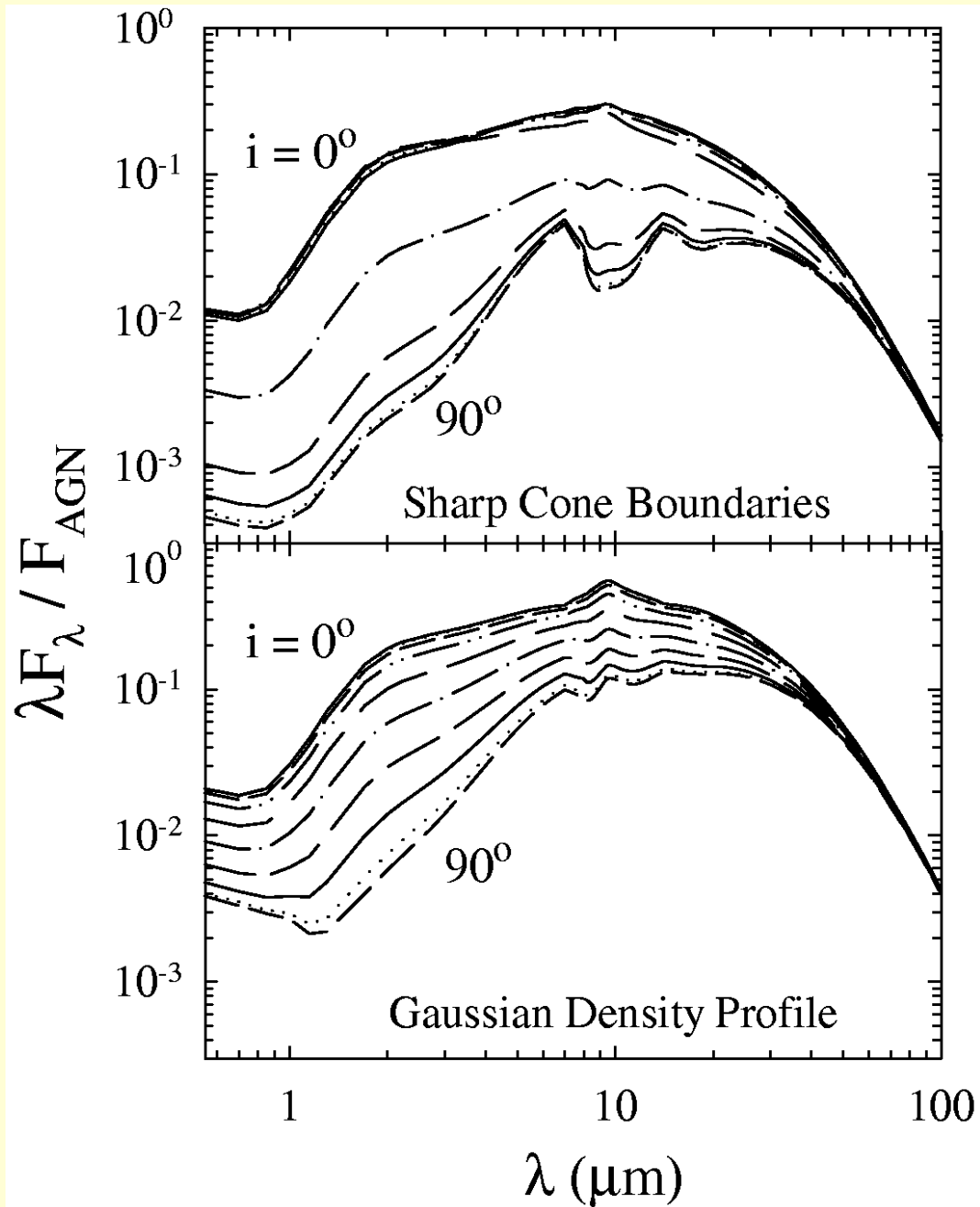
$$\mathcal{N}_T(\beta) = \mathcal{N}_T(0) \exp(-\beta^2/\sigma^2)$$

$$Y = R_o/R_d : T_d = 1500 \text{ K} \quad (R_d = 0.4 \text{ pc } L_{45}^{1/2})$$

