## Outline

- Introduction
  - Observational motivation; constraints on timescales
  - Mechanisms driving disc evolution (qualitative)
- Gas dynamics
  - Basic photoevaporation theory
  - Evolutionary models; comparison to observations
- Dust dynamics (and growth)
  - Forces affecting dust: diffusion, gas-drag, settling
  - Introduction to grain growth and planetesimal formation
- "Transition" discs
  - Observational review
  - Comparison to models

### Why should we care about dust?

- Dust is most of what we see when we observe protoplanetary discs.
- Dust dominates disc opacity, so thermal structure of the disc depends on dust heating & cooling.
- Most(ish) heavy elements in discs are in solid phase, so "dust" is the primary absorber of highenergy photons. Dust therefore has a strong influence on gas disc evolution via the MRI.
- Dust represents the "building blocks" for planets.

### What forces affect dust in discs?

- Dust "grains" in discs are subject to two main forces:
  - Gravity
  - Aerodynamic drag
- Crucially, however, dust is NOT subject to gas pressure. This is the origin of most differential gas-dust dynamics.
- Drag force on an individual (spherical) grain is:

$$F_{\rm D} = -\frac{1}{2}C_{\rm D} \cdot \pi s^2 \cdot \rho_{\rm g} v^2$$

 Drag coefficient C<sub>D</sub> is simple in Epstein regime (depends only on thermal velocity of gas); depends on Reynolds number in Stokes regime.

# Vertical settling (no turbulence)

• Useful to define "stopping timescale". In Epstein regime:

$$t_{\rm s} = \frac{mv}{|F_{\rm D}|} = \frac{\rho_{\rm d}}{\rho_{\rm g}} \frac{s}{v_{\rm th}}$$

- This is ~Is for micron-sized grains, so such grains are very well coupled to the gas. Often write  $T_s = t_s \Omega_k$  (dimensionless).
- Equate vertical forces (gravity and drag):

$$m = \frac{4}{3}\pi s^{3}\rho_{d}$$

$$m\Omega_{K}^{2}z = \frac{4}{3}\pi s^{2}v_{th}\rho_{g}v$$

$$t_{settle} = \frac{z}{v_{settle}} = \frac{v_{th}}{\Omega_{K}^{2}}\frac{\rho_{g}(z)}{\rho_{d}}\frac{1}{s}$$

 For micron-sized grains, this results in settling timescales of order 10<sup>5</sup>yr. Expect significant sedimentation of grains > 1μm over disc lifetime. (Turbulent effects: lectures by Hubert Klahr.)

#### Radial drift

Whipple (1972); Weidenschiling (1977); Takeuchi & Lin (2002)

- Two regimes:
  - "Dust": small particles are well-coupled to the gas, orbit at gas velocity. Migrate relative to gas because they don't feel pressure gradients.
  - "Rocks": larger particles poorly-coupled to gas, orbit at Keplerian velocity. Gas is sub-Keplerian, so rocks feel a "headwind" drag force.
- Gas orbital velocity is sub-Keplerian:

$$\frac{v_{\phi,\text{gas}}^2}{R} = \frac{GM_*}{R^2} + \frac{1}{\rho_g}\frac{dP}{dR}$$

• If  $P \sim R^{-n}$  and disc is locally isothermal, then

$$v_{\phi,\text{gas}} = v_{\text{K}}(1-\eta)^{1/2}$$
,  $\eta = n \frac{c_{\text{s}}^2}{v_{\text{K}}^2}$ 

 Gas is typically sub-Keplerian by ~100ms<sup>-1</sup> at 1AU. This is small fraction (~0.1%), but causes a STRONG HEADWIND!

#### Radial drift

Whipple (1972); Weidenschiling (1977); Takeuchi & Lin (2002)





$$\frac{d}{dt}(rv_{\phi,d}) = -\frac{r}{t_s}(v_{\phi,d} - v_{\phi,g})$$

• Assume particles spiral in on ~circular orbits:  $v_{\phi,d} \simeq v_{\phi,g} \simeq v_K$ 

- Azimuthal EoM becomes:  $v_{\phi,d} v_{\phi,g} \simeq -\frac{1}{2} \frac{t_s v_K}{r} v_{r,d} = -\frac{1}{2} T_s v_{r,d}$
- Radial EoM LHS is negligible (to  $O(h^2/r^2)$ ), so:

$$\frac{v_{\phi,d}^2}{r} - \frac{v_{\phi,g}^2}{r} - \eta \frac{v_K^2}{r} - \frac{1}{t_s} v_{r,d} \simeq 0$$
$$\frac{2v_K}{r} (v_{\phi,d} - v_{\phi,g}) - \eta \frac{v_K^2}{r} - \frac{1}{t_s} v_{r,d} \simeq 0$$

#### Radial drift

Whipple (1972); Weidenschiling (1977); Takeuchi & Lin (2002)

$$-\frac{v_{\mathrm{K}}}{r}T_{\mathrm{s}}v_{\mathrm{r,d}} - \eta\frac{v_{\mathrm{K}}^{2}}{r} - \frac{1}{t_{\mathrm{s}}}v_{\mathrm{r,d}} \simeq 0$$

• Substituted first term from azimuthal EoM. Now divide by  $(v_K/r)$ , and note that:  $T_s = t_s \Omega_K = t_s \frac{v_K}{r_s}$ 

$$v_{\mathrm{r,d}}T_s + v_{\mathrm{r,d}}T_s^{-1} = -\eta v_\mathrm{K}$$

$$v_{\rm r,d} = -\frac{\eta v_{\rm K}}{T_s + T_s^{-1}}$$

- $v_{r,g}$  depends only on viscosity, and  $\eta$  only on gas pressure.
- Plot in terms of: T<sub>s</sub> scales linearly with particle size, but also depends on conditions in gas disc.

