

Two-layer modeling of the circumstellar environment of π^1 Gru with VLTI/AMBER

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I. Abstract

The aim of this work is to determine the physical and geometrical parameters characterizing the giant S-type star π^1 Gru and its circumstellar environment. These parameters come from the literature and from the fit of the ISO/SWS spectrometric measurements with the radiative transfer numerical code DUSTY. The fit of the interferometric AMBER/VLTI measurements with an analytical thin-layer model reveals the existence of a double circumstellar layer.

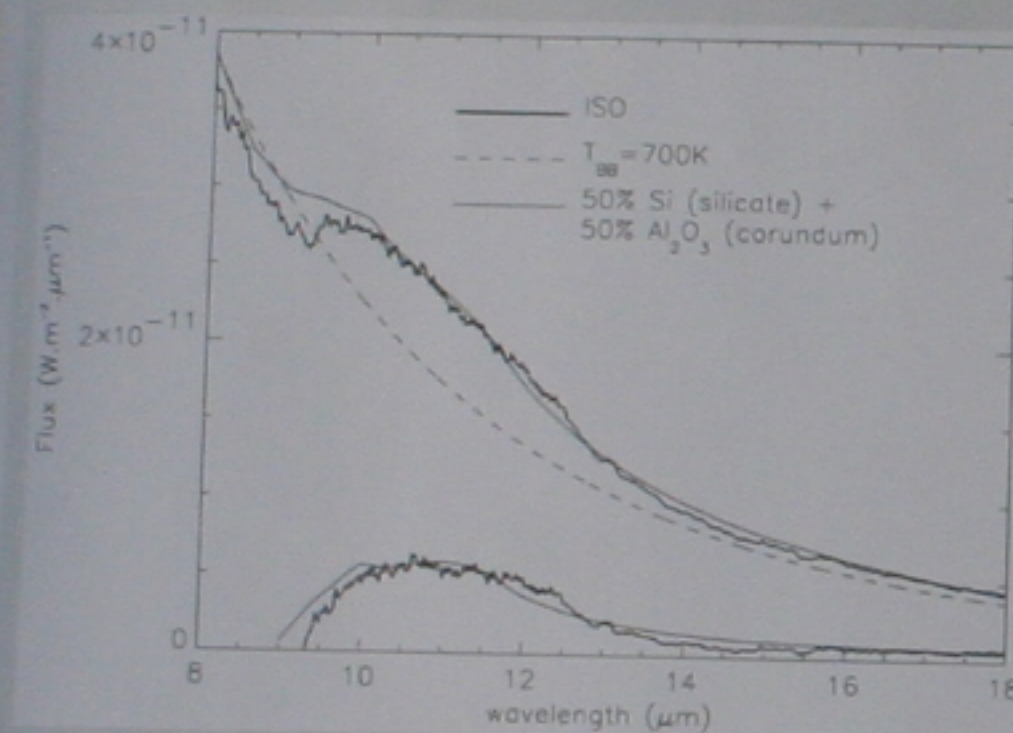
II. S-type star characteristics

Spectral feature	ZrO bands	
	INTRINSIC	EXTRINSIC
Techneium	Tc-rich	Tc-poor
K-[I2]	>0.86	<0.86
F(12 μ m)/F(2.2 μ m)	≈ 0.1	<0.1
Circumstellar dust	detectable	undetectable
Mass-loss rate (M_{\odot}/yr)	>10 ⁻⁷	<10 ⁻⁸
Ratio of S stars (solar neighbourhood)	64 \pm 5%	36 \pm 5%
Mass (M_{\odot})	~1 to ~5	1.5 to 2
Evolutionary scenario	M-S-C (AGB)	Ba-S (RGB or E-AGB)

III. Central star parameters

PII Gru	
General description	Intrinsic irregular variable of type Srb
Variation cycle	150 days
Distance	153 pc
Binary nature	Double (2.71" of separation, so that the companion can be neglected)
Visual magnitude	At maximum V brightness: 5.4
	At minimum V brightness: 6.7
C/O ratio	0.97
Effective temperature	3100 K
Angular diameter	19 mas
Luminosity	7600 L_{\odot}