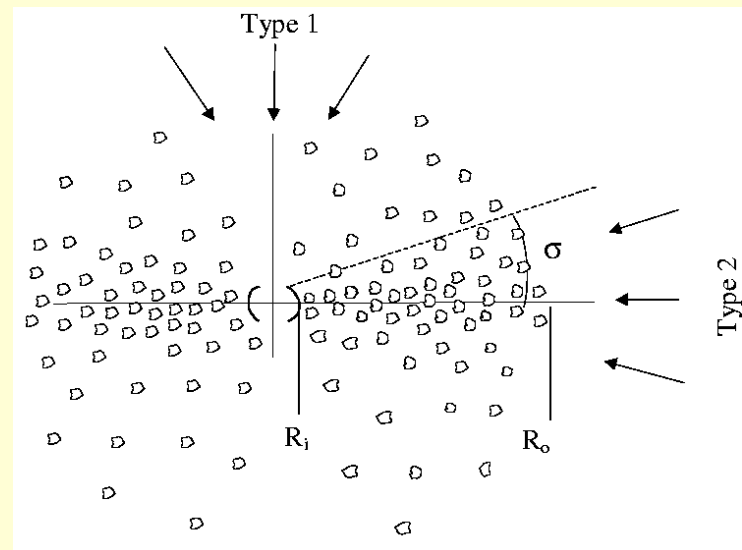
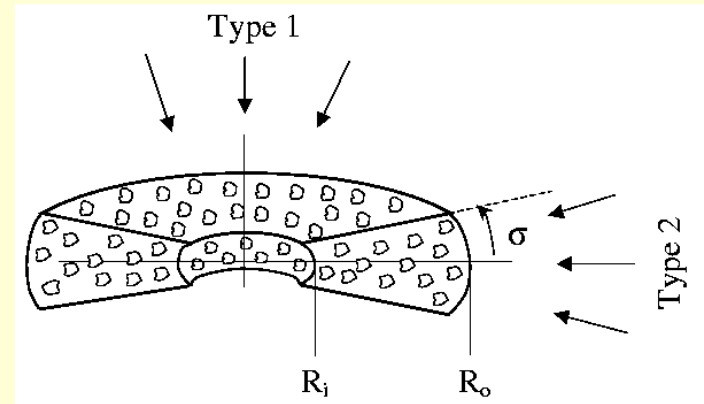
$$\mathcal{N}_0 = \mathcal{N}_T(0), \quad \sigma, \quad q: N(r, \beta) \propto \mathcal{N}_T(\beta)/r^q$$