#### Radial drift Whipple (1972); Weidenschiling (1977); Takeuchi & Lin (2002)



$$v_{\rm r,d} = \frac{v_{\rm r,g} T_s^{-1} - \eta v_{\rm K}}{T_s + T_s^{-1}}$$

- At the peak, this leads to large drift velocities, ~1000cm/s.
- For dM/dt =10<sup>-8</sup>M<sub>☉</sub>yr<sup>-1</sup> & α=0.01,T<sub>s</sub>=1 corresponds to a size of ~85cm. As disc evolves the peak shifts to smaller grains (lower gas density).
- Decay timescales at peak are very short, ~150yr at 1AU.

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- Decay timescales at peak are very short, ~150yr at IAU.

Planetesimal formation must occur very rapidly to overcome this barrier. This is often referred to as the "metre-size problem".

# Radial drift in "turbulent" discs



#### Armitage (2007)

If local pressure maximum has length-scale  $\Delta r$ , then pressure gradient (~P/ $\Delta r$ ) exceeds global pressure gradient (~P/r). "Concentration timescale" is therefore shorter than the drift timescale by ~ $(r/\Delta r)^2$ .

- In quiescent, viscous discs pressure gradient is outwards, so all gas is sub-Keplerian and particles drift inwards.
- In general, however, particle drift opposes pressures gradient: particles move towards pressure maxima.
- If disc is not quiescent, this can cause significant enhancements of the local dust/gas ratio for particles with T<sub>s</sub>~1.

## Radial drift in "turbulent" discs

Haghighipour & Boss (2003); Rice et al. (2004, 2006); Durisen et al. (2005)

#### Figures from Rice, Lodato et al. (2004)



Concentration of particles in this manner can dramatically increase collision rates, and *may* provide a solution to the metre-size problem.

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# Clumping in planet-induced structure

e.g. Pardekooper & Mellema (2004,2006); Rice et al. (2006)



Pardekooper & Mellema (2006)

- Presence of a planet alters structure of gas disc: spiral arms for low-mass planet; tidal gap for massive planet.
- Dust is concentrated in these local pressure maxima.
- Low-mass planet makes dust spiral arms.
- In gap-opening case, tend to starve inner region of dust and reduce local dust-to-gas ratio (Rice et al. 2006).

#### "Sweeping-up" of small grains RDA & Armitage (2007); see also Garaud (2007)



- Clearing phase of gas disc: viscosity + photoevaporative wind.
- "Two-fluid" model of dust, similar to Takeuchi et al. (2005).
- Once gap opens, pressure gradients concentrate dust at disc edge.

# Grain growth & planetesimal formation

e.g. Lissauer (1993); Youdin & Shu (2005); Dullemond & Dominik (2005); Dominik et al. (PPV)

- In standard theory, dust grains agglomerate to form planetesimals via "sticking" collisions.
- This model is viable, but many parameters are very uncertain. Sticking and fragmentation probabilities are especially problematic. (Growth to cm sizes seems OK, but larger grains stick much less efficiently.)
- Many theories invoke some variant of the Goldreich-Ward (1973) mechanism: grav. instability in a thin dust layer.
- Problems exist here also, primarily in how to concentrate the dust sufficiently. Various suggestions exist in the literature: settling, radial drift (Youdin & Shu 2005), photoevaporation (Throop & Bally 2005), etc.

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## Dust dynamics: summary

- Gas-grain interactions dominated by aerodynamic drag, arising because grains don't feel gas pressure.
- Grains with  $T_s \sim I$  are most susceptible to radial drift, and decay on very short timescales (<1000yr).
- Growth to ~mm-cm size (agglomeration) can occur in <1Myr.
- Planetisemal formation must occur sufficiently rapidly to overcome the "metre-size barrier".
- Effects of turbulence may be significant (see lectures by Klahr).
- Planetesimal formation still very poorly understood. Models exist, but all have their associated problems.

#### "Transition discs"



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# Why do we care?



IR Class II

#### IR Class III

- CTTs evolve into WTTs, and the transition is fast.
- Objects "caught in the act" of clearing provide a key test for models.

# Need spatially resolved data...



Qi et al. (2004): CO J=3-2 line (SMA)



- As we will see, SEDs are essentially degenerate between different models.
- Spatially resolved observations are key to breaking these degeneracies.
- IAU at I40pc ⇔ 7mas.
- Existing (sub-)mm observations have already resolved some spatial structure.
- Ideal (faint) targets for optical/ IR interferometry!