IV. Fit of the ISO spectra with DUSTY



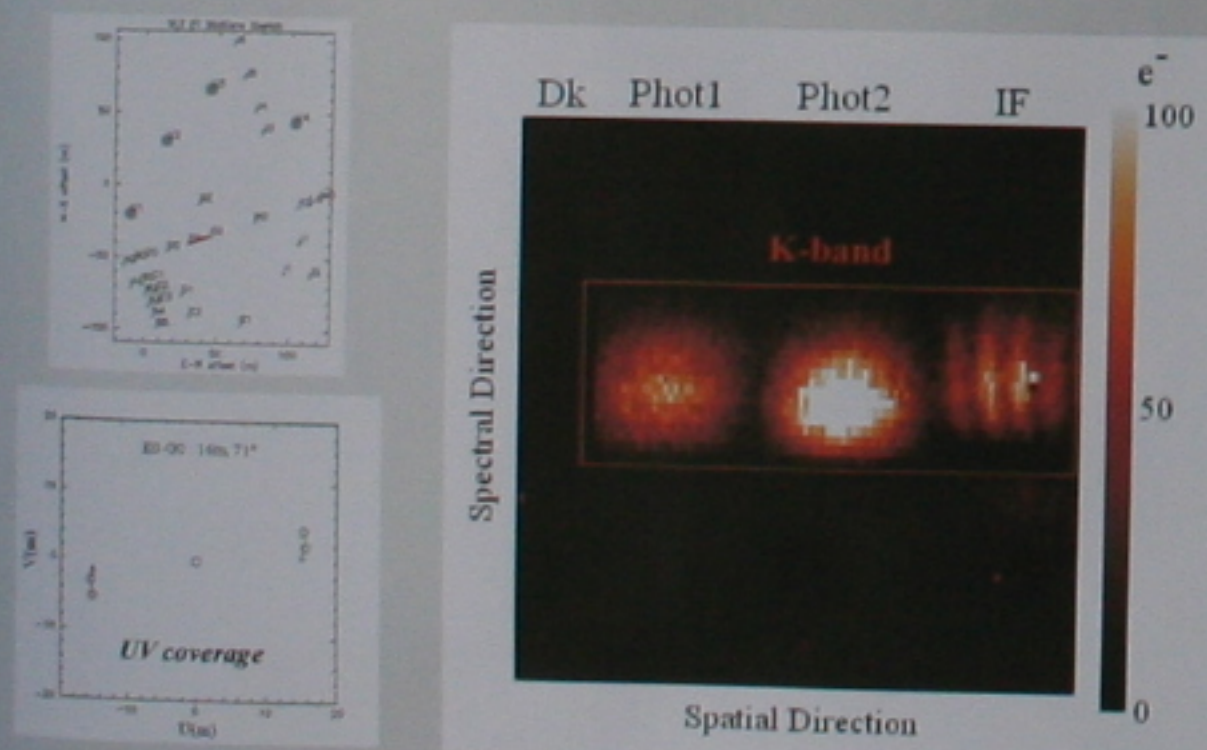
Dust feature	
Chemical composition	50 \pm 5% of Silicate and 50 \pm 5% of Corundum
Condensation temperature (K)	1500
Inner boundary radius (mas)	37 \pm 1
Optical depth @ 10 μ m	0.016 \pm 0.001
Dust density distribution	$\propto r^{-1.7}$
Single grain size distribution (μ m)	0.1
Thickness (in r_{in})	5000

V. AMBER/VLTI observations

AMBER (Astronomical Multi Beam Recombiner) is the VLTI beam combiner, operating in the near-infrared, using optical fibers. The instrument can operate at a resolution up to 10⁴ and delivers spectrally dispersed visibilities.

π^1 Gru was observed on 2005/07/14 with the single AT-VLTI baseline E0-G0 (16m, 71°) in the low-resolution (R=35) K-band spectral mode.