$$\tau_V$$

$$\mathcal{N}_0 = 5, \tau_V = 60, q = 1, Y = 30, \sigma = 45^\circ$$

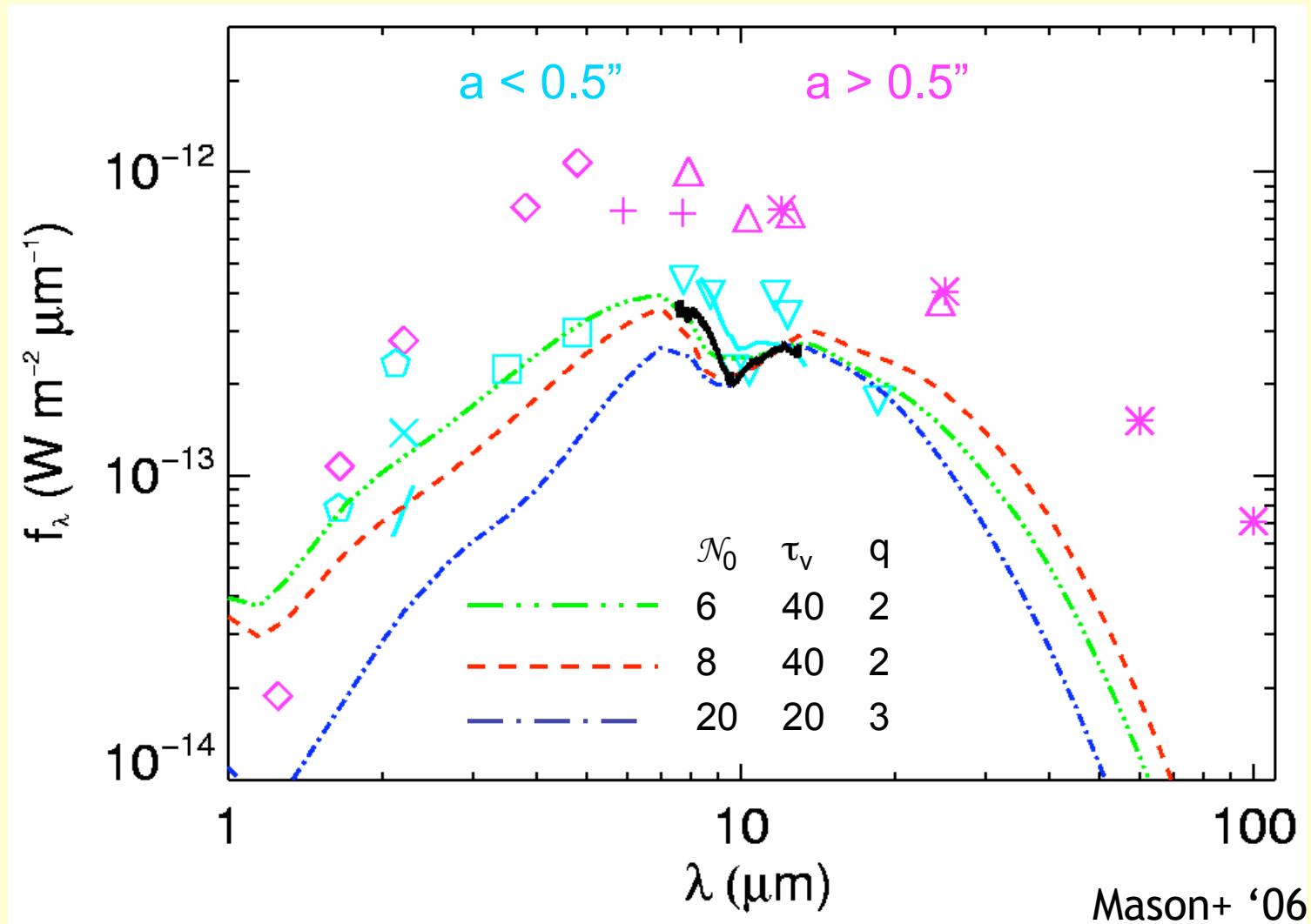


Geometry Effects



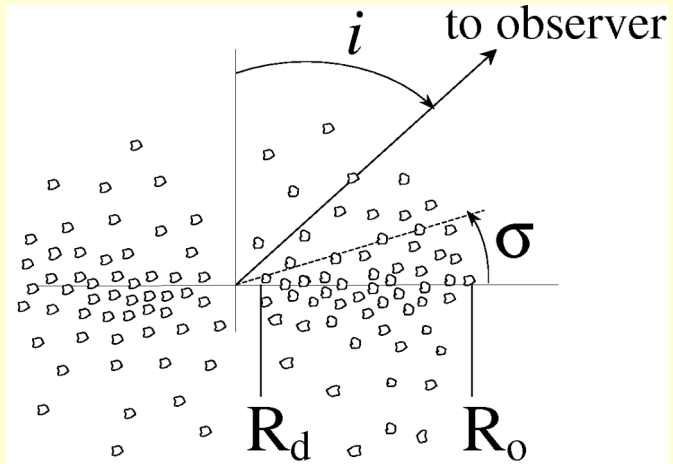
$$N \propto \mathcal{N}_0 \exp(-\beta^2/\sigma^2)/r^q$$

Modeling NGC1068 – Equatorial Viewing!



$L_{\text{Bol}} \text{ — } 2 \cdot 10^{45} \text{ erg s}^{-1}$

Clumpy Torus Modeling

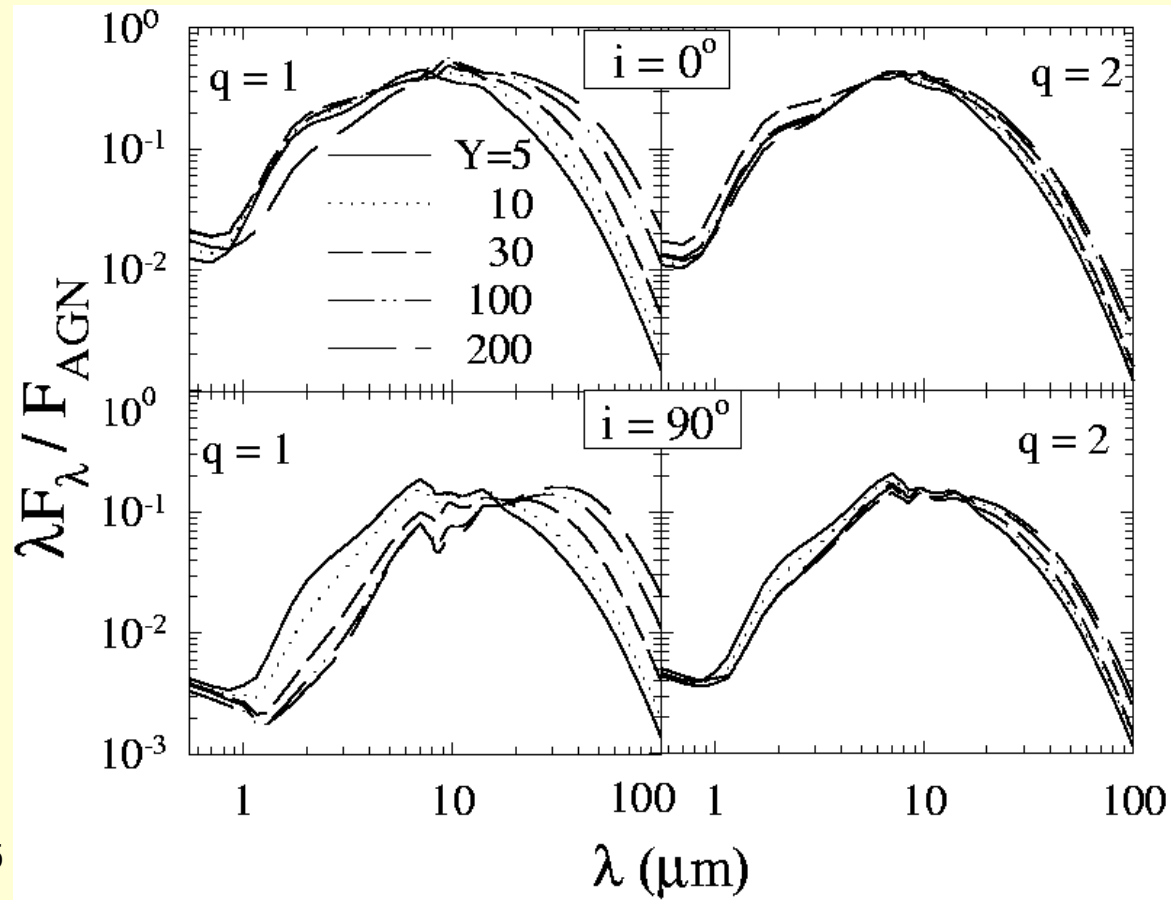


- $\mathcal{N}_0 = 5 - 10$ clouds
- $\sigma = 30^\circ - 60^\circ$
- $\tau_V = 40 - 120$
- $q = 1 - 2$
- $R_d = 0.4L_{45}^{1/2} \text{ pc}; \quad R_o \geq 5 R_d$