- "Properties between those typical of CTTs & WTTs" little consistency in how this is defined observationally.
- Najita et al. (2007) adopt the following definition:

"Objects are classed as transition objects if they show weak or no infrared excess shortward of 10µm and a significant excess at longer wavelengths."

- Based on Spitzer IRS spectra, they classify 12 objects in Taurus as "transitional".
- Demographically, these 12 objects show systematically lower accretion rates than CTTs of the same disc mass. Only 2/12 however, are spectroscopic WTTs.



#### • I prefer a more model-based definition:

"Transition objects have discs which are optically thin at shorter wavelengths and optically thick at longer wavelengths."

- Such a definition removes potential selection biases due to observed wavelength ranges, and requires a real physical change in the radial structure of the disc.
- This is more stringent that the Najita et al. (2007) criterion: only 6 of their 12 objects meet satisfy it.
- Unbiased samples will require observations at longer wavelengths: Spitzer is not sensitive to large "holes" (>20 -50AU, depending on spectral type).



- Physically, transitional SEDs are consistent with a hole or gap in the (dust) disc.
- Dust settling/growth can also give rise to a weakened IR excess: optical depth criterion should reject such objects.
- Several models for transition objects exist:
  - Clearing by planets
  - Photoevaporation/viscous clearing
  - Others: photophoresis, dust settling, MRI enhancement, etc.
- All such models predict very similar SEDs in the IR, so how do we distinguish between different modes?

# Disc clearing by planets

e.g. Papaloizou & Lin (1984); Takeuchi et al. (1996); Nelson et al. (2000)



Gap-opening criterion is essentially that the tidal torques from the planet must exceed the viscous torques in the disc. Can be written as:

$$q \gtrsim \frac{40}{\mathcal{R}} \simeq 40 \alpha \left(\frac{H}{R}\right)^2$$

- A sufficiently massive planet will open a gap in a disc, resulting in a "transitional" appearance.
- Gap-opening criterion is independent of surface density.
- Once gap opens planet undergoes Type II migration. Accretion across gap is a strong function of planet mass.
- For α=0.01, planets more massive than ~0.5MJup will open a gap.

# Disc clearing by planets

 Dynamical effect of a planet in a disc is to clear a gap or hole on a short (dynamical) timescale (e.g. Rice et al. 2003; Quillen 2004; Varnière et al. 2006).



# Disc clearing by planets

- Dynamical effect of a planet in a disc is to clear a gap or hole on a short (dynamical) timescale (e.g. Rice et al. 2003; Quillen 2004; Varnière et al. 2006).
- Models of these holes are consistent with observed infrared SEDs (e.g. Rice et al. 2003, 2006).
- Models usually assume presence of planet, and do not consider formation issues.
- Not clear whether accretion will persist across the gap over long timescales (see Lubow & d'Angelo 2006).



## Properties of inner hole models

- Planet-induced gaps/holes:
  - Disc masses typical of CTTs.
  - Accretion across gap likely ("leaky barrier"), although strong function of planet mass (e.g. Lubow & d'Angelo 2006).
  - Reduced dust/gas ratio inside gap (in <mm grains, Rice et al. 2006).
  - Hole sizes typically few planet radii, so <30-50AU.
- "Photoevaporated" holes:
  - Hole sizes ~uniformly distributed ( $\geq$ 1.5AU).
  - Little or no accretion ( $\leq 10^{-10} M_{\odot} yr^{-1}$ ).
  - Low disc mass (~ few M<sub>Jup</sub>).
  - Should represent ~I-I0% of total (CTT+WTT) population.

# Discriminating between models

RDA & Armitage (2007); see also Najita et al. (2007)



- Explore range of allowed parameters: accretion rates and disc masses.
- Combine with toy planet+disc model to compare to data. (Planet model adapted from Lubow et al. 1999 and Lubow & d'Angelo 2006).

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## Transition discs: summary

- Current data suggest that accreting:non-accreting ratio in transition objects is between 1:1 & 3:1 (Sicilia-Aguilar et al. 2006; Najita et al. 2007).
- No single object definitively matches any model(!): statistical approach seems best.
- Currently number statistics are poor (~15 objects known), and selection biases unclear.
- Multi-wavelength data essential: need more disc masses and accretion rates (especially meaningful upper limits for WTTs).
- Spatial scale (~IOAU) makes these ideal(ish) targets for the VLTI!

# Recommended reading...

- Observations: Beckwith et al. (1990); Kenyon & Hartmann (1995); Haisch et al. (2001); Andrews & Williams (2005).
- Theory: Pringle (1981); Hollenbach et al. (1994); Hartmann et al. (1998); Clarke et al. (2001); Weidenschilling (1977).
- Evolution of the protoplanetary cloud and formation of the earth and the planets, Safronov (1969).
- Recent reviews:
  - PPIV: Hollenbach et al., Calvet et al., Clarke et al.
  - PPV: Dullemond et al., Meyer et al.; Najita et al., Natta et al., Dominik et al.
- Other: lecture notes by Phil Armitage (astro-ph/0701485)