Its calibration star δ Gru, of spectral type M4.5IIIa, was observed under the same instrumental conditions.



Short exposure frame of the π^1 Gru signal on the AMBER detector.

First column (Dk): masked pixels (dark current).

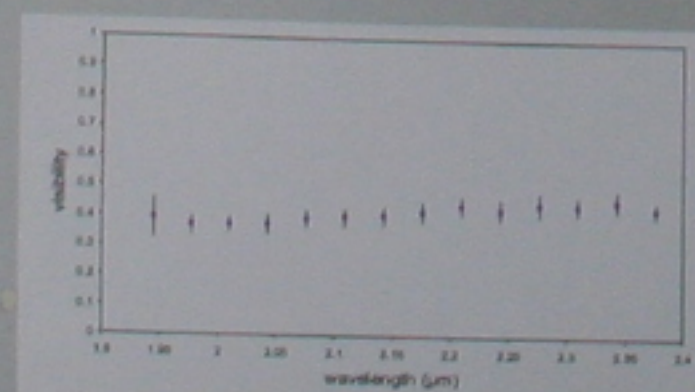
Second (Phot1) and Third (Phot2) columns: beams coming from the first and the second telescope respectively.

Fourth column (IF): fringe pattern obtained by superposition of the two beams.

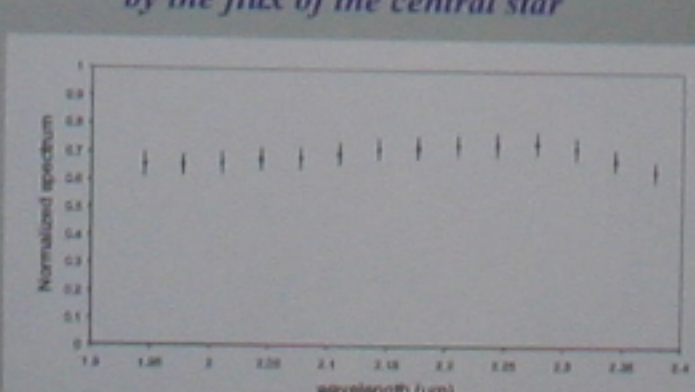
Calibration process:

- ✓ Cosmetics and flat field
- ✓ Image selection criteria
- ✓ Spectral calibration
- ✓ Instrumental calibration

Calibrated visibilities



Calibrated spectrum normalized by the flux of the central star



VI. The analytical thin-layer model

Expression of the emergent intensity, solution of the radiative transfer equation through an optically and geometrically thin layer:

$$dI_{\lambda} = (S_{\lambda} - I_{\lambda}) d\tau_{\lambda} \quad \text{with:} \quad d\tau_{\lambda} = \kappa_{\lambda} ds \quad \text{and:} \quad \kappa_{\lambda} = \kappa_{a\lambda} + \kappa_{s\lambda}$$

$$P \text{ point intensity: } I_{\lambda}(r; \theta) = B_{\lambda}(T_{star}) e^{-\tau_{\lambda}} \Theta(r_{star} - r \sin \theta) + I_{layer \lambda}$$

If we consider:

No scattering:

Thermodynamic equilibrium:

$$I_{layer \lambda} = \int_0^{\tau_{\lambda}} S_{\lambda} \exp(\tau_{\lambda} - \tau_{\lambda}') d\tau_{\lambda}'$$