$$N \propto \mathcal{N}_0 \exp(-\beta^2/\sigma^2)/r^q$$

Standard ISM dust works fine

Large q — SED Independent of R_{out}

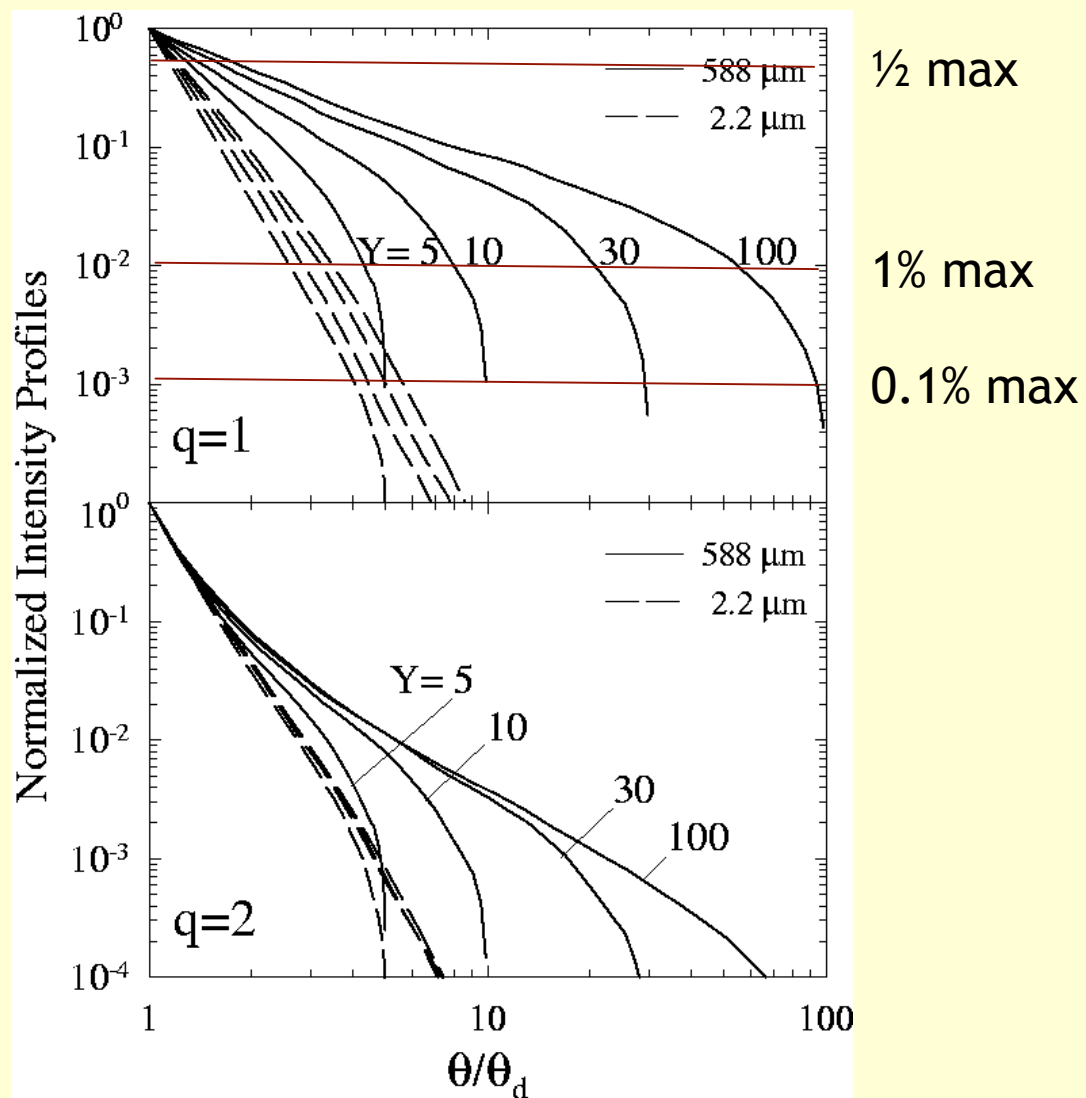


$$R_d = 0.4 \text{ pc } L_{45}^{1/2}$$

$$Y = R_o / R_d$$

$$N \propto r^{-q} \exp(-\beta^2 / \sigma^2)$$

So how big really is the torus?



NGC 1068: $\theta_d \approx 0.02''$

ALMA?

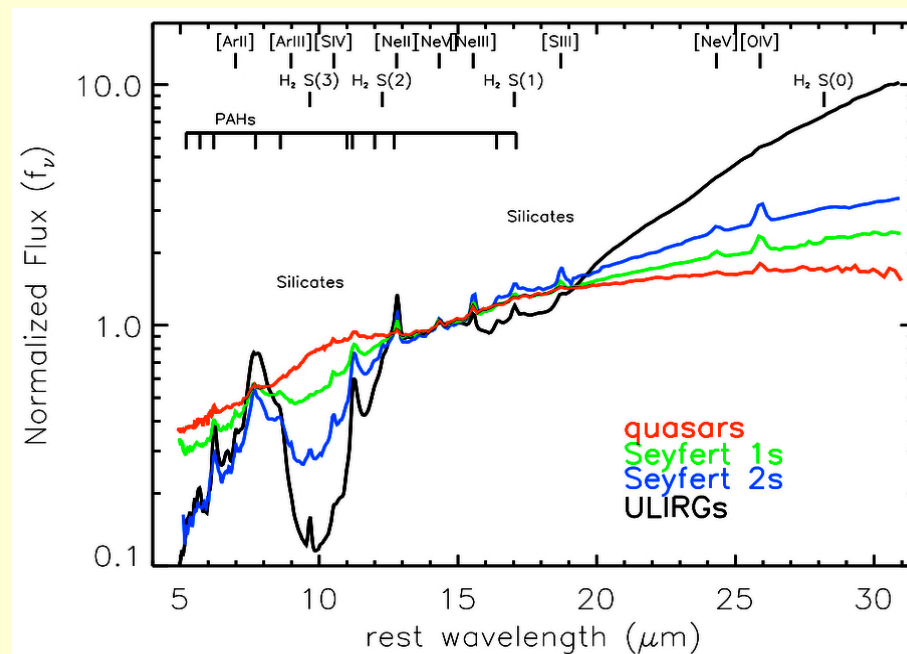
IR Puzzle #2

While its obscuration is highly anisotropic,
the torus emission is nearly isotropic:

Lutz et al '04 — $6\mu\text{m}$ vs 2-10 keV x-rays

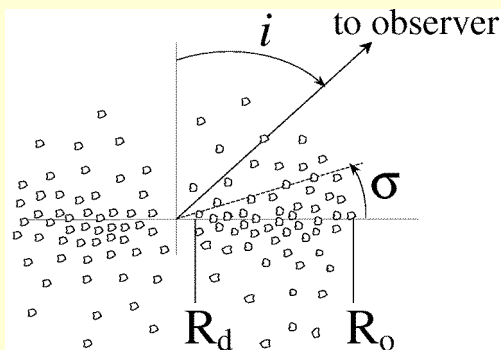
Horst et al '06 — $12\mu\text{m}$ vs 2-10 keV x-rays

Buchanan et al '06 — 5- $35\mu\text{m}$ vs radio



Hao+ 07

Clumpy Torus - Radial Density Variation



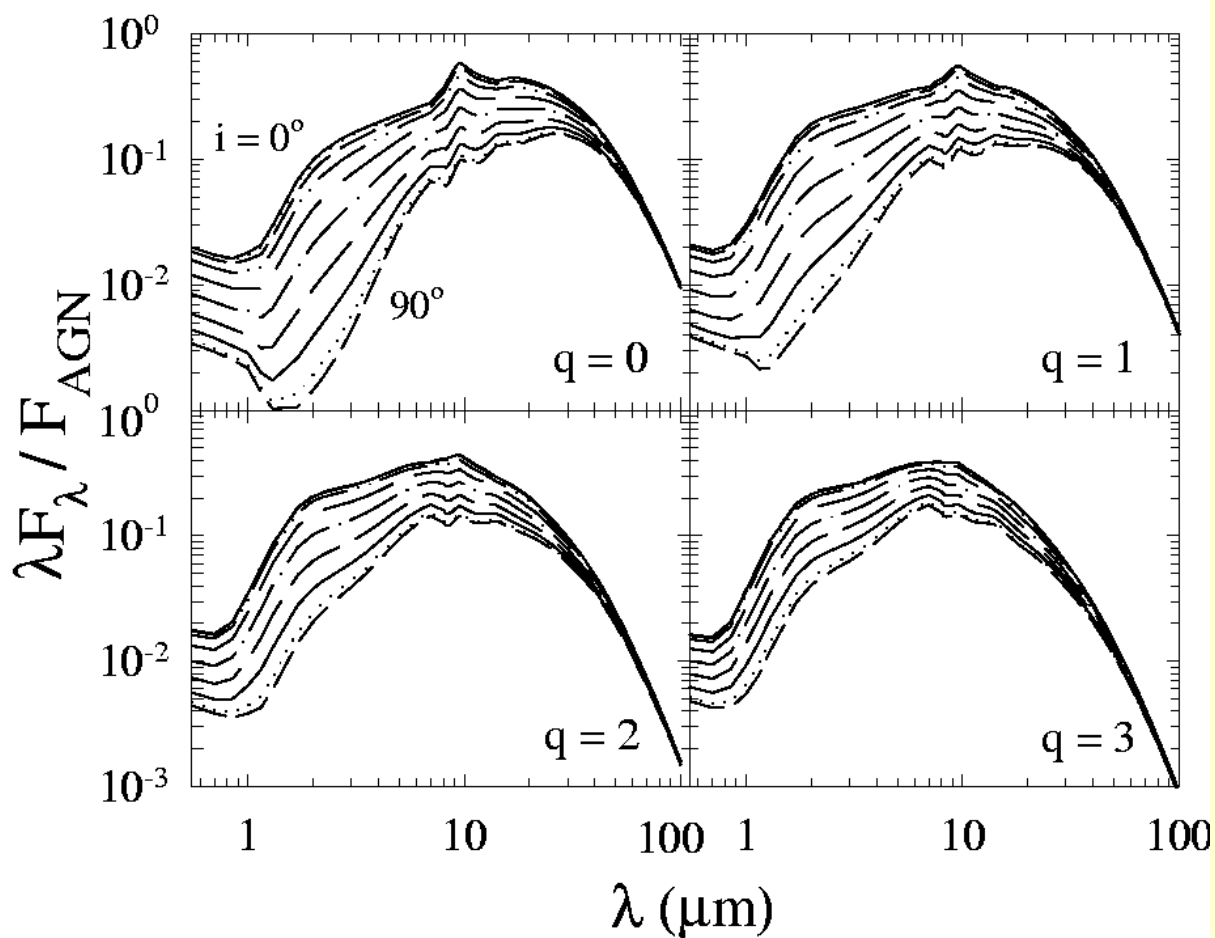
$$N \propto \mathcal{N}_0 \exp(-\beta^2/\sigma^2) / r^q$$

$$\mathcal{N}_0 = 5$$

$$\sigma = 45^\circ$$

$$Y = 30 \tau$$

$$v = 60$$



Large q (steep radial decline) –

Anisotropic obscuration with nearly isotropic emission!