$$\kappa_{s\lambda} = 0$$

$$S_{\lambda} \approx B_{\lambda}(T_{layer})$$

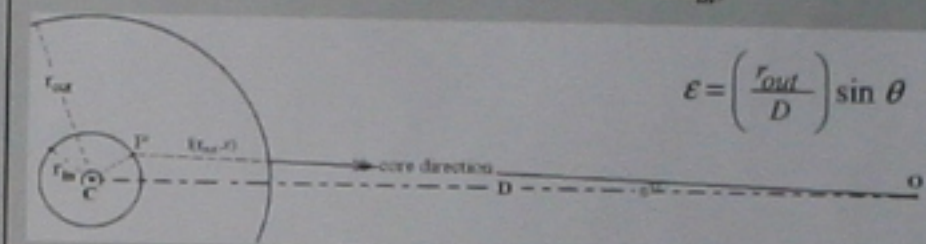
If we consider: an optically thin layer $I_{\lambda}(r_{out}; \theta) = B_{\lambda}(T_{star}) \Theta(r_{star} - r_{out} \sin \theta) + B_{\lambda}(T_{layer}) \tau_{\lambda}(r_{out}, \theta)$

Expression of the global optical depth for a geometrically thin layer:

$$\tau_{\lambda}(r_{out}; \theta) = \kappa_{\lambda}^{in} \left(\frac{r_{in}}{r_{out}} \right)^{\beta} I(r_{out}, \theta) \quad \text{with:} \quad \kappa_{\lambda}^{in} = \kappa_{\lambda}^{in} \left(\frac{\lambda}{\lambda_0} \right)^{-\beta}$$

and: $I(r_{out}; \theta) = r_{out} \cos \theta - \Theta(r_{in} - r_{out} \sin \theta) \sqrt{r_{in}^2 - r_{out}^2 \sin^2 \theta}$ layer geometrical thickness

« core » direction ($0 \leq \theta \leq \epsilon_{in}$)



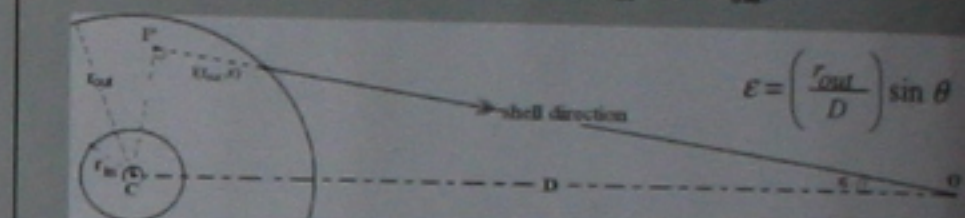
Output radiation dominated by material located at the inner boundary (P').

Temperature in P' equal to the inner boundary temperature:

$$T_{layer} = T_{in}$$

$$I_{\lambda}^{core}(\epsilon) = B_{\lambda}(T_{in}) \kappa_{\lambda}^{in} \left(\frac{\epsilon_{in}}{\epsilon_{out}} \right)^{\beta} D \left[\sqrt{\epsilon_{out}^2 - \epsilon^2} - \sqrt{\epsilon_{in}^2 - \epsilon^2} \right]$$

« shell » direction ($\epsilon_{in} \leq \theta \leq \epsilon_{out}$)



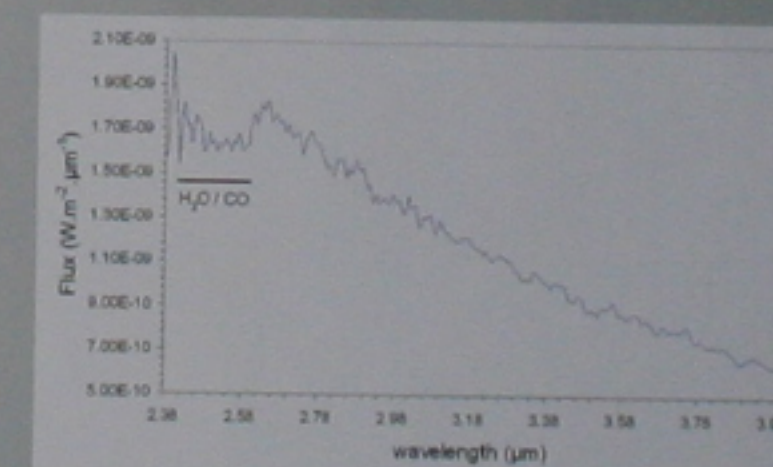
Hottest and most numerous material located at the P' point, closest from the center C.