Silicate Features — Clumpy Torus Models

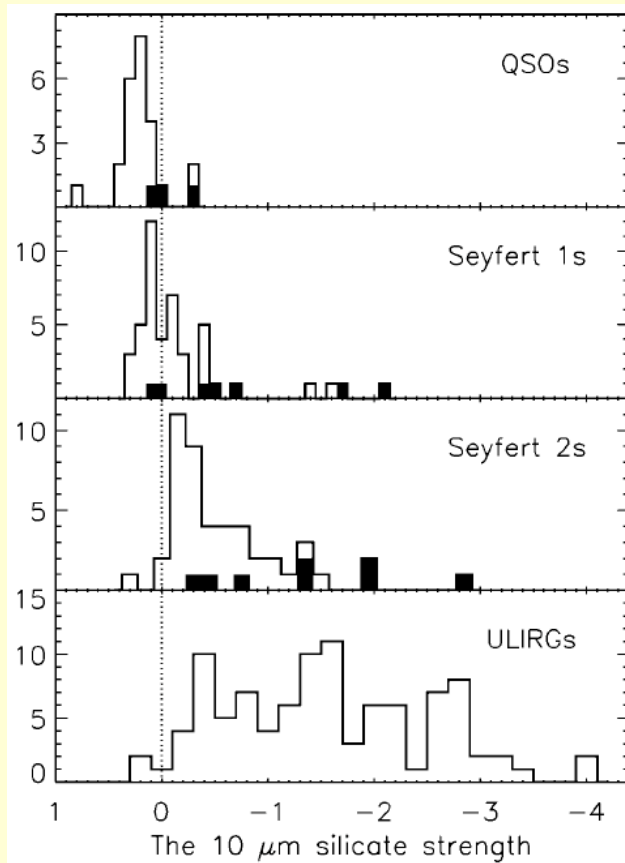
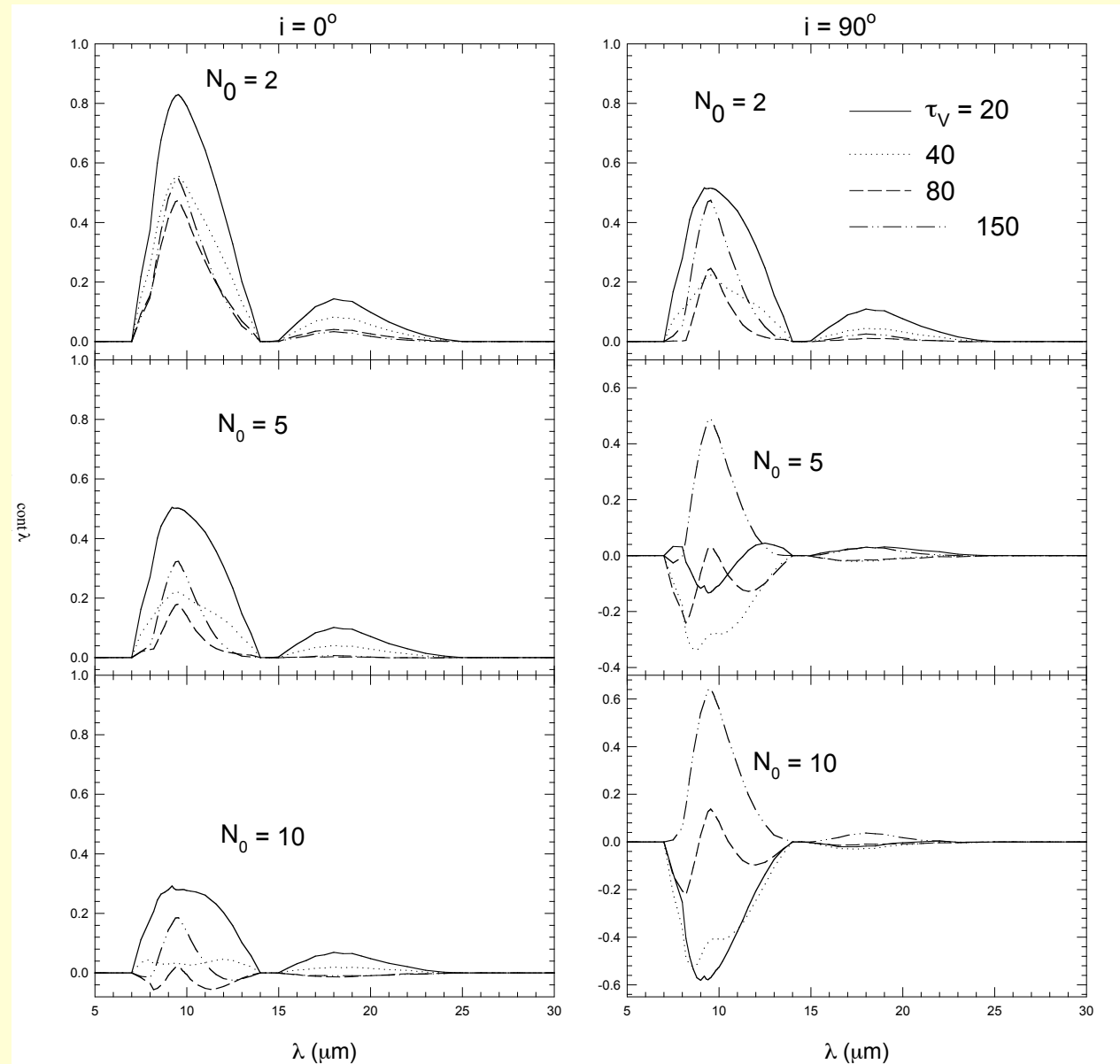


FIG. 2.—Distribution of the 10 μm silicate strength, S_{10} , for QSOs, Seyfert 1s, Seyfert 2s, and ULIRGs. Silicate absorption increases to the right. In QSOs, Seyfert 1s, and Seyfert 2s, the distributions of sources that are also in the ULIRG sample are shaded. The averages of the 10 μm silicate strengths are 0.20 for quasars, -0.18 for Seyfert 1s, -0.61 for Seyfert 2s, and -1.56 for ULIRGs. The range of the silicate strengths are $0 \leq S_{10} \leq 0.4$, $-0.7 \leq S_{10} \leq 0.3$, $-1.6 \leq S_{10} \leq 0$, $-4 \leq S_{10} \leq 0.2$ for most quasars, Seyfert 1s, Seyfert 2s, and ULIRGs.

Hao+ 07



Torus Mass

$$M = \int m_H n_H dV = m_H \int n_H r^2 dr d\Omega \quad N_H = \int n_H d\ell$$

- $\phi = 1$: $M_{\text{tot}} = m_H N_H \Omega \langle r^2 \rangle_{\text{gas}}$
- $\phi < 1$: $M_{\text{tot}} = m_H N_{H,\text{tot}} \Omega \langle r^2 \rangle_{\text{clouds}}$

$$M_{\text{Torus}} \propto N_H R_d^2 \approx 10^3 \sin\sigma N_{H,23} L_{45} Y I_q(Y) M_{\odot}$$

The Eddington Luminosity

$$F_{\text{grav}} = \frac{GMm_p}{r^2} \qquad F_{\text{rad}} = \sigma_T \frac{L/c}{4\pi r^2}$$

$$\Gamma = \frac{F_{\text{rad}}}{F_{\text{grav}}} = \frac{\sigma_T L}{4\pi G c m_p M} = \frac{L}{L_{\text{Edd}}}$$

$$L_{\text{Edd}} = \frac{4\pi G c m_p}{\sigma_T} M$$

$$L_{\text{Edd}} = 1.3 \times 10^{38} \text{ erg s}^{-1} M/M_{\odot} = 1.3 \times 10^{45} \text{ erg s}^{-1} M_7$$

Torus Mass (2)

$$M_{\text{Torus}} = 1.6 \times 10^3 \sin \sigma N_{\text{H},23} L_{45} Y I_q(Y) M_{\odot}$$

$$\frac{M_{\text{Torus}}}{M_{\text{BH}}} = 2 \times 10^{-4} \frac{L}{L_{\text{Edd}}} \sin \sigma N_{\text{H},23} Y I_q(Y)$$