Temperature in P' defined at the thermodynamical equilibrium:

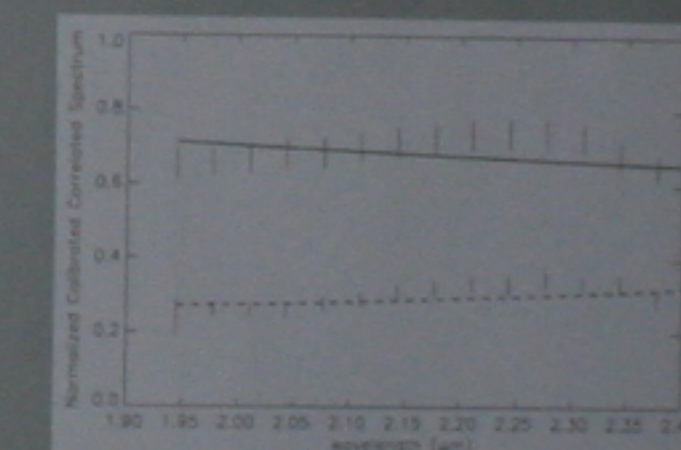
$$T_{layer} = T_{in} \left(\frac{\epsilon}{\epsilon_{in}} \right)^{\frac{\beta}{\beta+4}}$$

$$I_{\lambda}^{shell}(\epsilon) = B_{\lambda} \left(T_{in} \left(\frac{\epsilon}{\epsilon_{in}} \right)^{\frac{\beta}{\beta+4}} \right) \kappa_{\lambda}^{in} \left(\frac{\epsilon_{in}}{\epsilon_{out}} \right)^{\beta} D \sqrt{\epsilon_{out}^2 - \epsilon^2}$$

VII. Two-layer modeling

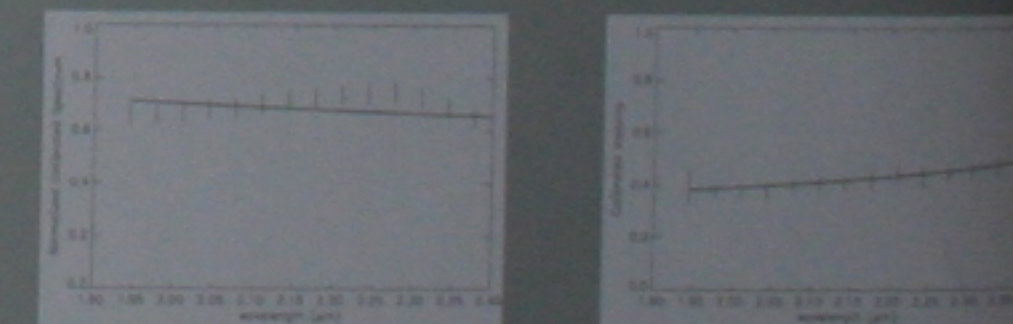


ISO/SWS spectrum of π^1 Gru. Absorption feature between 2.4 and 2.6 μ m corresponds to H₂O or CO molecules.



Best fit of the normalized correlated flux given by the two-layer analytical model

Minimization of the correlated spectrum ($F \times V$) simultaneously fits the visibility and the spectrum:



Parameters	Internal layer	External layer
Optical depth	1.58 \pm 0.08 (@2.4 μ m)	0.24 \pm 0.01 (@2.2 μ m)
Inner boundary temperature (K)	1391 \pm 18	1551 \pm 15
Inner boundary radius (mas)	20.5 \pm 0.2	40.2 \pm 0.8
Outer boundary radius (mas)	23.0 \pm 0.2	89 \pm 5

VIII. Conclusion

Interferometry gives complementary knowledge to the spectrophotometric study of the circumstellar environment. In the case of π^1 Gru, VLTI/AMBER observations give the physical and geometrical parameters associated to the internal and external layers. Both layers were suspected by ISO/SWS spectrometric measurements.