$$I = \begin{cases} Y/3 & q = 0 \\ Y/2 \ln Y & q = 1 \\ 1 & q = 2 \end{cases}$$

Total number of Torus Clouds

$$n_{\text{tot}} = \int n_c dV$$

$$N_c = n_c A_c = n_c R_c^2$$

$$\phi = n_c V_c = n_c R_c^3$$

$$n_{\text{tot}} = \int N_c^3 / \phi^2 dV$$

$$n_{\text{tot}} \approx \mathcal{N}_0^3 / \phi^2$$

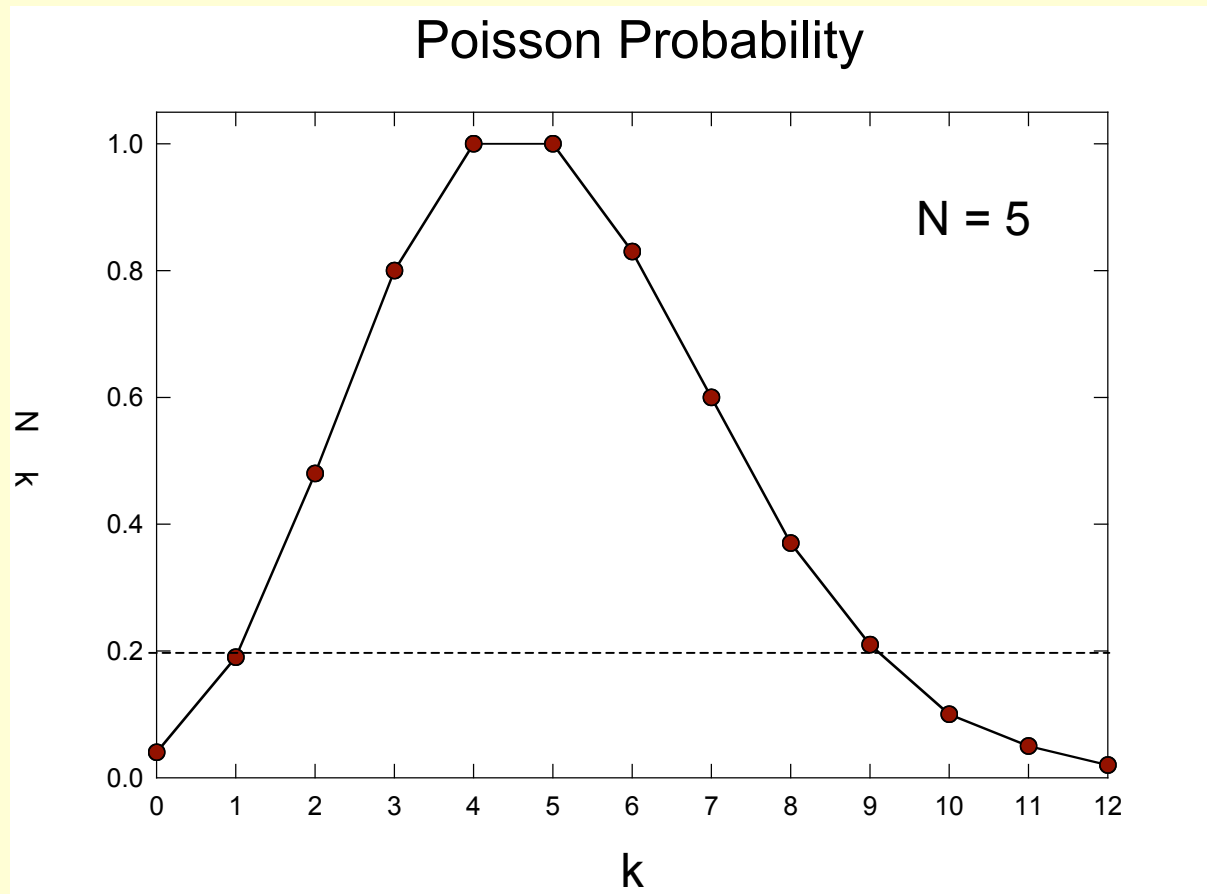
Example: $\phi = 10\% \Rightarrow n_{\text{tot}} = 100 \mathcal{N}_0^3 \approx 10^4 - 10^5$

Clumpy Emission vs Obscuration

- IR emission - average over many los
- x-ray absorption - single los

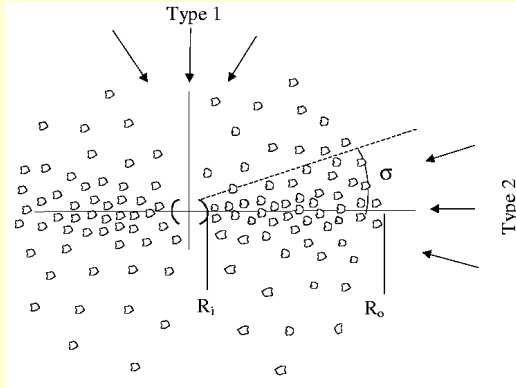
$$P_k \propto N^k/k!$$

$$P_5 = 18\%$$



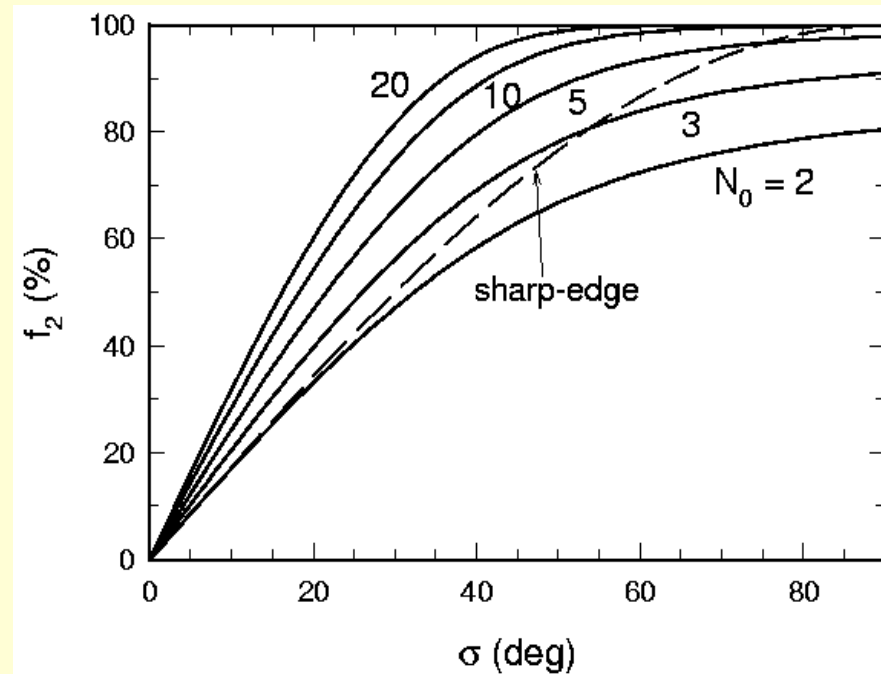
Clumpy Unification

$$N_c(\beta) = \mathcal{N}_0 \exp(-\beta^2/\sigma^2)$$



- Type 1 sources from “type 2 viewing”, and vice versa
- Flips between type 1 & 2 (Aretxaga et al 99)
- L variations of f_2 may arise from either σ or N_0 or both

AGN type is a viewing-dependent **probability!**



f_2 depends on both σ and \mathcal{N}_0 !